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**Jens von Bergmann\*** (jvonberg@nd.edu), Department of Mathematics, 255 Hurley Hall, Notre Dame, IN 46556-4618. *Compactness for folded holomorphic maps.*

Let  $(X, \omega)$  be an oriented closed folded symplectic manifold, i.e.  $\omega$  is a closed 2-form vanishing transversely on a hypersurface  $Z$  (the “fold”) separating  $X$  into two parts  $X^+$  and  $X^-$ , so that the kernel of  $\omega$  induces a 1-dimensional foliation on  $Z$ . Every oriented 4-manifold admits a folded symplectic structure. We assume that the leaves of the foliation are the orbits of a free  $S^1$ -action. This happens frequently.

Folded holomorphic maps are pseudoholomorphic maps from Riemann surfaces with boundary into  $X^\pm$  with boundary on  $Z$ , satisfying appropriate boundary conditions. The boundary conditions are mediated by  $\mathcal{H}$ -holomorphic maps into the fold, i.e holomorphic maps over the parameter space given by  $H_1$  of the domain.

We prove compactness for the space of  $\mathcal{H}$ -holomorphic maps with fixed topological data and deduce that the space of folded holomorphic maps is compact in certain cases. (Received September 26, 2006)