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**Hong-Jian Lai, Liming Xiong and Huiya Yan\*** (hyan@math.wvu.edu), 320 Armstrong Hall,  
Dept. of Math, West Virginia University, Morgantown, WV 26506. *Bounded number of  
components of 2-factors in line graphs.*

A 2-factor is a 2-regular spanning subgraph of a graph  $G$ . A lot of results on the components of a 2-factor in  $G$  have appeared by studying the conditions on the minimum degree of the graph  $G$ . In this paper we avoid studying the minimum degree and get the following: if  $\max\{d(x), d(y)\} \geq \frac{n-\mu}{p} - 1$  holds for any  $xy \notin E(G)$  and  $|U| \neq 2$ , where  $U = \{v : d(v) < \frac{n-\mu}{p} - 1\}$ ,  $p \geq 2$  and  $\mu$  are two positive integers, then for  $n$  sufficiently large relative to  $p$  and  $\mu$ ,  $L(G)$  has a 2-factor with at most  $p + 1$  components. Moreover,  $L(G)$  has a 2-factor with at most  $p$  components if  $|U| \leq 1$ . This result is best possible. Especially, it extends a result saying that if  $\delta(G) \geq \frac{n}{p} - 1$ , i.e.,  $U = \emptyset$ , then  $L(G)$  has a 2-factor with at most  $p$  components. We also show the graphs above are  $(p + 2)$ -supereulerian, i.e., have a spanning even subgraph with at most  $p + 2$  components. (Received September 04, 2008)