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David F Anderson and **Ayman R Badawi*** (abadawi@aus.edu), American University of Sharjah, Dept. of Math, P.O. Box 26666, Sharjah, 00000, United Arab Emirates. *On n -absorbing ideals of commutative rings.* Preliminary report.

Let R be a commutative ring with $1 \neq 0$ and n a positive integer. In this paper, we study two generalizations of a prime ideal. A proper ideal I of R is called an n -absorbing (resp., strongly n -absorbing) ideal if whenever $x_1 \cdots x_{n+1} \in I$ for $x_1, \dots, x_{n+1} \in R$ (resp, $I_1 \cdots I_{n+1} \subseteq I$ for ideals I_1, \dots, I_{n+1} of R), then there are n of the x_i 's (resp., n of the I_i 's) whose product is in I . We investigate n -absorbing and strongly n -absorbing ideals, and we conjecture that these two concepts are equivalent. In particular, we study the stability of n -absorbing ideals with respect to various ring-theoretic constructions and study n -absorbing ideals in several classes of commutative rings. For example, in a Noetherian ring every proper ideal is an n -absorbing ideal for some positive integer n , and in a Prüfer domain, an ideal is an n -absorbing ideal for some positive integer n if and only if it is a product of prime ideals. (Received September 04, 2008)