Muhammad N Ahmad* (naeem@math.ksu.edu), Department of Mathematics, Kansas State University, Mahattan, KS 66506. Complex N-Spin Bordism of Semifree Circle Actions and Elliptic Genera.

We give the complete geometric description of rational bordism groups of compact complex N-spin manifolds admitting semifree circle actions. We find a computable condition under which a conjecture of Höhn [1], describing the ideal $I_*^{N,t}$ in rational complex N-spin bordism ring $\Omega_*^{U,N} \otimes \mathbb{Q}$ gererated by the bordism classes of complex N-spin manifolds admitting a semifree action of type t in terms kernels of elliptic genera of level N, is true. We apply the bordism analysis developed in this work to verify the condition for several values of N and t, and thereby prove the conjecture of Höhn for those values of N and t. Moreover, the machinery developed here gives a mechanism to explore the ideal $I_*^{N,t}$ for any given values of N and t in terms of kernels of elliptic genera of level N.

References:

[1] G. Höhn, Komplex elliptische Geschlechter und S^1 -äquivariante Kobordismustheorie, Diplomarbeit, Bonn, 1991. (Received September 21, 2010)