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**Shannon Talbott\*** (talbotts@moravian.edu). *A Game of Crowns: Layered Generalized Crowns and Chromatic Number.*

Given a map of the United States, what is the smallest number of distinct colors needed to color the map in such a way that no two border states have the same color? Mathematically, this is the infamous graph coloring problem, which is listed as one of Karp's twenty-one *NP* complete problems in his 1972 paper. For  $\mathbb{P}$  a finite partially ordered set (poset), we can associate with this poset a hypergraph  $\mathbf{H}_{\mathbb{P}}^c$  as well as a graph  $\mathbf{G}_{\mathbb{P}}^c$ , whose chromatic number is bounded above by the order dimension of  $\mathbb{P}$ . A well known result of Trotter and Felsner proves that  $\dim(\mathbb{P}) = \chi(\mathbf{H}_{\mathbb{P}}^c) \geq \chi(\mathbf{G}_{\mathbb{P}}^c)$ . We discuss extensions to the infinite family of graphs which arise from posets called layered generalized crowns, whose chromatic number has a known upper bound. (Received September 11, 2015)