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Ian A. Rogers* (rogersia@rose-hulman.edu), 502 W White St., Freeburg, IL 62243. *On the Minimum Vector Rank of a Multigraph*. Preliminary report.

Given a multigraph G on the vertices $\{v_1, \dots, v_n\}$, in which all edges are multiedges, we associate a set of nonzero vectors $\vec{V} = \{\vec{v}_1, \dots, \vec{v}_n\}$ in \mathbb{C}^n to the vertices of G in the following manner: If vertices v_i and v_j are not joined then the corresponding vectors \vec{v}_i and \vec{v}_j are orthogonal. The rank of a vector representation \vec{V} is the maximum number of linearly independent vectors in \vec{V} . The *minimum vector rank* of G , $mvr(G)$, is the minimum rank among all vector representations of G .

We present methods for determining $mvr(G)$ if G is among certain classes of graphs, including perfect graphs and cycles. Further, we present upper and lower bounds on $mvr(G)$ for all multigraphs that contain only multiedges, and provide a conjecture on the exact value of $mvr(G)$ for such multigraphs. (Received July 28, 2006)