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Gennady Lyubeznik* (gennady@math.umn.edu), Department of Mathematics, University of Minnesota, Minneapolis, MN 55455. *A counterexample to an open problem concerning a comparison between the quasicohherent and étale cohomological dimension of a scheme.*

Let U be an n -dimensional Noetherian scheme over a separably closed field and let $\text{cd}U$ (resp. $\acute{\text{e}}\text{cd}U$) be the quasicohherent (resp. étale) cohomological dimension of U . Is one of the integers $\text{cd}U$ and $\acute{\text{e}}\text{cd}U - n$ always at least as big as the other? We will explain why this question is interesting.

Counterexamples to the inequality $\text{cd}U \geq \acute{\text{e}}\text{cd}U - n$ have long been known. Whether the inequality $\acute{\text{e}}\text{cd}U - n \geq \text{cd}U$ always holds has been an open problem for a long time. We will describe a striking counterexample to this inequality. (Received September 20, 2006)