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*Heegaard surfaces and the distance of amalgamation.*

Let  $M_1$  and  $M_2$  be orientable irreducible 3-manifolds with connected boundary and suppose  $\partial M_1 \cong \partial M_2$ . Let  $M$  be a closed 3-manifold obtained by gluing  $M_1$  to  $M_2$  along the boundary. We show that if the gluing homeomorphism is sufficiently complicated, then  $M$  is not homeomorphic to  $S^3$  and all small-genus Heegaard splittings of  $M$  are standard in a certain sense. In particular,  $g(M) = g(M_1) + g(M_2) - g(\partial M_i)$ , where  $g(M)$  denotes the Heegaard genus of  $M$ . This theorem can also be extended to manifolds with multiple boundary components. (Received August 18, 2008)