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**Xuhua Liu\*** (xzl0002@auburn.edu), Department of Mathematics and Statistics, 221 Parker Hall, Auburn University, Auburn, AL 36849, and **Tin-Yau Tam**. *Gradient Flows for the Minimum Distance to the Sum of Adjoint Orbits*.

Let  $G$  be a connected semisimple Lie group and  $\mathfrak{g}$  its Lie algebra. Let  $\mathfrak{g} = \mathfrak{k} \oplus \mathfrak{p}$  be the Cartan decomposition corresponding to a Cartan involution  $\theta$  of  $\mathfrak{g}$ . The Killing form  $B$  induces a positive definite symmetric bilinear form  $B_\theta$  on  $\mathfrak{g}$  defined by  $B_\theta(X, Y) = -B(X, \theta Y)$ . Given  $A_0, A_1, \dots, A_N \in \mathfrak{g}$ , we consider the optimization problem

$$\min_{k_i \in K} \left\| \sum_{i=1}^N \text{Ad}(k_i) A_i - A_0 \right\|,$$

where the norm  $\|\cdot\|$  is induced by  $B_\theta$  and  $K$  is the analytical subgroup of  $G$  with Lie algebra  $\mathfrak{k}$ . We obtain the gradient flow of a corresponding smooth function on the manifold  $K \times \dots \times K$ . Our results give unified extensions of several results of Li, Poon, and Schulte-Herbrüggen. They are also true for reductive Lie groups. (Received September 07, 2011)