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Andrey Rukhin* (andrey.rukhin@navy.mil). *On A Simple Recurrence In the Accelerated $3x + 1$ Minimum-Inverse Problem.*

The aim of this talk is to discuss a simple recurrence within the *Accelerated $3x + 1$ Minimum-Inverse Map*: we will consider the iterates of the function

$$\mathcal{F}(3k + t) = \begin{cases} 4k + 1, & t = 1 \\ 2k + 1, & t = 2 \end{cases}$$

on the set $\mathbb{Z} \setminus 3\mathbb{Z}$ where the argument $3k + t$ is an odd integer.

The talk will analyze the structural properties of rational expressions of the form

$$\frac{\sum_{0 \leq u < \tau} 3^u 2^{a(u)}}{3^\tau - 2^{a(\tau)}}$$

where the exponents $\{a(u)\}_{u=0}^{\tau}$ are non-negative integers; such rationals naturally arise when analyzing the functional orbits of \mathcal{F} . This talk will highlight a simple recurrence on the set $\{0, 1, 2, 3\}$ for generating the 3-adic canonical representations of such rational expressions; not only does this recurrence expedite the computations of such expressions when $\tau \gg 1$, but it also reveals a simple and deep connection between all of the iterate values within a functional orbit of \mathcal{F} . (Received September 10, 2015)