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Let  $A$  be an  $n \times n$  matrix over a commutative ring  $R$  with identity. If there exist  $n \times n$  matrices  $P$  and  $Q$  invertible over  $R$  such that  $B = PAQ$  is a diagonal matrix  $\text{diag}(\alpha_1, \dots, \alpha_n)$ , where  $\alpha_i | \alpha_{i+1}$  in  $R$  for  $1 \leq i \leq n-1$  (where  $\alpha | 0$  for all  $\alpha \in R$ ), then we call  $B$  a *Smith normal form* (SNF) of  $A$ . Over a PID an SNF always exists and is unique up to multiplication by units. We will give a survey of some combinatorial aspects of SNF. The two main topics are (1) the distribution of the SNF of a random integer matrix, and (2) interesting examples of the SNF of combinatorially defined matrices. (Received August 28, 2015)