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Adam Boocher and **James Seiner***, james.seiner@stonybrook.edu. *Lower Bounds on Betti Numbers.*

Let R be a polynomial ring and I an ideal of R of height c . The *Betti numbers* $\beta_i(R/I)$ of R/I are the ranks of the modules in a minimal free resolution of R/I . Intuitively, these give some measure of the complexity of relations on the generators of I , and therefore we expect that there should be “at least as many relations as there are trivial ones,” an expectation which motivates a conjecture due to Buchsbaum-Eisenbud and Horrocks that $\beta_i(R/I) \geq \binom{c}{i}$. This conjecture however, has been open since 1977. In this talk I will discuss some variants of the conjecture— various weakenings and special cases, including our recent result that if I is a monomial ideal that is not a complete intersection then $\sum \beta_i(R/I) \geq 2^c + 2^{c-1}$. (Received September 20, 2018)