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**Nathaniel Karst, Jessica Oehrlein\*** (jessoehrlein@gmail.com), **Denise Sakai Troxell** and **Junjie Zhu**. *The minimum span of  $L(2, 1)$ -labelings of generalized flowers.*

Given a positive integer  $d$ , an  $L(d, 1)$ -labeling of a graph  $G$  is an assignment of nonnegative integers to its vertices such that adjacent vertices must receive integers at least  $d$  apart, and vertices at distance two must receive integers at least one apart. The  $\lambda_d$ -number of  $G$  is the minimum  $k$  so that  $G$  has an  $L(d, 1)$ -labeling using labels in  $\{0, 1, \dots, k\}$ . Informally, an amalgamation of two disjoint graphs  $G_1$  and  $G_2$  along a fixed graph  $G_0$  is the simple graph obtained by identifying the vertices of two induced subgraphs isomorphic to  $G_0$ , one in  $G_1$  and the other in  $G_2$ . A flower is an amalgamation of two or more cycles along a single vertex. We provide the exact  $\lambda_2$ -number of a generalized flower, which is the Cartesian product of a path  $P_n$  and a flower, or equivalently, an amalgamation of cylindrical rectangular grids along a certain  $P_n$ . In the process, we provide general upper bounds for the  $\lambda_d$ -number of the Cartesian product of  $P_n$  and any graph  $G$ , using circular  $L(d+1, 1)$ -labelings of  $G$  where the labels  $\{0, 1, \dots, k\}$  are arranged sequentially in a circle and the distance between two labels is the shortest distance on the circle. (Received August 20, 2015)