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John C. Baez* (baez@math.ucr.edu), Department of Mathematics, University of California, Riverside, CA 92521. *Classifying Spaces for Topological 2-Groups.*

Categorifying the concept of topological group, one obtains the notion of a topological 2-group. This in turn allows a theory of “principal 2-bundles” generalizing the usual theory of principal bundles. It is well-known that under mild conditions on a topological group G and a space M , principal G -bundles over M are classified by either the Čech cohomology $H^1(M, G)$ or the set of homotopy classes $[M, BG]$, where BG is the classifying space of G . Here we review work by Bartels, Jurco, Baas-Bökstedt-Kro, Stevenson and myself generalizing this result to topological 2-groups. We explain various viewpoints on topological 2-groups and the Čech cohomology $H^1(M, \mathbf{G})$ with coefficients in a topological 2-group \mathbf{G} , also known as “nonabelian cohomology”. Then we sketch a proof that under mild conditions on M and \mathbf{G} there is a bijection between $H^1(M, \mathbf{G})$ and $[M, B|\mathbf{G}|]$, where $B|\mathbf{G}|$ is the classifying space of the geometric realization of the nerve of \mathbf{G} . (Received September 08, 2008)