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Kitaev, Liese, Remmel and Sagan recently defined generalized factor order on words with letters from a poset  $(P, \leq_P)$  by setting  $u \leq_P w$  if there is an embedding of  $u$  into  $w$ . If  $P$  is the positive integers with the usual ordering, they defined the weight of a word  $u = u_1 \dots u_n$  to be  $\text{wt}(u) = x^{\sum_{i=1}^n u_i} t^n$  and introduced the weight generating function  $F(u; t, x) = \sum_{w \geq_P u} \text{wt}(w)$ . They defined two words  $u$  and  $v$  to be Wilf equivalent if and only if  $F(u; t, x) = F(v; t, x)$ , and provided combinatorial proofs of many Wilf equivalences. We continue this study by giving an explicit formula for a related generating function in the event that  $u$  has a certain factorization, allowing us to classify Wilf equivalence for all words of length 3. We then extend Kitaev, Liese, Remmel and Sagan's ideas to the poset  $\mathcal{P}_k$ , defined as the positive integers with the ordering  $i <_k j$  if  $i < j$  and  $i \equiv j \pmod k$  for  $k \geq 2$ , providing many analogues of their results in this new setting. We also give an analogue of our generating function formula, valid for a rich class of words, and classify Wilf equivalence for permutations of  $n$  with  $n \leq 2k$ , and for all words of length 3 in this context. (Received September 21, 2009)