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Mohammad Javaheri* (javaheri@uoregon.edu), Mohammad Javaheri, Department of Mathematics, University of Oregon, Eugene, OR 97403. *Biased monotonic random walks in the plane*. Preliminary report.

A random walk in the plane is called monotonic β -biased if it moves from (a, b) to $(a + 1, b)$ with probability $1/(1 + \beta)$ and moves to $(a, b + 1)$ with probability $\beta/(1 + \beta)$. We study the problem of finding $\Phi_\beta(\alpha)$, the probability that a monotonic β -biased random walk starting from the origin crosses the line $y = \alpha x$ in the plane. We illustrate the rich combinatorial structure of this problem and show that if $\beta \geq \lceil \alpha \rceil$, then $\Phi_\beta(\alpha) = 1$. This result is a generalization of the fact that the one-dimensional standard random walk returns to the origin with probability 1. (Received September 12, 2007)