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D. Raghavarao, S. S. Shrikhande and M. S. Shrikhande* (shrik1m@cmich.edu),
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Matrices and Inequalities for Combinatorial Designs.*

In this paper we use incidence matrices of block designs and row-column designs to obtain proofs of some well known combinatorial inequalities. We introduce the concept of *nearly orthogonal* Latin squares by modifying the usual definition of orthogonal Latin squares: Let $v = 2m$ and L_1 and L_2 be Latin squares on symbols $\{0, 1, 2, \dots, 2m - 1\}$. Then L_1 and L_2 are said to be *nearly orthogonal* if on superimposition of L_2 and L_1 , the identical pairs do not occur together and symbols l and l' ($l \neq l'$) occur 2 times or 1 time according as $|l - l'| = m$ or not.

Theorem: Let L_1, L_2, \dots, L_t be t Latin squares of order $v = 2m$ on symbols $\{0, 1, 2, \dots, 2m - 1\}$ such that each pair of squares is nearly orthogonal. Then

$$t \leq \frac{v}{2} + 1, \text{ if } v \equiv 2 \pmod{4},$$

$$t \leq \frac{v}{2}, \text{ if } v \equiv 0 \pmod{4}.$$

The concept of nearly orthogonal latin squares opens up interesting combinatorial problems and is expected to be useful in planning experiments by statisticians. (Received September 21, 2006)