Suppose that \((R, m, k)\) is a normal complete local ring of dimension 2, and \(k\) is algebraically closed of characteristic zero. If \(X \to \text{spec}(R)\) is a resolution of singularities, then we associate a multi-graded \(R\)-algebra \(T_X = \oplus \Gamma(X, \mathcal{O}_X(-D_n))\), where the \(D_n\) are the effective divisors with exceptional support on \(X\). We show that \(T_X\) is a finitely generated \(R\)-algebra for all resolutions \(X\) if and only if \(R\) has a rational singularity. We also give criterion for a Poincare series associated to \(T_X\) to be rational. (Received September 29, 2004)