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**Oliver Y. Knitter\*** (oknitter@mail.sfsu.edu). *Understanding the Complexity of the Domain of Approximation of a Rational Tuple*. Preliminary report.

In continued fraction theory, a convergent is an irreducible rational number that “best” approximates a particular real number when compared to all rationals of smaller denominator. Generalizing this definition to include rational tuples of arbitrary length  $d$  shows that every point in  $\mathbb{Q}^d$  determines a domain of approximation: the set of all points in  $\mathbb{R}^d$  that are best approximated by this particular rational. It is known that the domain of approximation is star-convex and rectilinear. We shall examine the geometric properties of a carefully constructed set of sheared lattices in order to characterize the “corner points” of the domain of approximation, with a particular emphasis placed on identifying “primary” corners. The goal of this work is to show that for any 2-tuple  $(\frac{p_1}{q}, \frac{p_2}{q}) \in \mathbb{Q}^2$ , the number of primary corners in its corresponding domain of approximation is  $O(\log q)$ . (Received January 25, 2019)