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Shinichiro Iai* (iai.shinichiro@s.hokkyodai.ac.jp). *Associated graded modules of canonical modules over almost Gorenstein local rings.*

This is a joint work with S. Goto. Let (A, \mathfrak{m}) be a Cohen-Macaulay local ring possessing the canonical module K_A of $d = \dim A > 0$. Assume A/\mathfrak{m} is infinite. Set $\mathcal{G}(\mathfrak{m}) = \bigoplus_{i \geq 0} \mathfrak{m}^i/\mathfrak{m}^{i+1}$ and $\mathcal{G}(\mathfrak{m}, K_A) = \bigoplus_{i \geq 0} \mathfrak{m}^i K_A/\mathfrak{m}^{i+1} K_A$. Let Q be a minimal reduction of \mathfrak{m} . Put $c = \mu_A(K_A)$. Then two results in the talk can be stated as follows.

Proposition. *Assume that A is an almost Gorenstein local ring. Then*

$$\mu_A(\mathfrak{m}^i K_A) - \mu_A(\mathfrak{m}^i) = (c - 1) \binom{d + i - 2}{d - 2}$$

for all integers $i \geq 0$. In particular, $\mu_A(\mathfrak{m} K_A) - \mu_A(\mathfrak{m}) = (c - 1)(d - 1)$.

Theorem. *Assume that A is an almost Gorenstein local ring. Then the following two conditions are equivalent.*

- (1) $\mathcal{G}(\mathfrak{m}, K_A)$ is a Cohen-Macaulay $\mathcal{G}(\mathfrak{m})$ -module.
- (2) $\mathcal{G}(\mathfrak{m})$ is a Cohen-Macaulay ring and $QK_A \cap \mathfrak{m}^2 K_A = Q\mathfrak{m} K_A$.

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