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Self-dual embeddings of $K_{4m,4n}$ in pseudosurfaces.

A pseudosurface is the result of identifying a finite number of points of a surface. A proper embedding of a graph G in a pseudosurface P is an embedding in which the regions of the complement of G in P are homeomorphic to discs and pinchpoints of P correspond to vertices in G . We say that a proper embedding of a graph G in a pseudosurface P is self dual if there exists an isomorphism from G to its topological dual. We give an explicit construction of a self-dual embedding of the complete bipartite graph $K_{4m,4n}$ in an orientable pseudosurface for all $m, n \geq 1$, which maximizes the number of umbrellas of each vertex and has the property that for any vertex v of $K_{4m,4n}$, there is a face of the constructed embedding that intersects all umbrellas of v . Leveraging these properties, and applying a lemma of Bruhn and Diestel, we apply a surgery introduced here and a different known surgery of Edmonds to each of our constructed embeddings for which at least one of $m, n \geq 1$, we show that there exist several distinct orientable and nonorientable pseudosurfaces with the same Euler characteristic that feature a self-dual embedding of $K_{4m,4n}$. (Received September 20, 2015)