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Natasha Dobrinen* (natasha.dobrinen@du.edu), University of Denver, Department of Mathematics, C.M. Knudson Hall 300, Denver, CO 80208. *Ramsey theory of the Henson graphs.*

A central question in the theory of homogeneous relational structures asks which structures have finite big Ramsey degrees. An infinite structure \mathbf{S} is *homogeneous* if any isomorphism between two finitely generated substructures of \mathbf{S} can be extended to an automorphism of \mathbf{S} . \mathbf{S} has *finite big Ramsey degrees* if for each finite substructure A of \mathbf{S} , there is a number $n(A)$ such that any coloring of the copies of A in \mathbf{S} , can be reduced down to no more than n colors on some substructure \mathbf{S}' isomorphic to \mathbf{S} . A main obstacle to a fuller development of this research area has been the lack of techniques and methods. In this talk, we present new work proving that all Henson graphs \mathcal{H}_k , the k -clique-free universal homogeneous graphs for $k \geq 3$, have finite big Ramsey degrees. Our proof provides a streamlined and unified approach to the Ramsey theory of Henson graphs, likely to extend to a large class of homogeneous structures with forbidden configurations. Central to the proof is the method of forcing, used to obtain a Ramsey theorem in ZFC for trees coding copies of \mathcal{H}_k , building on ideas of Harrington. (Received September 24, 2018)