

1116-54-1048

**W. Kulpa** and **A. Szymanski\*** ([andrzej.szymanski@sru.edu](mailto:andrzej.szymanski@sru.edu)), Department of Mathematics, Slippery Rock University, Slippery Rock, PA 16057, and **M. Turzanski** and **D. Zagrodny**.

*L\*-operators and fixed-point theorems.* Preliminary report.

An  $L^*$ -operator on a topological space  $X$  is a function  $\Lambda$  satisfying the following condition: If  $A$  is a finite subset of  $X$  and  $\{U_x : x \in A\}$  is an open cover of  $X$ , then there exists  $\emptyset \neq B \subseteq A$  such that  $\Lambda(B) \cap \bigcap \{U_x : x \in B\} \neq \emptyset$ . The convex hull operator restricted to any convex subset of a topological vector space is an  $L^*$ -operator. The family of all sets closed under an  $L^*$ -operator is a convexity structure that generalizes  $L$ -structures due to Ben-El-Mechaiekh, et. al., and, independently, Park, 1998. Several types of fixed point theorems (e.g., Schauder-Tychonoff, Kakutani) and equilibrium type theorems (e.g., Nash, ESS) hold true for spaces endowed with continuous  $L^*$ -operators. We are going to review some of the older results and report on the most recent progress. (Received September 17, 2015)