1014-52-1230 Ralph Howard\* (howard@math.sc.edu), Department of Mathematics, University of South Carolina, Columbia, SC 29208, and Daniel Hug (daniel.hug@math.uni-freiburg.de), Mathematisches Institut, Universität Freiburg, Freiburg, Germany. Convex Bodies with Constant Projection Functions.

Let  $G_k(\mathbf{R}^n)$  be the Grassmannian of all k-dimensional subspaces of  $\mathbf{R}^n$ . If K is a convex body in  $\mathbf{R}^n$ , then the kprojection function of K is the function that maps  $U \in G_k(\mathbf{R}^n)$  to the k dimensional volume of the orthogonal projection, K|U, of K onto U. When this function is constant K is said to have **constant** k-brightness. Constant 1-brightness is the familiar case of constant width.

**Theorem.** If  $n \ge 5$  and the convex body K in  $\mathbb{R}^n$  has constant width and constant 3-brightness, then K is a Euclidean ball.

The main point is that no regularity assumptions are being made about K. (Received September 27, 2005)