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Let  $p$  be a prime and  $Q$  be a polynomial with integer coefficients. We discuss the asymptotics of the  $p$ -adic valuation of the sequence  $t_n$ , defined by  $t_n = Q(n)t_{n-1}$  and the initial condition  $t_0 = 1$ . The example  $Q(n) = n$  deals with Legendre's classical formula for the valuation of  $n!$ . The case  $Q(n) = n^2 + 1$  is linked to the (conjectured non-integrality of the ) sequence  $x_n = (n + x_{n-1})/(1 - nx_{n-1})$ ,  $x_0 = 1$  for  $n \geq 5$ .

**Theorem.** Assume that, for every possible zero of  $Q$  modulo  $p$ , the derivative does not vanish (modulo  $p$ ). Then the  $p$ -adic valuation of  $t_n$  grows linearly in  $n$ . (Received September 14, 2007)