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**Jason J Molitierno\*** (molitiernoj@sacredheart.edu), Sacred Heart University, Department of Mathematics, 5151 Park Avenue, Fairfield, CT 06825-1000. *Submatrices of Laplacian Matrices for Graphs with Cut Vertices.*

In graph theory, a graph  $\mathcal{G}$  on  $n$  vertices labeled  $1, \dots, n$  can be represented by an  $n \times n$  Laplacian matrix  $L$  where the diagonal entries  $\ell_{i,i}$  are each the degree of vertex  $i$ , and the off-diagonal entries  $\ell_{i,j}$  are  $-1$  if vertices  $i$  and  $j$  are adjacent and  $0$  otherwise. The submatrix  $L_i$  of  $L$  is obtained by deleting the row and column of  $L$  corresponding to vertex  $i$  of  $\mathcal{G}$ . If  $\lambda_n$  and  $\lambda_{n-1}$  are the largest eigenvalues of  $L$ , and  $\rho(L_i)$  is the largest eigenvalue of  $L_i$ , it follows from the interlacing theorem of eigenvalues that  $\lambda_{n-1} \leq \rho(L_i) \leq \lambda_n$ . In this talk, we will investigate the Laplacian matrices for graphs that contain cut vertices. By observing the values of  $\rho(L_i)$  when  $i$  represents a cut vertex, we will be able to classify such graphs  $\mathcal{G}$  into two categories based on whether  $\mathcal{G}$  contains a cut vertex  $i$  such that  $\rho(L_i) = \lambda_{n-1}$ . We will also investigate the values of  $\rho(L_i)$  for non-cut vertices and obtain some surprising results, especially when there exists a vertex such that  $\rho(L_i) = \lambda_n$ . (Received September 12, 2007)