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**Edray Herber Goins\*** ([edray.goins@pomona.edu](mailto:edray.goins@pomona.edu)), 610 North College Avenue, Claremont, CA 91711. *Visualizing Toroidal Belyĭ Pairs*. Preliminary report.

A Belyĭ map  $\beta : \mathbb{P}^1(\mathbb{C}) \rightarrow \mathbb{P}^1(\mathbb{C})$  is a rational function with at most three critical values; we may assume these values are  $\{0, 1, \infty\}$ . A Dessin d'Enfant is a planar bipartite graph obtained by considering the preimage of a path between two of these critical values, usually taken to be the line segment from 0 to 1. Such graphs can be drawn on the sphere by composing with stereographic projection:  $\beta^{-1}([0, 1]) \subseteq \mathbb{P}^1(\mathbb{C}) \simeq S^2(\mathbb{R})$ .

Replacing  $\mathbb{P}^1$  with an elliptic curve  $E$ , there is a similar definition of a Belyĭ map  $\beta : E(\mathbb{C}) \rightarrow \mathbb{P}^1(\mathbb{C})$ . The corresponding Dessin d'Enfant can be drawn on the torus by composing with an elliptic logarithm:  $\beta^{-1}([0, 1]) \subseteq E(\mathbb{C}) \simeq \mathbb{T}^2(\mathbb{R})$ . In this project, we use the open source **Sage** to write code which takes an elliptic curve  $E$  and a Belyĭ map  $\beta$  to return the Dessin d'Enfant of this map – both in two and three dimensions. We focus on several examples of Belyĭ maps which appear in the *L-Series and Modular Forms Database* (LMFDB). (Received September 15, 2020)