

1077-11-1915

**Avraham Bourla\*** (avraham.bourla@trincoll.edu), Department of Mathematics, Trinity College, 300 Summit st., Hartford, CT 06106. *Recovering the sequence of approximation coefficients from a pair of successive pairs.*

Let  $\{a_n\}_1^\infty$  be the sequence of digits for the regular continued fraction expansion of an irrational number  $r$  and let  $\{\theta_n\}_0^\infty$  be its sequence of approximation coefficients (SAC) from Diophantine approximation. We will show that for all irrational numbers and  $n \geq 1$ , there is an integer valued function on two variables, whose value for both  $(\theta_{n-1}, \theta_n)$  and  $(\theta_{n+1}, \theta_n)$  is  $a_{n+1}$ . In tandem with a theorem due to Jurkat and Peyerimhoff, this will prove that there is a real valued function  $f$  on two variables such that  $\theta_{n+1} = f(\theta_{n-1}, \theta_n)$  and  $\theta_{n-1} = f(\theta_{n+1}, \theta_n)$ , revealing elegant symmetrical structure. In particular, the entire SAC can be recovered from a single pair of successive terms. (Received September 21, 2011)