

1145-VP-233

**Monsikarn Jansrang\*** (jansr1m@cmich.edu). *Graph Complement Conjecture for the Minimum Semidefinite Rank*. Preliminary report.

Given an  $n \times n$  Hermitian matrix  $A = [a_{ij}]$  we associate a graph  $G(A)$  to the matrix  $A$  such that the set of vertices is  $\{v_1, \dots, v_n\}$  and the set of edges is  $E = \{\{v_i, v_j\} : a_{ij} \neq 0, i \neq j\}$ . The diagonal entries of  $A$  do not have an effect on  $G(A)$ . Let  $P(G) = \{A \in M_n(\mathbb{C}) : A^* = A, A \text{ is positive semidefinite, } G(A) = G\}$ . The *minimum semidefinite rank* of  $G$  is defined to be  $mr_+^{\mathbb{C}}(G) = \min\{\text{rank}(A) : A \in P(G)\}$ . If we restrict to real symmetric positive semidefinite matrices, the real minimum semidefinite rank is denoted by  $mr_+^{\mathbb{R}}(G)$ .

It has been conjectured that  $mr_+^{\mathbb{R}}(G) + mr_+^{\mathbb{R}}(\overline{G}) \leq |G| + 2$  where  $\overline{G}$  is the complement of the graph  $G$  and  $|G|$  is the number of vertices in  $G$ . This conjecture is called “Graph Complement Conjecture” and is denoted  $GCC_+$ . Given a graph  $G$ , the *shadow graph*  $S(G)$  is obtained from  $G$  by adding for each vertex  $u$  of  $G$ , a new vertex  $v$  called the shadow vertex of  $u$ , and joining  $v$  to the neighbors of  $u$  in  $G$ . In this talk we will present some new results about classes of shadow graphs that satisfy  $GCC_+$ . (Received August 23, 2018)