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Anders J. Frankild, Sean Sather-Wagstaff and Roger Wiegand*

(rwiegand@math.unl.edu), Department of Mathematics, University of Nebraska, Lincoln, NE 68588-0130. *Ascent of module structures, vanishing of Ext, and extended modules.*

Let (R, \mathfrak{m}) and (S, \mathfrak{n}) be commutative Noetherian local rings, and let $\varphi : R \rightarrow S$ be a flat local homomorphism inducing an isomorphism on residue fields and satisfying the condition $\mathfrak{m}S = \mathfrak{n}$. Given a finitely generated R -module M , we show that M has an S -module structure compatible with its R -module structure (if and) only if the natural map $M \rightarrow S \otimes_R M$ is an isomorphism. Another necessary and sufficient condition is that $\text{Ext}_R^i(S, M) = 0$ for all $i > 0$. We consider also the question of which S -modules are extended from finitely generated R -modules. We show that when S is the Henselization of R every finitely generated S -module is a direct summand of an extended module, but that the analogous result fails for the completion. (Received September 14, 2007)