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**Arthur E. Fischer\*** ([aef@ucsc.edu](mailto:aef@ucsc.edu)), Department of Mathematics, University of California, Santa Cruz, CA 95064. *New Results in Conformal Ricci Flow and the Conformally Reduced Einstein Evolution Equations.*

We discuss new results in *conformal Ricci flow*, which is a variation of the Ricci flow equations that modifies the *volume constraint* of those equations to a *scalar curvature constraint*. The resulting equations are named the *conformal Ricci flow equations* because of the role that conformal geometry plays in constraining the scalar curvature. These new equations are

$$\begin{aligned}\frac{\partial g}{\partial t} + 2(\text{Ric}(g) + \frac{1}{n}g) &= -pg \\ R(g) &= -1\end{aligned}$$

for a dynamically evolving metric  $g$  and a non-dynamical scalar field  $p$ , known as the *conformal pressure*. The conformal Ricci flow equations are analogous to the Navier-Stokes equations

$$\begin{aligned}\frac{\partial v}{\partial t} + \nabla_v v + \nu \Delta v &= -\text{grad } p \\ \text{div } v &= 0\end{aligned}$$

Just as the real physical pressure in fluid mechanics serves to maintain the incompressibility constraint of the fluid, the conformal pressure serves as a Lagrange multiplier to conformally deform the metric flow so as to maintain the scalar curvature constraint. The conformal Ricci flow equations can be thought of as Navier-Stokes style equations for the metric and also as a parabolic model for the *conformally reduced Einstein evolution equations*. (Received September 23, 2015)