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The *Bohr topology* on an infinite (discrete) abelian group G is the topology $\mathcal{T}^\#$ induced by $\text{Hom}(G, \mathbb{T})$. These facts are known: (a) $(G, \mathcal{T}^\#)$ is totally bounded (“precompact”, in the terminology of many authors); (b) $(G, \mathcal{T}^\#)$ is not pseudocompact—that is, it is not G_δ -dense in its (compact) Weil completion; (c) $\mathcal{T}^\#$ contains every totally bounded group topology on G , in particular every pseudocompact group topology.

The authors conjecture that for every abelian G which admits a pseudocompact group topology \mathcal{U} , the supremum of the set of all such topologies is $\mathcal{T}^\#$. They have established this, so far, in case (1) G is a torsion group, or (2) \mathcal{U} may be chosen so that $\omega \leq w(G, \mathcal{U}) \leq \mathfrak{c}$. (Received September 23, 2006)