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**Ravi Vakil\*** (vakil@math.stanford.edu), Dept. of Mathematics, Stanford University, Stanford, CA 94305, and **Melanie Matchett Wood**. *Cutting and pasting in (algebraic) geometry*.

Given some class of “geometric spaces”, we can make a ring as follows.

- (i) (*additive structure*) When  $U$  is an open subset of such a space  $X$ ,  $[X] = [U] + [(X \setminus U)]$ ;
- (ii) (*multiplicative structure*)  $[X \times Y] = [X][Y]$ .

In the algebraic setting, this ring (the “Grothendieck ring of varieties”) contains surprising “stabilization” structure, connecting geometry to arithmetic and topology. I will discuss some remarkable statements about this ring (both known and conjectural), and present new statements (again, both known and conjectural). A motivating example will be polynomials in one variable. (This talk is intended for a broad audience.) This is joint work with Melanie Matchett Wood. (Received February 16, 2016)