1145-11-33 **Benedict H. Gross*** (gross@math.harvard.edu), 142 N Rios Ave, Solana Beach, CA 92075. Complex multiplication: past, present, future.

The theory of complex multiplication, which studies both the arithmetic of elliptic curves and orders in imaginary quadratic fields, has a distinguished history. In the first lecture, I will recall the roots of this theory, starting with the ideas of Euler, Lagrange, and Gauss. I will review the main results obtained in the nineteenth century, and will end with a discussion of Heegner's paper on the class number one problem. (Received June 27, 2018)