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Let  $\Sigma_n$  be the symmetric group. For  $l \leq n$ ,  $\Sigma_l$  is naturally identified as a subgroup of  $\Sigma_n$ . Let  $k$  be an algebraically closed field of characteristic  $p$ . The algebra  $k\Sigma_n^{\Sigma_l}$  is the centralizer in the group algebra  $k\Sigma_n$  of  $k\Sigma_l$ . The authors are engaged in a project to find all simple  $k\Sigma_n^{\Sigma_l}$ -modules.

In the 1970's, James produced a construction of all simple  $k\Sigma_n$ -modules. He associates to each partition  $\lambda$  of  $n$  a  $k\Sigma_n$ -permutation module  $M^\lambda$ . The Specht module  $S^\lambda$  is the intersection of the kernels of certain homomorphisms with domain  $M^\lambda$ , and  $S^{\lambda^\perp}$  is the sum of the images of certain homomorphisms with codomain  $M^\lambda$ . The module  $D^\lambda := S^\lambda / (S^\lambda \cap S^{\lambda^\perp})$  is 0 or simple.

We investigate an analogous construction for  $k\Sigma_n^{\Sigma_l}$ , with role of the permutation modules played by the  $k\Sigma_n^{\Sigma_l}$ -modules  $\mathcal{M}^{\lambda,\mu} := \text{Hom}_{\Sigma_l}(M^\mu, M^\lambda_{k\Sigma_l})$ , where  $\lambda$  is a partition of  $n$  and  $\mu$  is a partition of  $l$ . For some choices of  $n$  and  $l$ , the results look very much like the classical results. (Received September 16, 2015)