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Christopher Ryan Loga* (loga@math.utk.edu), 2734 Bakertown Rd., Apt. 18, Knoxville, TN 37931. *An Extension Theorem for Matrix Weighted Sobolev Space on a Lipschitz Domain.* Preliminary report.

Let $D \subset \mathbb{R}^n$ be a bounded Lipschitz domain and $1 < p < \infty$. Suppose for each $x \in \mathbb{R}^n$ that $W(x)$ is an $m \times m$ positive definite matrix which satisfies the matrix A_p condition. For $k = 0, 1, 2, 3, \dots$ define the matrix weighted, vector valued, Sobolev space $L_k^p(D, W)$ with norm

$$\|\vec{f}\|_{L_k^p(D, W)}^p = \sum_{|\alpha| \leq k} \int_D \|W^{1/p}(D^\alpha \vec{f})\|^p dx$$

where $\vec{f} = (f_1, \dots, f_m) : D \rightarrow \mathbb{C}^m$. We show that for $\vec{f} \in L_k^p(D, W)$ there exists an extension $E(\vec{f}) \in L_k^p(\mathbb{R}^n, W)$ such that $E(\vec{f}) = \vec{f}$ on D and

$$\|E(\vec{f})\|_{L_k^p(\mathbb{R}^n, W)} \leq C \|\vec{f}\|_{L_k^p(D, W)}$$

for some constant independent of \vec{f} . This generalizes a known result for scalar A_p weights. (Received August 12, 2015)