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**Gail Ratcliff\*** (ratcliffg@ecu.edu) and **Chal Benson** (bensenf@ecu.edu). *Geometric models for the spectra of certain Gelfand pairs associated with Heisenberg groups.*

Let  $K$  be a compact Lie group acting on a finite dimensional Hermitian vector space  $V$  via some unitary representation. Then  $K$  acts by automorphisms on the associated Heisenberg group  $H_V = V \times \mathbb{R}$  and we say that  $(K, H_V)$  is a Gelfand pair when the algebra  $L_K^1(H_V)$  of integrable  $K$ -invariant functions on  $H_V$  commutes under convolution. In this situation an application of the Orbit Method yields an injective mapping  $\Psi$  from the space  $\Delta(K, H_V)$  of bounded  $K$ -spherical functions on  $H_V$  to the space  $\mathfrak{h}_V^*/K$  of  $K$ -orbits in the dual of the Lie algebra of  $H_V$ . We show that  $\Psi$  is a homeomorphism onto its image provided that the action of  $K$  on  $V$  is “well-behaved” in a sense made precise in this work. Our result encompasses a widely studied class of examples arising in connection with Hermitian symmetric spaces. (Received September 15, 2010)