## 1145-VP-2776 **Curtis Clark\*** (curtis.clark@morehouse.edu), 830 Westview Drive, Atlanta, GA 30314. Ultimately Economical Multigraphs. Preliminary report.

For positive integers  $\lambda$  and v,  $\lambda K_v$  denotes the complete multigraph with  $\lambda$  parallel edges between each pair of v distinct vertices. For vertices x and y in a multigraph F, the multiplicity of the edge xy is the number of edges that have x and y as their endpoints, denoted  $\mu_F(xy)$ . Let F be a multigraph with v(F) vertices and e(F) edges such that  $v(F) \leq v$  and  $\mu_F(xy) \leq \lambda$  for each pair of vertices x and y in F. In the F-achievement game on  $\lambda K_v$ , two players alternately color different edges of  $\lambda K_v$  so as to make a copy of F in his color. The multigraph F is achievable on  $\lambda K_v$  if a player can make a copy of F in his color. The least number of moves it takes for this player to win is the move number of F on  $\lambda K_v$ . The multigraph F is economical on  $\lambda K_v$  if the move number of F is equal to e(F). The multigraph F is ultimately economical multigraphs are determined, and it is shown that there are no forbidden subgraphs for ultimately economical multigraphs.

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