

1035-11-309

George W Grossman* (gross1gw@cmich.edu), Department of Mathematics, Central Michigan University, Mount Pleasant, MI 48859, and **Zinyun Zhu** (zhu1x@cmich.edu), Department of Mathematics, Central Michigan University, Mount Pleasant, MI 48859. *Sum of powers of integers and binomial coefficients.*

We derive a linear, nonhomogeneous, recurrence relation having two indices, that is, doubly-recurrent. We construct solutions which are rational expressions with indeterminate forms evaluated in a limit at a binomial coefficient.

The following problem is posed: express sums of the form $\sum_{i=1}^n i^p$, $p \in \mathbb{N}$, denoted $S_p(n)$, as a linear combination of binomial coefficients $\binom{an+b}{cn+d}$ for constants a, b, c, d and having integer coefficients independent of n , with the condition that at least one of the finite (increasing) sequences $\{an+b\}$ (over a, b) or similarly, $\{cn+d\}$ is strictly increasing. We offer solutions for $p = 2, 3$ and also derive an explicit nonhomogeneous recurrence relation satisfied by $S_p(n), p \geq 1$, based on Riemann sums. (Received August 31, 2007)