We discuss a recently discovered class of inverse semigroups called the inverse semigroups of self-similar graph actions. To describe this class, we characterized the idempotents, ideals, Green's Relations, and other properties common to inverse semigroups in general. Furthermore, we provide conditions that ensure a self-similar graph action is fundamental or 0 -disjunctive and, more generally, when it satisfies properties of inverse semigroups relevant to the study of $C^{*}$ algebras. (Received September 17, 2019)

