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**Curtis Cooper\*** (cooper@ucmo.edu), Dept. of Math. & Comp. Sci., University of Central Missouri, Warrensburg, MO 64093. *On the Natural Density of the  $k$ -Zeckendorf Niven Numbers.*

The  $k$ -generalized Fibonacci numbers are defined as

$$F_n^{(k)} = \begin{cases} 0, & \text{for } n < k - 1 \\ 1, & \text{for } n = k - 1 \\ \sum_{i=1}^k F_{n-i}^{(k)}, & \text{for } n \geq k. \end{cases}$$

The  $k$ -Zeckendorf representation of a positive integer is defined as

$$n = \sum_{i \geq k} \epsilon_i F_i^{(k)},$$

where  $\epsilon_i \in \{0, 1\}$  and for all  $i \geq k$  we have  $\epsilon_i \epsilon_{i+1} \cdots \epsilon_{i+k-1} = 0$ . Given this representation of a number  $n$  we say the  $k$ -Zeckendorf digital sum of  $n$  is  $z_k(n) = \sum_{i \geq k} \epsilon_i$  and if  $z_k(n) | n$  then  $n$  is called a  $k$ -Zeckendorf Niven number. We prove that the natural density of the  $k$ -Zeckendorf Niven numbers is zero. (Received September 19, 2007)