We determine all the graphs whose flow polynomials have only integer roots. These graphs are exactly those graphs with cocycle matroids isomorphic to cycle matroids of chordal graphs with no $M\left(K_{5}\right)$-restrictions. As the flow polynomial of a planar graph is the chromatic polynomial of its dual graph, we have also determined all planar graphs whose chromatic polynomials have only integer roots. The proof is a conceptual one (requiring some easy inequalities for coefficients of polynomials with only real roots and some matroid theory). (Received August 03, 2014)

