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**Harvey Cohn\*** ([hcohn@ccrwest.org](mailto:hcohn@ccrwest.org)), IDA Center for Communications Research, 4320 Westerra Court, San Diego, CA 92121. *Abelian Manifolds of arbitrary genus with Complex Multiplication*. Preliminary report.

Given a companion ( $g \times g$ ) matrix  $S$  for an irreducible monic equation with  $g$  real roots (listed in decreasing order) and integral matrices  $A, B$  commuting with  $S$ . Then we solve the matrix equation  $W^2 - AW + B = 0$  (after diagonalizing by the Vandermondian). The diagonalized values of  $W$  are assumed totally complex with alternating signs for the imaginary surds. We also need a unimodular matrix  $U$  for which both  $U$  and  $US$  are symmetric. Then  $Z = WU^{-1}$  is a Riemann Matrix ( $Z = Z^t, \Im Z \gg 0$ ) and the Abelian period matrix  $J = [E, Z]$  has the endomorphisms  $S, W$ , ( $SJ = [S, ZS^t], WJ = [ZU, ZA^t - BU^{-1}]$ ). The case  $g = 1$  is elliptic, and Humbert (1899) showed for  $g = 2$  this is the most general case (not likely for  $g > 2$ ). If the signs of the surds are chosen by group theory (not order)  $Z$  could be imaginary quadratic (but singular). (Received September 12, 2008)