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**Abbas Mahdi Alhakim\*** (aa145@aub.edu.lb). *Properties of Generalized de Bruijn Digraphs*. Preliminary report.

Generalized binary de Bruijn digraphs are regular directed graphs with  $N$  nodes, labeled  $0, 1, \dots, N-1$ , with edges from  $i$  to  $2i$  and  $2i+1 \pmod N$ . Traditional de Bruijn sequences, which have been used as pseudorandom sequences, correspond to Hamiltonian cycles when  $N$  is a pure power of 2. We discuss some interesting properties of these digraphs for general  $N$ , stressing the similarities with traditional de Bruijn digraphs. For instance, Hamiltonian cycles exist when  $N$  is even and they correspond bijectively to Eulerian circuits in digraphs of size  $N/2$ . Moreover, cycles of all orders exist, two disjoint cycles can be joined into one cycle via the cross-join operation, and we establish that a Hamiltonian cycle can be cross-joined repeatedly to make another arbitrary Hamiltonian cycle. We also show some interesting computational results. (Received September 22, 2015)