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A group  $G$  of automorphisms on a group  $V$  acts freely (also called fixed-point-freely or regularly) if no non-trivial element in  $G$  fixes a non-trivial element in  $V$ . The finite groups that act freely on an abelian group are exactly those that occur as Frobenius complements in some finite Frobenius groups. Infinite groups with a free action are less well understood: Every structural result for these groups that we know of requires some kind of finiteness assumption.

We show that every group of exponent  $2^m \cdot 3^n$  for natural numbers  $m, n$  with  $n \leq 2$  that acts freely on an abelian group is in fact finite. The proof involves some general facts on locally finite groups and a result on regular automorphisms of order 3 by A. Zhurтов. Using some elementary number theory we then obtain the corollary that every near-field whose multiplicative group has exponent  $2^m \cdot 3^n$  with  $n \leq 2$  is either a finite field of prime order or one of finitely many finite exceptions. (Received September 17, 2007)