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**Sam Northshield\*** ([northssw@plattsburgh.edu](mailto:northssw@plattsburgh.edu)). *Ford Circles and Spheres*. Preliminary report.

Given coprime non-negative integers  $a, b$ , the circle above and tangent to the  $x$ -axis at  $a/b$  with radius  $1/2b^2$  is called a Ford circle. One can alternatively parameterize these circles:

$$\{[a, b] : (a + b + c)^2 = a^2 + b^2 + c^2, \gcd(a, b, c) = 1\}$$

where  $[a, b]$  denotes the circle above and tangent to the  $x$ -axis at  $(a^2 + b^2)/(a + b)$  with radius  $1/2(a + b)$ . This generalizes nicely: let  $P_1, P_2$  and  $P_3$  denote the vertices of an equilateral triangle of side length 1, and let  $[a, b, c]$  denote the sphere above and tangent to the  $x, y$ -plane at  $(aP_1 + bP_2 + cP_3)/(a + b + c)$  with radius  $1/2(a + b + c)$ . Then the family of spheres

$$\{[a, b, c] : (a + b + c + d)^2 = a^2 + b^2 + c^2 + d^2, \gcd(a, b, c, d) = 1\}$$

shares many of the properties of the family of Ford circles. (Received September 22, 2011)