

XV

THE PRESIDENTS

Presidents of the Society were elected annually, until Dec., 1900, when, with the sixth P, biennial periods went into force. So it has remained ever since, with immediate reelection prohibited. The Society has had 24 presidents, each serving for two years except the second P, Dr. McClintock, who held the office for four consecutive terms. At the time of their first election to the office their ages varied from 38.6 (Fiske) to 62.8 (Newcomb), the average age being 49.7 years; for the last ten presidents, this age has been 51.6 years. Ten of the presidents have died and the average of their ages at the time of death was 72.2 years. Four presidents were born outside of the United States: one in Canada, two in England (one never naturalized), and one in Russia. Only two remained unmarried; three married Germans.

Most of the presidents have been men of national, or international, distinction. Seventeen have been members of the NAS; one has attained to a position in the Hall of Fame; two were Copley medalists of the RS London; one was a for. assoc. of the Acad. des Sci., Institut de France; one was a fellow, and two were foreign members of the RS London; five were elected correspondents of the Acad. des Sci., Institut de France; four, presidents of the AAAS; one, president of a great research institution; one, chm. of the Div. Phys. Sci. NRC; eight were awarded honorary degrees by foreign universities (Hill, Newcomb, E. H. Moore, Van Vleck, Brown, Veblen, Birkhoff, Snyder); ten were vice-presidents of AAAS and chairmen of Section A; three served as acting president or vice-president of their universities; seven have had books published in foreign languages—one P had books translated into Bohemian, Dutch, German, Japanese, Norwegian, Russian, Swedish; and one had his collected mathematical works published.

The names of the presidents, together with their periods of service, are as follows:

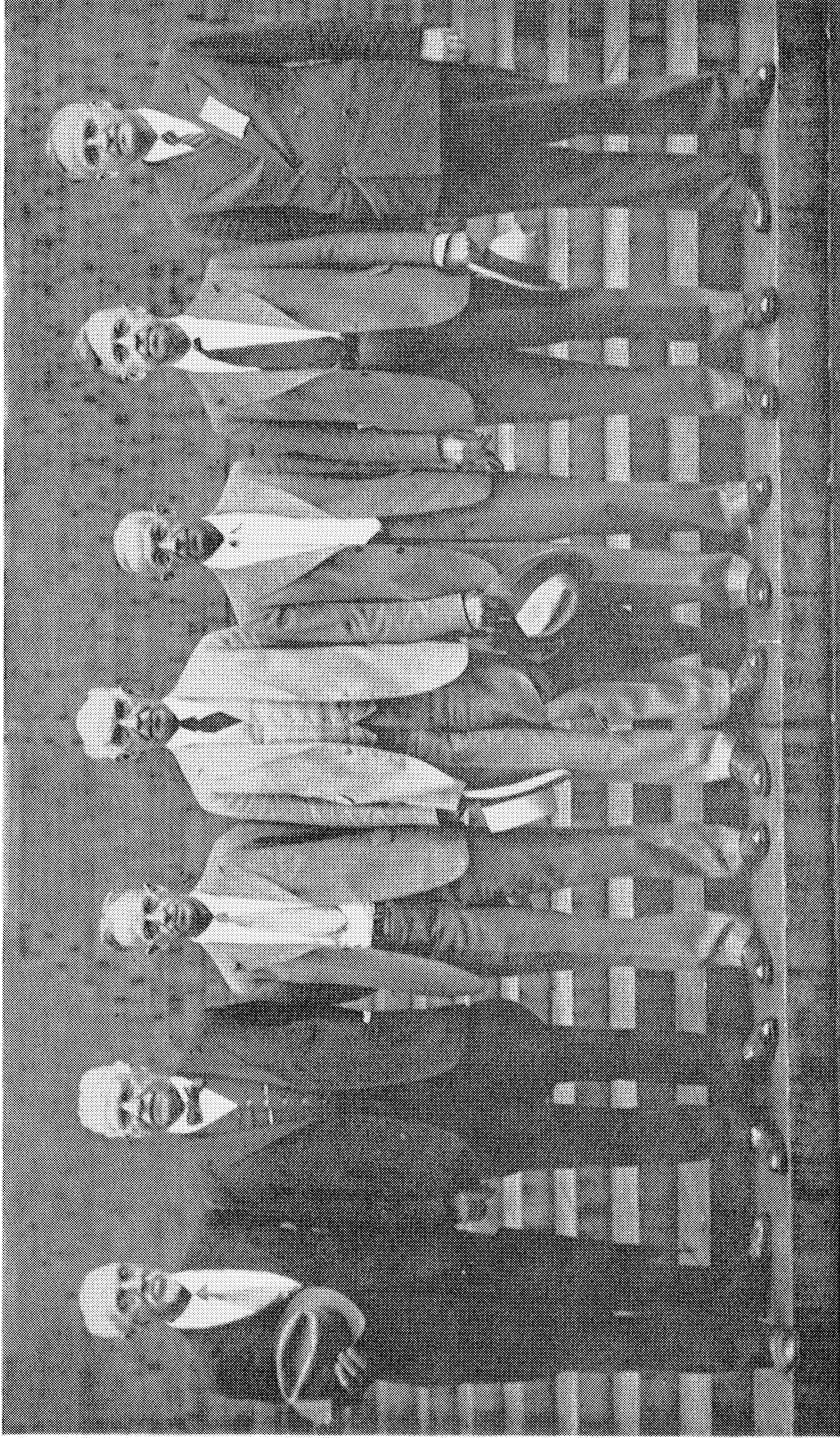
- | | |
|---|--------------------------------|
| 1. J. H. Van Amringe, 29 Dec. 1888-1890 | 13. E. W. Brown, 1915-1916 |
| 2. J. E. McClintock, 1891-1894 | 14. L. E. Dickson, 1917-1918 |
| 3. G. W. Hill, 1895-1896 | 15. F. Morley, 1919-1920 |
| 4. S. Newcomb, 1897-1898 | 16. G. A. Bliss, 1921-1922 |
| 5. R. S. Woodward, 1899-1900 | 17. O. Veblen, 1923-1924 |
| 6. E. H. Moore, 1901-1902 | 18. G. D. Birkhoff, 1925-1926 |
| 7. T. S. Fiske, 1903-1904 | 19. V. Snyder, 1927-1928 |
| 8. W. F. Osgood, 1905-1906 | 20. E. R. Hedrick, 1929-1930 |
| 9. H. S. White, 1907-1908 | 21. L. P. Eisenhart, 1931-1932 |
| 10. M. Bócher, 1909-1910 | 22. A. B. Coble, 1933-1934 |
| 11. H. B. Fine, 1911-1912 | 23. S. Lefschetz, 1935-1936 |
| 12. E. B. Van Vleck, 1913-1914 | 24. R. L. Moore, 1937-1938 |

Among living presidents Lefschetz is the youngest, and then Birkhoff, both b. in 1884; R. L. Moore, b. 1882, comes next. According to colleges or universities where the presidents received their first degrees, four each were from Columbia U. (Van Amringe, McClintock, Woodward, Fiske), and Harvard U. (Newcomb, Osgood, Bôcher, Birkhoff—see also Veblen, below); two each from U. Cambridge (Brown, Morley), Gettysburg C. (Eisenhart, Coble), U. Texas (Dickson, R. L. Moore), and Wesleyan U. (White, Van Vleck); one each from U. Chicago (Bliss), École Centrale (Lefschetz), U. Iowa and Harvard U. (Veblen), Iowa State C. (Snyder), U. Michigan (Hedrick), Princeton U. (Fine), Rutgers C. (Hill), and Yale U. (E. H. Moore).

Among the first twelve presidents E. H. Moore and Van Vleck were the only ones who were not from the "East"; among the next twelve there were five—Dickson, Bliss, Hedrick, Coble, R. L. Moore. The universities or organizations with which the presidents were connected when elected, are as follows: U. California at L. A. (Hedrick), U. Chicago (E. H. Moore, Dickson, Bliss), Columbia U. (Van Amringe, Woodward, Fiske), Cornell U. (Snyder), Harvard U. (Osgood, Bôcher, Birkhoff), U. Illinois (Coble), JHU (Newcomb, Morley), Mutual Life Insurance Co. of N. Y. (McClintock), Nautical Almanac Office (Hill, Newcomb), Princeton U. (Fine, Veblen, Eisenhart, Lefschetz), U. Texas (R. L. Moore), Vassar C. (White), U. Wisconsin (Van Vleck), Yale U. (Brown). Five of the presidents received their doctor's degrees under three other presidents, viz.: under E. H. Moore (Dickson, Veblen, Birkhoff); under Veblen at Chicago (R. L. Moore); and under Morley (Coble). Five presidents took their degrees under Klein (Bôcher, Fine, Van Vleck, Snyder, White). Among the others who guided presidents to the doctorate were H. A. Newton (E. H. Moore), M. Noether (Osgood), O. Bolza (Bliss), D. Hilbert (Hedrick), T. Craig (Eisenhart), W. E. Story (Lefschetz).

In 1903 when 80 of the leading mathematicians were listed according to their rated achievements at that time (*Amer. Men Sci.*, 5th ed.), 16 of the names of the presidents appeared in the following order: 1. E. H. Moore, 2. Hill, 3. Osgood, 4. Bôcher, 5. Newcomb, 6. Morley, 7. Brown, 8. White, 9. Dickson, 11. Van Vleck, 17. McClintock, 21. Woodward, 22. Fiske, 29. Fine, 38. Hedrick, 41. Snyder. Under Astronomy Newcomb and Hill were bracketed equal in first place among 50; and under Physics Woodward was no. 11 among 150.

In the following pages an attempt is made to bring together in very compact form an array of material which may suggest the career, achievements (and their recognition), and some characteristics, of each P. For the most part the Bibliographies of publications are fairly complete—about 2000 out of some 2400 items (395 by Newcomb were omitted). References to most "abstracts" have been omitted. The presidents published about 140 v. (a quarter of them by Newcomb) and nearly two scores of pamph-



FORMER PRESIDENTS OF THE SOCIETY AT HARVARD UNIVERSITY SEPTEMBER 1936

WHITE

FISKE

BLISS

OSGOOD

COBLE

DICKSON

BIRKHOFF

lets. It is believed that these Bibliographies, especially in the case of members of the NAS, may be very suggestive of the development of mathematical research in America during the past half century. A few brief notes draw attention to some of the most important items, or to others which, for one reason or another, appear to be of some interest. Doctoral dissertations and the Society's Presidential addresses are specially noted. The first of these addresses was given by McClintock, the second P, in 1894, at the close of his fourth term as P. Since the By-Laws thereafter stated that "it shall be the duty of each President to deliver an address before the Society at the annual meeting next succeeding his first election as president of the Society", the third, fourth and fifth presidents each served another year after the delivery of his address. Three changes in the By-Laws then introduced provided that the president be elected for a term of two years, that he be ineligible for immediate reelection, and that he be required to deliver an address "at the annual meeting at which his term of office expires." This applied to the succession of presidents sixth to nineteenth inclusive, but the following four exceptions had to be made: (i) on account of illness the delivery of President Osgood's address was postponed from Dec. 1906 to April 1907; (ii) President Bôcher was requested by the Council to postpone his address from the annual meeting of 1910 to an especially arranged meeting of the Society in April 1911; this wise move for promoting good feeling in the Chicago group was brought about by Professor Van Vleck; (iii) President Fine being absent in Europe during 1912-13, his address was delivered at the annual meeting of 1913 instead of that in 1912; (iv) because of President Snyder's absence in Europe at the time of the annual meeting in 1928, his retiring address was a feature of the following summer meeting. The next form of By-Law in this connection was equally inflexible, "It shall be the duty of the President to deliver an address . . . at the annual meeting one year after his term of office expires"; on this mandate Professor Hedrick, the twentieth P, delivered his retiring address in 1931. But the next retiring address was delivered by Professor Eisenhart at the annual meeting of 1932 because the By-Laws had once again been changed, stating that the address was to be given "at the close of his term of office or within one year thereafter." Such a By-Law from the first would, without special actions, have covered all exceptional cases which had earlier occurred.

Each living ex-president was a member of the Council of the Society from April 1900 to the end of 1923; since then, the period of such membership has been limited to the six years after the expiration of his presidential term. Thus there are at most three ex-presidents who are *ex officio* members of the Council.

In connection with the following sketches the "Sources" contain references to fuller information in different directions. There were ten "Presidents" at the summer meeting of 1936 at Harvard U. (Fiske, Osgood,

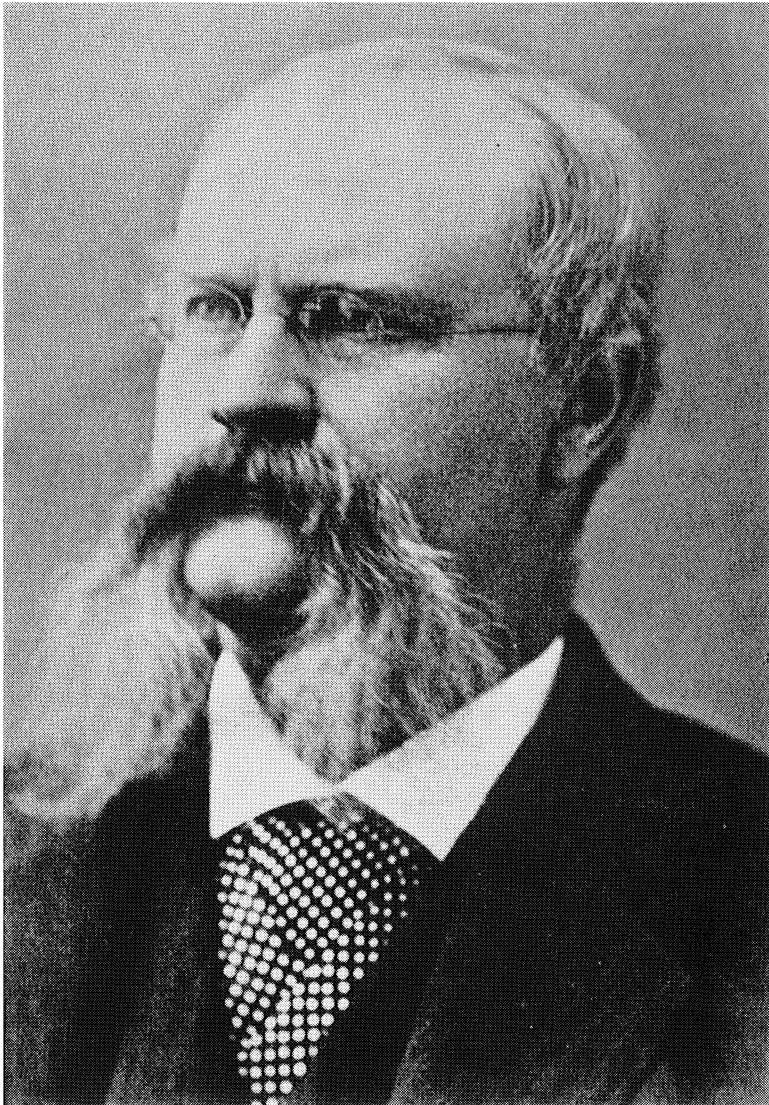
White, Brown, Dickson, Bliss, Birkhoff, Hedrick, Coble, Lefschetz). A group picture of seven of these, taken at that time, is reproduced in this v.

1. JOHN HOWARD VAN AMRINGE

CURRICULUM VITAE.—B. Philadelphia, Pa. 3 Apr. 1835 (not 1836); d. Morristown, N.J. 10 Sept. 1915. Educated by his father and at Montgomery Academy, N.Y., whence he entered Yale in 54. He remained two years. After a two-year interlude of teaching he entered Columbia C. (58–60, A.B. 60; tutor in math. 60–63, A.M. 63). At Columbia he was adjunct prof. 63–65, prof. of math. in the School of Mines 65–73, and in the School of Arts 73–10; emeritus prof. of math. 10–15; head of the dept. math. 92–10; dean of the School of Arts 94–96; dean of Columbia C. 96–10.

HONORS.—Secy. Alumni Assoc. Columbia C. early 70's. Hon. Ph.D. U. State of N.Y. 77. One of the charter members and first P NYMS Dec. 88–90; mem. its Council 91–93. Hon. L.H.D. Columbia C. 90. P Alumni Assoc. Columbia C. 91–93; P Alumni Council 95–13. Hon. LL.D. Union C. 95. Vestryman of the Parish of Trinity Church, New York 99–15. Acting P Columbia U. for a short time 99. Portrait painted by Eastman Johnson, now in South Hall, College Lib. 00; best portrait. P Columbia U. Club in New York City from its foundation to his death 01–15. Mem. board managers St. Luke's Hospital 01–15; VP 12–14. Mem. executive comm. N.Y. Hist. So. Dec. 05–Feb. 09. P Church Club of N. Y. 06–08. Hon. LL.D. Columbia U. 10. Bust executed by W. O. Partridge and two casts made, one for Hamilton Hall and one for the Columbia U. Club 11; the first of these was placed in the Van Amringe Memorial in the middle of the Van Amringe quadrangle in front of Hamilton Hall, in 22. This Memorial, a circular structure of classic design, was dedicated in 18; north and south of it are stone benches containing inscriptions taken from Van Am's speeches, (see J. W. Robson's *A Guide to Columbia University*, 1937, p. 91–92). VP Century Assoc. 12–15. P Alumni Federation 13–15. Among other positions of honor which he held are the following: trustee of the Protestant Episcopal So. for the Promotion of Religion and Learning in the State of New York; trustee of the N.Y. Protest. Episcopal Public School; mem. board managers, N.Y. Bible and Common Prayer Book So.; trustee General Theological Seminary of the Protest. Episcopal Church in the U.S.

BIOGRAPHICAL NOTES.—Prof. Van Amringe's grandfather was a soldier under Frederick the Great and emigrated from Holland to America in 1791. "Van Am," as he was universally called, is a unique figure in the history of Columbia U. "Probably no other teacher of his day was so loved and revered, and 'his boys' have delighted to perpetuate his memory at Columbia in song [there's a *Van Am Columbia Songster*, 1909], and stone, and bronze, and oils. Scarcely had he become an alumnus when he began to arouse an interest in the college among the alumni, and to restore the semi-moribund alumni association; imbuing others slowly with his own enthusiasm, he made the association a vital and vivifying influence in the whole university. . . . He was a fluent orator, speaking in 'exquisitely phrased sentences, rich in thought and suggestion, often imbued with deep feeling and genial humor.'" (M. H. Thomas). Although in no sense ranking with research mathematicians of his own day it was only natural that one of his prominence, occupying the position that he did, should have become our Society's first president. "In spite of life in a great city, he was a veritable provincial. . . . He knew almost nothing nor cared to know anything of any other educational institution in this country or



J. H. Van Orman

1890

the world. He was, therefore, the ideal college patriot, and consequently the idol of the students and alumni of the college, although he was quite a disciplinarian in his classroom. . . . He was a brave man and a perfectly unselfish one. He cared nothing for money; spent his salary before he received it; and was always having some accident, such as breaking an arm or a leg. His good wife once said to me that she trembled every time the doorbell rang, lest Howard should be brought in with a broken leg. He was a great smoker and a great frequenter of clubs. He was also something of a politician and was frequently to be found at the caucuses of his party. He was a good, staunch, reliable friend and very agreeable in social intercourse. No one could know the man and not love him." (Burgess). He was very fond of outdoor life and fishing and he spent many summers in the Adirondacks, some of them in the company of Judge Gildersleeve.

One of Columbia's most popular songs is the adaptation to Van Am (by the well-known author and editor, W. A. Bradley) of "John Peel," the fine old English hunting song:

D'ye ken Van Am, with his snowy hair,
 D'ye ken Van Am, with his whiskers rare,
 D'ye ken Van Am, with his martial air,
 As he crosses the Quad in the morning?

Refrain: For the sight of Van Am raised my hat from my head;
 And the sound of his voice often filled me with dread,
 Oh! I shook in my boots at the things that he said,
 When he asked me to call in the morning.
 Yes, I kenn'd Van Am—to my sorrow, too,
 When I was a Freshman of verdant hue;
 First a cut, then a bar, then an interview
 With the Dean in his den in the morning.
 But we love Van Am from our heart and soul;
 Let's drink to his health! Let's finish the bowl!
 We'll swear by Van Am through fair and through foul,
 And wish him "the top o' the morning!"
 D'ye ken Van Am, with his fine old way,
 Dean of Columbia many a day?
 Long may he live, and long may he stay
 Where his voice may be heard in the morning.

It is not a little moving to be present towards the close of a Columbia U. banquet when the great volume of the sonorous melody of this song rises and falls by candle light, and tears run down the furrowed faces of many "old grads," as their thought dwells on earlier contacts with Van Am.

SOURCES.—The best single source is *Columbia Alumni News*, 5 Nov. 1915, in which section 2, 42 p., is devoted to Van Am, containing portraits, a biography by J. B. Pine, memorial addresses by President Butler and Seth Low, the song quoted above, etc. M. H. Thomas, *DAB*, v. 19, 1936. *Nat. Cycl. Amer. Biog.*, v. 13, 1906, portrait. *Universities and their Sons*, v. 2, 1899, portrait. N. M. Butler, *Columbia Spectator*, 20 Apr. 1931. J. W. Burgess, *Reminiscences of an American Scholar*, 1934.

BIBLIOGRAPHY

1. Edited *General Catalogue* of Columbia University, 9 editions, 1865–1906. Based on the alumni necrology which he prepared for many years.
2. *Life Assurance and Savings Banks. A lecture delivered . . . in the Cooper Institute February 17, 1872*, New York, 1872, 32 p.
3. *A Plain Exposition of the Theory and Practice of Life Assurance, with a Brief Sketch of its History*, New York, 1874, 61 p. The substance of this pamphlet was prepared as an article for Johnson's *New Universal Cycl.*
4. *An Historical Sketch of Columbia College in the City of New York 1754–1876*, New York, 1876, ii+243 p.
5. Edited *Elements of Geometry and Trigonometry from the Works of A. M. Legendre adapted to the course of mathematical instruction in the United States* by Charles Davies, 1882, 275+134+62 p.; 1885, 291+150+71 p.; 1890, 291+150+71 p.
6. C. Davies, *Elements of Surveying and Levelling*, rev. by J. H. Van Amringe, New York, Chicago, 1883, 374+29+161 p.
7. "The school of mines," *School of Mines Quart.*, v. 10, 1889, p. 338–350.
8. "History of Columbia University," *Universities and their Sons*, New York, v. 1, 1898, p. 571–731. He was also the author or ed. of the sketches of Columbia men in v. 2–5, 1899–1900.
9. Address to the Alumni, Commencement 1898, *Columbia U. Quart.*, v. 1, 1898, p. 21–24.
10. "What the college buildings should be," *Columbia U. Quart.*, v. 1, 1899, p. 272–273.
11. "Columbia University and the education of women," *Church Eclectic*, New York, v. 28, 1900, p. 33–37.
12. Letters of Van Am in *Class Books* of 1900, 1902, 1904, *Five Year Class Book* [of Class of 1899] 1904, 1905, 1906, 1907, 1908, 1909, 1910; and also in the junior class *Columbian*, 1909, 1910, 1911, 1912. Van Am's portrait appeared in several of the v.
13. "Ogden N. Rood," *Columbia U. Quart.*, v. 5, 1902, p. 47–62.
14. "Charles King LL.D.," *Columbia U. Quart.*, v. 6, 1904, p. 121–137+portrait frontispiece.
15. "King's College and Columbia College" in *A History of Columbia University 1754–1904*, New York, 1904, p. 1–195.
16. "Columbia men in the making of the nation," *Columbia Mo.*, v. 2, 1905, p. 97–98 [Extract from an address at the sesquicentennial dinner of the Alumni].
17. "A letter from the dean," *Columbia Mo.*, v. 2, 1905, p. 209–210.
18. "Some reflections on the growth of Columbia College," *Columbia U. Quart.*, v. 9, 1906, p. 34–36.
19. "Henry Yates Satterlee," *Columbia U. Quart.*, v. 10, 1908, p. 198–199.
20. "Edward Mitchell," *Columbia U. Quart.*, v. 11, 1909, p. 342–343.
21. "George Gosman DeWitt," *Columbia U. Quart.*, v. 14, 1912, p. 176–178.

2. JOHN EMORY McCLINTOCK

CURRICULUM VITAE.—B. Carlisle, Pa. 19 Sept. 1840; d. Bay Head, N.J. 10 July 1916. Student at Dickinson C., Carlisle (54–56), Yale U. (56–57), Columbia U. (57–59, A.B. 59; tutor math. 59–60; A.M. 62). Student chemistry at U. Paris and U. Göttingen (61–62). U.S. consular agent at Bradford, Eng. 63–66. Connected with a banking firm in Paris 66–67. Actuary Asbury Life Ins. Co. of N.Y. 67–71; and Northwestern Mutual Life Ins. Co. Milwaukee 71–89. Actuary Mutual Life Ins. Co. of N.Y. (89–11; vice-pres. and trustee 06–11; consulting actuary 11–16).

HONORS.—Fellow Institute of Actuaries, London 74. Hon. Ph.D. U. Wisconsin 84. Hon. LL.D. Columbia U. 85. A founder and fellow ASA 89; mem. council 89–91. VP AMS 90. P AMS 91–94. VP ASA 91–95. Assoc. fellow AAcAS 92. Awarded second prize, for an essay (Bibl. no. 42), by the Institute of Actuaries, London 92. P ASA 95–97. Corresp. mem. Association des Actuaire Belges 96. VP for the U.S. of the Permanent Comm. of Intern. Congresses of Actuaries

96-16. Corresp. mem. Institut des Actuaire Français 96. Hon. LL.D. Yale U. 99. Governor So. Colonial Wars in the State of N.J. 00-04. Starred *Amer. Men Sci.* 06.

BIOGRAPHICAL NOTES.—Dr. McClintock was a son of John M'Clintock (not McClintock) whose parents were both born in county Tyrone, Ireland, but moved to Pennsylvania. This John M'Clintock was prof. of math. Dickinson College, Carlisle, Pa. 1837-40 and prof. of classics there 1840-48; it was he who collaborated with J. Strong in editing the great *Cyclopaedia of Biblical, Theological, and Ecclesiastical Literature*, (New York, 12 v., 1857-87). On his mother's side Dr. McClintock was of puritan ancestry, being a descendant of John Wakeman (d. 1661) of Hartford, Conn., whose parents were natives of Bewdley, England. J. Emory received his degree A.B. at Columbia, *honoris causa*, when only eighteen years of age, and some time before the rest of his class, because the authorities wished to meet an emergency by at once appointing him a tutor. But he resigned in 1860 to go to Paris where his father during the Civil War was in charge of the American chapel and of signal service to the Union cause.

Although our list of McClintock's publications is probably incomplete, it is much more extensive than anything of the kind previously published. It will be observed that thirty articles dealing with various actuarial questions were published during the years 1868-77. His services to the Northwestern helped greatly in developing its policy and in building up that company, and he became one of the best informed life insurance men in the country. His remarkable abilities and long experience "gave him a unique position in the insurance world in the stormy days of the Armstrong Investigation in 1905. His testimony before that committee [no. 70] was the most complete and comprehensive statement of the phases through which American life insurance passed since its early days . . . and the opinions which he then expressed on various subjects formed the basis of much of the legislation which followed." (Hutcheson). After his appointment in 1906 as vice-president of the Mutual he went to Europe to direct changes in the company's European agencies, made necessary because of recent legislative investigation and enactments. His testimony at this time before a comm. appointed by the House of Lords to investigate the necessity of requiring foreign companies doing business in Great Britain to deposit funds for the security of British policy holders (no. 71) did much to influence this comm. to report against any such action. His influence in stabilizing, and inspiring confidence in life insurance at this time was great, but he broke under the strain, and had to limit his activities after 1906. Then, and for many years earlier, he was universally recognized as the foremost actuary America had produced, one who had made epoch-making contributions to the theory of life insurance, and one whose judgment on all questions pertaining to his profession was accorded a weight attached to the views of no other. As a business executive also his broad and com-

prehensive views seldom failed to carry conviction. It was during his presidency of the Actuarial So. of America that the examination system for admission to the Society was inaugurated, and its success was largely due to his inspiration and efforts.

Of McClintock's 22 strictly mathematical papers 15 were published in *AJM*, 5 in *NY* and *AMS Bull.*, one (no. 66) in *AM* on a simplified solution of the cubic, and one of particular importance (no. 67) in *AMS Trans.*, on the nature and use of the functions employed in the recognition of quadratic residues. Eight of the papers appearing in *AJM* before the Society was founded included the remarkable essay on the calculus of enlargement (no. 31; see "Sources" below, for comment on a paper about this memoir by W. S. Nichols) which was an effort to present the theory of finite differences and the differential calculus from a unified point of view. The paper may be regarded as a precursor of attempts to consider difference equations as differential equations of infinite order. His other more important papers were a series of researches on solvable quintic equations (nos. 36, 37, 61), indicating remarkable clarity of vision and power of manipulation, and the one on quadratic residues (no. 67) already noted. In 1909 he had hoped, with the assistance of Mr. S. A. Joffe, to bring out a v. of his collected papers, but this plan never materialized. McClintock was one of the creative mathematicians of high rank flourishing before the Society came into existence. In 1903 when 80 of the leading mathematicians of the country were selected, McClintock was rated seventeenth, next after Cole. McClintock is known to have expressed regret that he had not followed an academic career, which would have permitted him to give a large share of his time to research and to the enjoyment of those mutually inspiring relations, so often existing between a teacher and his students. In such a direction he would probably have gone far. Professor Fiske, a friend of many years, has written, "McClintock never failed to stimulate and inspire everyone of scientific aptitude or taste with whom he came in contact." Aside from his scholarship he possessed those traits which constitute a really great man. Quiet and unassuming, he was ever ready to extend a helping hand to those who sought his counsel. No subject was too insignificant for him to discuss with the young inquirer. He always gave the impression of being thankful for an opportunity to impart the results of his own thought and experience.

McClintock arrived in New York from Milwaukee in the autumn of 1889 and became a member of the New York Mathematical Society in December. He had that year already participated in the founding of the Actuarial So. of Amer. Almost at once he was elected a VP of NYMS and in the following year its P, the only president in the Society's history to serve for four years, four consecutive terms. Numerous very notable achievements of the Society in this administration are set forth in chapter I. He was a voracious, omnivorous reader, including volumes of his-



Emory McClintock

1904

tory and fiction. Genealogy greatly interested him, and he spent much time in tracing his ancestors in Great Britain and America. For many years his home was at Kemble Hill, near Morristown, N. J.; one of his publications (no. 49) deals with Washington's camp in this neighborhood during the revolution. By his first wife, a Yorkshire lady, he had one son, Major John McClintock, of the U. S. Army, for some time military attaché of the American legation at the court of Austria-Hungary.

SOURCES.—E. McClintock, Autobiographical sketch of extraordinary interest (Bibl. no. 76)-*Appleton's Cycl. Amer. Biog.*, New York, v. 9, 1922, portrait. W. A. Hutcheson, T. B. Macaulay, W. S. Nichols, *ASA Trans.*, v. 17, 1916; it is hardly conceivable that Nichols was really informed on the subject (Bibl. no. 31) about which he was writing. T. S. Fiske, *AMS Bull.*, v. 23, 1917. *Intern. Ins. Encycl.*, v. 1, New York and London, 1910. H. F. Tyrrell, *Semi-centennial History of the Northwestern Mutual Life Insurance Co. of Milwaukee*, 1908, portrait. D. E. Smith, *DAB*, v. 11, 1933. *Amer. Men Sci.*, 2d ed., 1910 and 5th ed., 1933.

BIBLIOGRAPHY

1. "Accumulation formula," *Ins. Times*, v. 1, 1868, p. 306.
2. "Valuation of all kinds of policies by means of gross premiums alone," *Ins. Times*, v. 1, 1868, p. 306.
3. "Valuation of note policies on a cash basis," *Ins. Times*, v. 1, 1868, p. 378.
4. "Annuitants' mortality," *Ins. Times*, v. 1, 1868, p. 450.
5. "5 per cent commutation columns. British annuitants' table—males," *Ins. Times*, v. 1, 1868, p. 450.
6. "Improved accumulation formula," *Spectator*, v. 1, 1868, p. 274.
7. "Comparative valuation table," *Ins. Times*, v. 2, 1869, p. 111-112.
8. "Surrender value," *Ins. Times*, v. 2, 1869, p. 125.
9. "The contribution plan. A theoretical limitation," *Ins. Times*, v. 2, 1869, p. 211; "The contribution plan again," p. 515.
10. "On the iniquity of net valuations," *Ins. Times*, v. 2, 1869, p. 719.
11. "The contribution plan: its merits and defects," *Spectator*, v. 3, 1869, p. 75.
12. "Actual vs. assumed premiums," *Ins. Times*, v. 3, 1870, p. 23.
13. "The proposed reform in state valuations," *Ins. Times*, v. 3, 1870, p. 805. The index states incorrectly that the art. "Relative merit" in this v. was also by McClintock.
14. "Cash surrender values. Elizur Wright's proposed bill," *Ins. Times*, v. 4, 1871, p. 339.
15. "On the comparative importance of policies," *Ins. Times*, v. 4, 1871, p. 570a-570b.
16. "On the comparative importance of life policies," *Ins. Times*, v. 4, 1871, p. 733.
17. "On the comparative importance of life insurance policies," *Ins. Times*, v. 4, 1871, p. 857, 859, 861, and v. 5, 1872, p. 274.
18. "Formulae for dividend calculations," *Ins. Times*, v. 4, 1871, p. 657.
19. "Valuation formulae," *Spectator*, v. 7, 1871, p. 446-447.
20. "Suggestions on the use of Elizur Wright's calculating machine," *Ins. Times*, v. 5, 1872, p. 743.
21. "Arousing the sleepers," *Ins. Times*, v. 6, 1873, p. 131.
22. "Assessing expenses," *Ins. Times*, v. 6, 1873, p. 656.
23. "On insurance and deposit values," *Ins. Times*, v. 6, 1873, p. 839, 841-842; v. 7, 1874, p. 99.
24. "On the American ten-year non-forfeiture policies," *Inst. Act., Journ.*, v. 17, 1873, p. 301-304. Reprinted in *Ins. Times*, v. 6, 1873, p. 204-205.
25. "Proposition for ascertaining the real cost of life insurance," National Convention of Ins. Commissioners, *Proc.*, v. 5, 1874, p. 4-10. Reprinted in *Ins. Times*, v. 7, 1874, p. 677-678.

26. "On the computation of annuities on Mr. Makeham's hypothesis," *Inst. Act., Journ.*, v. 18, 1874, p. 242-247.
27. "The interest ratio," *Ins. Times*, v. 8, 1875, p. 31-32.
28. "Rules for calculating reserves," *Ins. Times*, v. 8, 1875, p. 408.
29. "On surrender values," *Ins. Times*, v. 8, 1875, p. 795-798.
30. "Net or gross values," *Ins. Times*, v. 10, 1877, p. 557.
31. "An essay on the calculus of enlargement," *AJM*, v. 2, 1879, p. 101-161.
32. "A new general method of interpolation," *AJM*, v. 2, 1879, p. 307-314.
33. "On a theorem for expanding functions of functions," *AJM*, v. 2, 1879, p. 348-353; v. 3, 1880, p. 173.
34. "On certain expansion theorems," *AJM*, v. 4, 1881, p. 16-24.
35. "On the remainder of Laplace's series," *AJM*, v. 4, 1881, p. 96.
36. "On the resolution of equations of the fifth degree," *AJM*, v. 6, 1884, p. 301-315.
37. "Analysis of quintic equations," *AJM*, v. 8, 1886, p. 45-84
38. W. H. C. Bartlett, *Interest Tables used by The Mutual Life Insurance Co. of New York for the Calculation of Interest and Prices of Stocks and Bonds for Investment*, edited and enlarged by E. McClintock, New York, 3d ed., 1889, 51 p.; 4th ed., 1904, 54 p.
39. Response to toast, The English Institute of Actuaries, *ASA Trans.*, v. 1, pt. 1, 1889, p. 36-37.
40. "Formulae for ascertaining 'Contributions to surplus'," *ASA Trans.*, v. 1, pt. 4, 1890, p. 23-27; discussion, v. 2, 1891, p. 87-92.
41. Discussion of papers written by others, *ASA Trans.*, v. 1, pt. 4, 1890, p. 15, 16; v. 2, 1891-92, p. 92, 93-94, 103-104, 192-194, 207, 210, 212, 218, 409-410; v. 3, 1893-94, p. 152, 153-154, 156-157, 268-269, 278-279, 280, 282, 284, 285, 286-287, 371, 377-386, 393, 409, 417, 457-458, 471, 488-489, 497, 501, 504, 505; v. 4, 1895-96, p. 65, 66, 67, 71-73, 354, 357, 360, 467-468; v. 5, 1897-98, p. 162-164; v. 6, 1899-1900, p. 105-106, 208-209, 231, 433, 436-437; v. 7, 1901-03, p. 55-58, 60, 151-152, 155, 240, 257-259, 374-375, 467; v. 8, 1904, p. 76-78, 80-81, 145-146; v. 9, 1905-06, p. 62, 188; v. 10, 1908, p. 687-689; v. 12, 1911, p. 285-288; v. 13, 1912, p. 381.
42. *On the Effects of Selection. An Actuarial Essay*, New York, 1892, 89 p.; prize essay of Inst. Actuaries, pub., by permission, by the Mutual Life Ins. Co. of N.Y. Reprinted in *ASA Trans.* v. 3, 1893, p. 59-143.
43. "On the algebraic proof of a certain series," *AJM*, v. 14, 1892, p. 67-71.
44. "On independent definitions of the functions $\log(x)$ and e^x ," *AJM*, v. 14, 1892, p. 72-86.
45. "On lists of covariants," *NYMS Bull.*, v. 1, 1892, p. 85-91, 142, 236.
46. "On the non-Euclidean geometry," *NYMS Bull.*, v. 2, 1892, p. 21-33, 51.
47. "On the computation of covariants by transvection," *AJM*, v. 14, 1892, p. 222-229.
48. "On the early history of the non-Euclidean geometry," *NYMS Bull.*, v. 2, 1893, p. 144-147.
49. *Topography of Washington's Camp of 1780 and its Neighborhood*, a paper read . . . before the Washington Association of New Jersey at the meeting February 22, 1894, (Morristown (?), N.J., 1894), 39 p. incl. map.
50. "The past and future of the society," *AMS Bull.*, v. 1, 1895, p. 85-94. AMS ret. P add. 28 Dec. 1894.
51. "Theorems in the calculus of enlargement," *AJM*, v. 17, 1895, p. 69-80.
52. "A method for calculating simultaneously all the roots of an equation," *AJM*, v. 17, 1895, p. 89-110.
53. "On the rates of death loss among total abstainers and others," *ASA Trans.*, v. 4, 1895, p. 9-18; discussion, p. 161-168.
54. Presidential add. delivered October 10, 1895, *ASA Trans.*, v. 4, 1895, p. 258-269.
55. Presidential add. delivered April 30, 1896, *ASA Trans.*, v. 4, 1896, p. 369-376.
56. Presidential add. delivered October 8, 1896, *ASA Trans.*, v. 4, 1896, p. 472-480.
57. Presidential add. (not personally delivered), *ASA Trans.*, v. 5, 1897, p. 74-81; discussion, p. 176-185.

58. "On a solution of the biquadratic which combines the methods of Descartes and Euler," *AMS Bull.*, v. 3, 1897, p. 389-390; v. 4, 1898, p. 283.
59. "On the most perfect forms of magic squares, with methods for their production," *AJM*, v. 19, 1897, p. 99-120.
60. "General principles," *ASA Trans.*, v. 5, 1898, p. 283-299; discussion, v. 6, 1899, p. 96-99.
61. "Further researches in the theory of quintic equations," *AJM*, v. 20, 1898, p. 157-192.
62. "General plans, reserves and investments," p. 88-130 of *Insurance "A Text Book" a compilation of the addresses delivered before the twenty-ninth session of the National Convention of Insurance Commissioners, 1898*, compiled by W. A. Fricke, Milwaukee (?), 1898.
63. "Special tables for the estimation of mortality among annuitants," *ASA Trans.*, v. 6, 1899, p. 13-23, 152.
64. "Sur les recherches spéciales relatives aux pertes financières par rapport aux différents genres d'occupations, ou autrement" (in French), and also in English, "On special investigations for the comparison of death losses by occupations or otherwise," *Intern. Congress Actuaries, Proc.*, Paris, 1901, p. 420-427, 428-432. German abstract p. 433; "An English version" of the Congress paper is the following: "On the objects to be attained in future investigations of mortality and death loss," *ASA Trans.*, v. 6, 1900, p. 373-379.
65. "De l'évaluation des valeurs negociables comprises dans l'actif d'une compagnie" (in French), and also in English, "On the valuation of the negotiable securities included in the assets of a company," *Intern. Congress Actuaries, Proc.*, Paris, 1901, p. 498-501, 502-504. German abstract, p. 505.
66. "A simplified solution of the cubic," *AM*, s. 2, v. 2, 1901, p. 151-152.
67. "On the nature and use of the functions employed in the recognition of quadratic residues," *AMS Trans.*, v. 3, 1902, p. 92-109.
68. "On first-year mortality," *ASA Trans.*, v. 7, 1902, p. 186-190; discussion, p. 367-370.
69. "The logarithm as a direct function," *AMS Bull.*, v. 9, 1903, p. 467-469.
70. *Testimony of Emory McClintock, Actuary of The Mutual Life Insurance Company of New York, given before the Insurance Investigation Committee October 24, 25, 1905*, New York, 1905, 133 p.
71. *Statement of Emory McClintock, Vice-President and Actuary of The Mutual Life Insurance Company of New York*, London, 1906, 18 p. This begins: "To the Life Insurance Companies Select Committee, House of Lords. My Lords, I have compiled the following statement on behalf of The Mutual Life Insurance Company of New York in consequence of the invitation conveyed by the Secretary of your Lordship's Committee to my Company." See also Great Britain, House of Lords, *Minutes*, London, 1906, *Report* no. 194 on *Life Insurance Companies*, p. 11-22, 57-59.
72. "What are the prospects for the future of the Society?" *ASA Trans.*, v. 11, 1909, p. 20-26.
73. "Should not the work of the 'Specialized Mortality Investigation' be extended?" *ASA Trans.*, v. 11, 1909, p. 125-126.
74. "On annuity reserves," *ASA Trans.*, v. 11, 1909, p. 141-143; discussion, p. 367-374.
75. "Charles Gill: the first actuary in America," *ASA Trans.*, v. 14, 1913, p. 9-16; 212-237; v. 15, 1914, p. 11-35+portrait; 228-270.
76. "How I became an Actuary," *1889 ASA 1914. Twenty-fifth Anniversary Dinner* May 21, 1914, privately printed, by the ASA, New York, 1914, p. 15-24. Autobiographical sketch.

3. GEORGE WILLIAM HILL

CURRICULUM VITAE.—B. New York City 3 Mar. 1838; d. West Nyack, N.Y. 16 Apr. 1914. After attending the local school he went to Rutgers C. (A.B. 59); joined the staff of the Nautical Almanac Office (61), but after a year or two in Cambridge he obtained permission to do his work at his home in West Nyack until he moved to Washington, D.C. in 82 and worked there until 92, when he resigned his position and returned to West Nyack, where he spent the rest of his life. He lectured on Celestial Mechanics at Columbia U. for four years 93-95, and 98-00 (see Hill's

letter 8 July 1907 in Mittag-Leffler Library, Djursholm, Sweden, and *Columbia U. Bull.*, July 1894).

HONORS.—Hon. Ph.D. Rutgers C. 72. Assoc. fellow AAAS 73. Mem. NAS 74. For. assoc. RAS 78. Gold Medal RAS, for his researches on the lunar theory (see presidential address by J. W. L. Glaisher, *RAS MN*, v. 47, p. 203–220) 87. Hon. mem. Cambridge Phil. So. 90, “on the ground of his investigations on the secular motion of the moon’s perigee and other researches in the lunar theory;” elected at the same time as Brioschi, Gibbs, Kronecker, Lie, and Poincaré. Hon. Sc.D. U. Cambridge 92. Corresp. mem. Manchester Lit. and Hist. So. 92. Hon. LL.D. Columbia U. 94. P AMS 95–96. Hon. LL.D. Princeton U. 97. Corresp. mem. BAAS 97. Damoiseau triennial prize of 2000 francs of the Acad. des Sci., Institut de France 98, “pour l’ensemble de ses travaux mathématiques et astronomiques” (see report *CR Paris*, v. 127, 1898, p. 1080–1081). Hon. mem. N.Y. Acad. Sci. 98. For. mem. RS London 02. Mem. Amer. Phil. So. 03. Corresp. mem., sect. astr., Acad. des Sci., Institut de France 03. Schubert Prize (900 roubles, about \$461) by the Imperial Acad. Sci., St. Petersburg 05; this prize is the income of a foundation in honor of a former academician F. F. Schubert, a general in the infantry. Hill’s *Collected Mathematical Works*, 4v., published by the Carnegie Institution, Washington, D.C., 07–09. Hon. mem. LMS 07. Hon. fellow RS Edinburgh 08. Corresp. mem. Bavarian Acad. Sci. 08. Bruce Gold Medal, ASP 08; (eighth award, see presidential address by C. Burckhalter, *ASP Pub.*, v. 21, p. 51–60). Copley Medal RS London 09; the highest scientific honor in the gift of the British Empire. Assoc. mem. Acad. Royal des Sci. . . . de Belgique 09. For. mem. So. of Sci. in Christiania 10. Hon. mem. Calcutta Math. So. 10; at the same time as Osgood, Darboux and Picard. For. mem. Swedish Acad. Sci. 13. For. mem. Acad. Lincei 13. Centenary of Hill’s birth to be celebrated by a special number of *AJM*, Oct. 38; the following are among announced contributors: Birkhoff, E. W. Brown, Levi-Civita, Morse and Hedlund, v. Neumann, Toeplitz, Whittaker, Wintner.

BIOGRAPHICAL NOTES.—G. W. Hill’s grandfather John Hill (1770–1850), and father John William Hill (1812–79), were both born in England. The grandfather (see *DAB*) made his mark as an engraver in aquatint in London before emigrating to Philadelphia in 1816, and settling there. About 1846 he retired to a lonely upland farm near West Nyack. The father was a painter as well as an engraver and leader of the Pre-Raphaelite school in America. G. W. Hill’s brother John H. Hill (1839–1922), carried on the family tradition as an artist into the twentieth century.

G. W. Hill was one of the small number of outstanding research mathematicians among the Society’s presidents (Simon Newcomb is not counted among these), and none of them, except Birkhoff, has yet equalled Hill in the extensive international recognition of his eminence. In 1903 Newcomb wrote that Hill would “easily rank as the greatest master of mathematical astronomy during the last quarter of the nineteenth century.” In 1903 mathematicians also voted that E. H. Moore was the leading mathematician of the United States and Hill next; by the astronomers Hill and Newcomb were bracketed as first, and equal, in their field (see *Amer. Men Sci.*, 5th ed., p. 1269, 1272).

Hill’s first publication (Bibl. no. 1) appeared before he graduated from Rutgers, and less than twenty years elapsed when memoirs of epoch-making importance had appeared (nos. 31, 35). One of these, “Researches in the lunar theory”, was in the opening number of the newly founded *AJM*. “In this paper he calculated the first step in a new method for treating



G. W. Hill

1890

the motion of the moon under the attractions of the earth and sun. What proved to be equally important in the paper was the initiation of the 'periodic orbit'—an idea which has had a profound effect on the later development of celestial mechanics. In the hands of H. Poincaré, G. H. Darwin, and many others, it has greatly changed the approach to the study of the motions of three mutually attracting bodies. Its publication gave new life to a subject which had seemed to be marking time in merely securing higher numerical accuracy for the various gravitational theories of the bodies in the solar system, and the impetus is not yet exhausted. Another useful idea, the surface of zero velocity, is also set forth in this paper." (E. W. Brown, 1932). It is a surface consisting of various ovals and folds, giving certain limitations on the path of the moon, and therefore carrying on the stability of its motion one important step. "This memoir of but fifty quarto pages has become fundamental for the development of celestial mechanics in three different directions. It would be difficult to say as much for any other publication of its length in the whole range of modern mathematics, pure or applied. Poincaré's remark that in it we may perceive the germ of all the progress which has been made in celestial mechanics since its publication is doubtless fully justified." (Brown, 1915).

Hill's second great memoir (no. 31) was first published privately in 1877, in the year before the one to which reference has just been made; it was entitled, "On the part of the motion of the lunar perigee which is a function of the mean motions of the sun and moon," and while not so far reaching as the memoir first discussed above, from the point of view of future developments, it is even more remarkable as an exhibition of Hill's extraordinary power of analysis. His discussion leads him to the differential equation

$$\frac{d^2 p}{dt^2} + (\theta_0 + \theta_1 \cos 2t + \theta_2 \cos 4t + \dots) p = 0,$$

($\theta_0, \theta_1, \theta_2 \dots$ being constants), now known as "Hill's equation." A recent work (in Russian) of G. V. Bondarenko is entitled *Urvnenie Khilla i ego Primenenie v Oblasti Tekhnicheskikh Kolebanii* [*Hill's Equation and its Application in the Domain of Technical Oscillations*] (Moscow and Leningrad, 1936, 51 p.). For Lord Rayleigh's use of the equation in the discussion of physical questions see *Phil. Mag.*, v. 24, 1887, p. 145 or Rayleigh, *Scientific Papers*, v. 3, p. 1f. See also A. N. Krylov's recent volume, supplementary to v. 5-6 of his collected works (Moscow-Leningrad, 1937), p. 152-248; and E. L. Ince, "On a general solution of Hill's equation," *RAS MN*, v. 75, 1915, p. 436-448. This equation is equivalent to an infinite number of algebraic linear equations. By a most elegant method Hill showed how to develop the infinite determinant corresponding to these equations. This determinant is set equal to zero and the unknown is calculated correct to fifteen places of decimals. Hill's work with the infinite

determinant was wholly original; he knew nothing of Fürstenau's obscure publications of a few years earlier and if he had they would have aided him not at all in arriving at his results. Hill reduced his determinant to a convergent form, but the proof of the convergence was left to Poincaré (*SMF Bull.*, v. 14, 1886, p. 77). It is not a little interesting that J. C. Adams of Cambridge, England, the co-discoverer with Leverrier of the planet Neptune, had somewhat earlier than Hill constructed and evaluated the infinite determinant but he kept to the lunar problem while Hill extended the idea in a general manner (see *RAS MN*, v. 38, Nov. 1877, p. 43-49).

During his ten years in Washington, Hill worked constantly on the theories of Jupiter and Saturn, the most difficult parts of Newcomb's grandiose scheme involving all of the planets. The final result of Hill's achievement in this connection is one of the most important contributions to mathematical astronomy of the past century. Among his later papers is a noteworthy contribution (nos. 42 and 45) for calculating the effects of the planets on the motion of the moon. This is, in effect, a particular case of the problem of four bodies. (Brown). His biographies of Oliver and Hall (nos. 69, 97) are exceedingly interesting.

Among the unpublished manuscripts left behind by Hill, and now deposited in the library of Columbia University, are two of some interest. The earlier is a carefully written diary, illustrated with photographs, containing an account of the second expedition which he made to the north-west of Canada. The route followed took him, with a companion and guides, by rivers and lakes from Lake Superior to Hudson's Bay and back. It must have been sufficiently laborious, with the numerous portages of the canoes and supplies, but Hill apparently found enough spare energy to record everything of sufficient interest to appeal to him. The other manuscript, which must have cost him a great deal of labor, consists of the lectures delivered at Columbia University. They are a more or less complete, but very concise, account of the methods by which the motions of the moon and planets are computed.

Hill loved to roam through pathless woods, and the whole country in Virginia, for twenty miles about Washington, and for miles about West Nyack, was an open book to him. He knew all the trees and flowers, and in most cases their common and botanical names, genera, and species. He would walk twenty-five or thirty miles a day with little apparent exertion. Birds held not a little fascination for him. Nature's secrets, oddities, and beauties were objects of his constant search.

Hill never married. His chief characteristic was a single-minded devotion to the subject which he had made his own. A highly sensitive conscience was always apparent in his dealings with the world. "He never appeared to be melancholy or morose. To him the world was always bright. He could tell amusing stories of some hardships on his excursions, but not

a word of complaint. He mingled with his fellow men wherever he went, and was always glad to see his friends, both abroad and at his home. He freely helped all who asked his aid." (Hedrick).

In April 1936 Prof. Frank Schlesinger, the director of the Yale Observatory, and one of Hill's students at Columbia U., placed a bronze tablet on the Hill homestead in West Nyack. It bears the following inscription: George William Hill | 1838-1914 | Astronomer Mathematician | lived in this house.

SOURCES.—E. W. Brown: (a) *DAB*, v. 9, 1932; (b) with H. B. Hedrick and others, *NAS Biog. Mem.*, v. 8, 1916; (c) RS London, *Proc.* v. 91 A, 1915, reprinted in *AMS Bull.*, v. 21, 1915. E. W. Brown, E. T. Whittaker and others in *Encyk. d. Math. Wiss.*, v. 6.2.A and B, 1912-26 (see numerous references in alphabetical index). J. J[erwood], *RAS MN*, v. 75, 1915. S. C[hapman], *LMS Proc.*, s. 2, v. 14, 1915. H. Poincaré, *Collected Mathematical Works of George William Hill*, v. 1, Washington, D.C., 1905. F. Schlesinger, "Recollections of George William Hill," *ASP Pub.*, v. 49, 1937. S. Newcomb, *Reminiscences of an Astronomer*, 1903. T. Muir, *Theory of Determinants in the Historical Order of Development*, London, v. 3, 1920. Thieme—Becker, *Lexikon der bildenden Künstler*, v. 17, Leipzig, 1924. F. Weitenkampf, *American Graphic Art*, New York, 1912.

BIBLIOGRAPHY

All papers listed below except those with a star before the number are also included in Hill's *Collected Mathematical Works*.

1. "On the curve of a drawbridge," *Runkle's Math. Mo.*, v. 1, 1859, p. 174-175.
2. "Discussion of the equations which determine the position of a comet or other planetary body from three observations," *Runkle's Math. Mo.*, v. 3, 1860, p. 26-29.
3. "On the conformation of the earth," *Runkle's Math. Mo.*, v. 3, 1861, p. 166-182.
4. "Ephemeris of the great comet of 1858," *AN*, v. 64, 1865, p. 181-190.
5. "On the reduction of the rectangular coordinates of the sun referred to the true equator and equinox of date to those referred to the mean equator and equinox of the beginning of the year," *AN*, v. 67, 1866, p. 141-142.
6. "Discussion of the observations of the great comet of 1858, with the object of determining the most probable orbit," *AAcAS Mem.*, v. 9, 1867, p. 67-100.
7. *Tables to facilitate the Reduction of Places of the Fixed Stars. Prepared for the Use of the American Ephemeris and Nautical Almanac* (with J. H. C. Coffin and P. G. Bartlett), Wash., 1869 xxxviii+162 p. Also 2d ed. 1873.
8. "Determination of the elements of a circular orbit," *AAcAS Proc.*, v. 8, 1870, p. 201-209.
9. "New method for facilitating the conversion of longitudes and latitudes of heavenly bodies, near the ecliptic, into right ascensions and declinations, and vice versa," *AAcAS Proc.*, v. 8, 1870, p. 210-213.
10. *Tables of Venus, prepared for the use of the American Ephemeris and Nautical Almanac*, Wash., 1872, vi+37+81 p. Also an ed. dated 1873.
11. "Charts and tables for facilitating predictions of the several phases of the transit of Venus in December, 1874," U.S. Commission on the transit of Venus, 1874, *Papers relating to the Transit of Venus in 1874*, part 2, 1872, p. 7-48.
12. "On the derivation of the mass of Jupiter from the motion of certain asteroids," *AAcAS Mem.*, n.s., v. 9, 1873, p. 417-420.
13. "On the inequality of long period in the longitude of Saturn, whose argument is six times the mean anomaly of Saturn minus twice that of Jupiter minus three times that of Uranus," *AN*, v. 82, 1873, p. 83-88.
14. "A method of computing absolute perturbations," *AN*, v. 83, 1874, p. 209-224.
15. "On a long period inequality in the motion of Hestia arising from the action of the earth," *AN*, v. 84, 1874, p. 41-44.

16. "Solution of a problem in the theory of numbers," *Analyst*, v. 1, 1874, p. 27–28.
17. "A second solution of the problem of no. 8," *Analyst*, v. 1, 1874, p. 43–46.
18. "Remarks on the stability of planetary systems," *Analyst*, v. 1, 1874, p. 53–60.
- *19. "Answer to Prof. Brooks' query" [as to proof of formula $x/(A \log x - B)$ for the number of primes in any number x], *Analyst*, v. 1, 1874, p. 64–66. In his interesting reply Hill finds that "endeavouring to represent the distribution of primes below 3,000,000 by the formula," "A and B ought to have the values $A = 1.0093786$, $B = 1.210564$."
- *20. Solution of a problem, *Analyst*, v. 1, 1874, p. 70.
21. "Useful formulas in the calculus of finite differences," *Analyst*, v. 1, 1874, p. 141–145; v. 2, 1875, p. 8–9.
22. "Elementary treatment of the problem of two bodies," *Analyst*, v. 1, 1874, p. 165–170.
23. "The differential equations of dynamics," *Analyst*, v. 1, 1874, p. 200–203.
24. "On the solution of cubic and biquadratic equations," *Analyst*, v. 2, 1875, p. 4–8.
25. "On the equilibrium of a bar fixed at one end half way between two centers of force," *Analyst*, v. 2, 1875, p. 57–59.
26. "The deflection produced in the direction of gravity at the foot of a conical mountain of homogeneous density," *Analyst*, v. 2, 1875, p. 119–120.
27. "On the development of the perturbative function in periodic series," *Analyst*, v. 2, 1875, p. 161–180.
28. "Demonstration of the differential equations employed by Delaunay in the lunar theory," *Analyst*, v. 3, 1876, p. 65–70.
29. "Solution of a problem in the motion of rolling spheres," *Analyst*, v. 3, 1876, p. 92–93.
30. "Reduction of the problem of three bodies," *Analyst*, v. 3, 1876, p. 179–185.
31. *On the Part of the Motion of the Lunar Perigee which is a Function of the Mean Motions of the Sun and Moon*, Cambridge, Mass., May 1877, 28 p. Privately printed in an ed. of 200 copies; reviewed by J. C. Adams in *RAS MN*, v. 38, p. 43, 92. Reprint with some notes in *Acta M.*, v. 8, 1886, p. 1–36. In a letter to Mittag-Leffler, dated May 7, 1886, Hill noted that the first equation on p. 5 of the reprint should have been $\lambda = \sqrt{JFG} W$.
32. "Empirical formula for the volume of atmospheric air," *Analyst*, v. 4, 1877, p. 97–107.
- *33. Solution of the problem: "Given the lengths of the eight edges of a quadrangular pyramid to find its altitude," *Analyst*, v. 4, 1877, p. 153.
34. "On Dr. Weiler's secular acceleration of the moon's mean motion," *AN*, v. 91, 1878, p. 251–254.
35. "Researches in the lunar theory," *AJM*, v. 1, 1878, p. 5–26, 129–147, 245–260.
36. "On the motion of the centre of gravity of the earth and moon," *Analyst*, v. 5, 1878, p. 33–38.
37. "The secular acceleration of the moon," *Analyst*, v. 5, 1878, p. 105–110.
- *38. Report on the total solar eclipse of July 29th 1878 observed at Denver, U.S. Nautical Almanac, *Wash. Obs.* for 1878, app. 3, p. 221–222, 1880.
39. "Note on Hansen's general formulae for perturbations," *AJM*, v. 4, 1881, p. 256–259.
40. "Notes on the theories of Jupiter and Saturn," *Analyst*, v. 8, 1881, p. 33–40, 89–93.
41. "On Gauss's method of computing secular perturbations, with an application to the action of Venus on Mercury," *APAE*, v. 1, 1881, p. 315–361.
42. "On certain possible abbreviations in the computation of the long-period inequalities of the moon's motion due to the direct action of the planets," *AJM*, v. 6, 1883, p. 115–130.
43. "On the lunar inequalities produced by the motion of the ecliptic," *AM*, v. 1, 1884, p. 5–10, 25–31, 52–58.
44. "Determination of the inequalities of the moon's motion which are produced by the figure of the earth, a supplement to Delaunay's lunar theory," *APAE*, v. 3, 1884, p. 201–344.
45. "On certain lunar inequalities due to the action of Jupiter, and discovered by Mr. E. Neison," *APAE*, v. 3, 1885, p. 373–393.
46. "Elements and perturbations of Jupiter and Saturn," *AN*, v. 113, 1886, p. 273–302.
47. "A reply to Mr. Neison's strictures on Delaunay's method of determining the planetary perturbations of the moon," *RAS MN*, v. 47, 1886, p. 1–8.

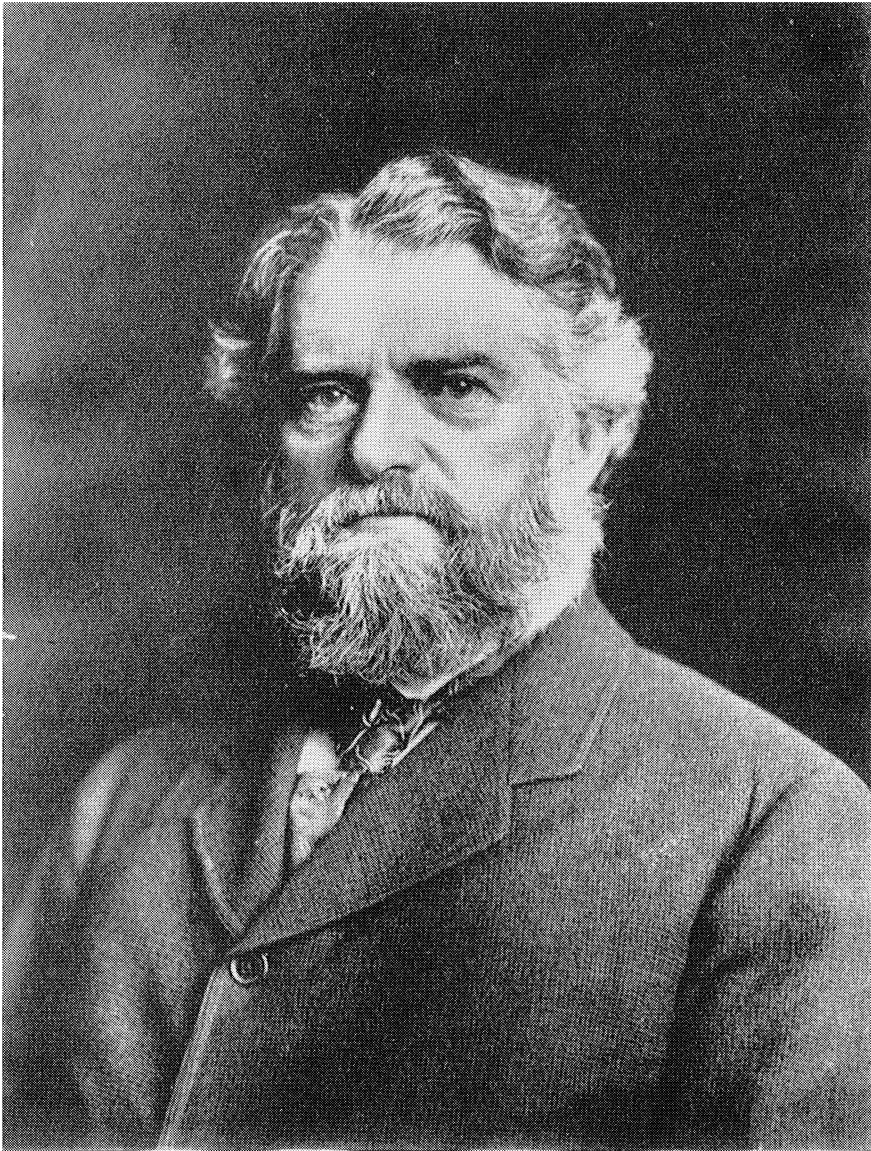
48. "Coplanar motion of two planets, one having a zero mass," *AM*, v. 3, 1887, p. 65-73.
49. "On differential equations with periodic integrals," *AM*, v. 3, 1887, p. 145-153.
50. "On the interior constitution of the earth as respects density," *AM*, v. 4, 1888, p. 19-29.
51. "The motion of Hyperion and the mass of Titan," *AJ*, v. 8, 1888, p. 57-62.
52. "On Leverrier's determination of the second-order terms in the secular motions of the eccentricities and perihelia of Jupiter and Saturn," *AJ*, v. 9, 1889, p. 89-91.
53. "The secular perturbations of two planets moving in the same plane; with application to Jupiter and Saturn," *AM*, v. 5, 1890, p. 177-213.
54. "A new theory of Jupiter and Saturn," *APAE*, v. 4, 1890, 577 p.
55. "The secular variation of the motion of the moon's perigee," *AJ*, v. 10, 1890, p. 73-74.
56. "Additional terms in the great inequalities of Jupiter and Saturn," *AJ*, v. 11, 1891 p. 49-51.
57. "On the connection of precession and nutation with the figure of the earth," *AJ*, v. 13, 1893, p. 1-6.
58. "On intermediate orbits," *AM*, v. 8, 1893, p. 1-20.
59. "Literal expression for the motion of the moon's perigee," *AM*, v. 9, 1894, p. 31-41.
- *60. *Course of Lectures on Celestial Mechanics by Dr. G. W. Hill delivered at Columbia College 1893-94*, New York, Columbia U., 1894. Fourteen lectures hektographed; a copy at Columbia U., through part of lecture XI, contains 256 p.
61. "Discussion of the observations of Jupiter with resulting values for the elements of the orbit and the mass of Saturn," *APAE*, v. 7, 1895, p. 5-22.
62. "Discussion of the observations of Saturn with resulting values for the elements of the orbit and the masses of Jupiter and Uranus," *APAE*, v. 7, 1895, p. 147-167.
63. "The periodic solution as a first approximation in the lunar theory," *AJ*, v. 15, 1895, p. 137-143.
- *64. "Tables of Jupiter, constructed in accordance with the methods of Hansen," *APAE*, v. 7, 1895, pt. I, p. 1-144.
- *65. "Tables of Saturn, constructed in accordance with the methods of Hansen," *APAE*, v. 7, 1895, pt. II, p. 145-285.
66. "On the convergence of the series used in the subject of perturbations," *AMS Bull.*, v. 2, 1896, p. 93-97.
67. "Remarks on the progress of celestial mechanics since the middle of the century," *AMS Bull.*, v. 2, 1896, p. 125-136, AMS P add. 27 Dec. 1895. Also in *Science*, n.s., v. 3, 1896, p. 333-341.
68. "Jupiter-perturbations of Ceres, of the first order, and the derivation of the mean elements," *AJ*, v. 16, 1896, p. 57-62.
- *69. "Memoir of James Edward Oliver 1829-1895," *NAS Biog. Mem.*, v. 4, 1896, p. 57-74.
70. "On the values of the eccentricities and longitudes of the perihelia of Jupiter and Saturn for distant epochs," *AJ*, v. 17, 1897, p. 81-87.
71. "On intermediary orbits in the lunar theory," *AJ*, v. 18, 1897, p. 81-87.
- *72. "Observations on Professor Newcomb's determination of the principal element of precession," *AJ*, v. 18, 1898, p. 153-156; correction p. 168.
73. "Note on the mass of Mercury," *AJ*, v. 19, 1898, p. 157-158, 167.
74. "On the inequalities in the lunar theory strictly proportional to the solar eccentricity," *AJ*, v. 20, 1899, p. 115-124.
75. "On the extension of Delaunay's method in the lunar theory to the general problem of planetary motion," *AMS Trans.*, v. 1, 1900, p. 205-242, 508-509.
76. "Ptolemy's problem," *AJ*, v. 21, 1900, p. 33-35.
77. "Normal positions of Ceres," *AJ*, v. 21, 1900, p. 51-54.
78. "Secular perturbations of the planets," *AJM*, v. 23, 1901, p. 317-336.
79. "On the use of the sphero-conic in astronomy," *AJ*, v. 22, 1901, p. 53-56.
80. "Illustrations of periodic solutions in the problem of three bodies," *AJ*, v. 22, 1902, p. 93-97, 117-121.
81. "On the application of Delaunay transformations to the elaboration of the secular perturbations of the solar system," *AJ*, v. 22, 1902, p. 183-189.

82. "Examples of periplegmatic orbits," *AJ*, v. 24, 1904, p. 9-14.
83. "The theorems of Lagrange and Poisson on the invariability of the greater axes in an ordinary planetary system," *AJ*, v. 24, 1904, p. 27-29.
84. "Comparison of the new tables of Jupiter and Saturn with the Greenwich observations of 1889-1900," *AJ*, v. 24, 1904, p. 60-61.
85. "Development of functions in power series from special values," *AJ*, v. 24, 1904, p. 123-128.
86. "Deduction of the power series representing a function from special values of the latter," *AJM*, v. 27, 1905, p. 203-216.
87. "Integrals of planetary motion suitable for an indefinite length of time," *AJ*, v. 25, 1905, p. 1-12.
88. *The Collected Mathematical Works of George William Hill* (CI Pub.), Wash., D.C., 4v., 1905-1907. These v. were ed. by Hill; they include all of the items except the 17 which are starred (*).
89. "Application of the Delaunay transformation in the planetary theories," *CI Pub.*, no. 9, v. 4, 1907, p. 345-391.
90. "Remarks supplementary to memoir no. 79," *CI Pub.*, no. 9, v. 4, 1907, p. 392-397.
91. "Development, in terms of the true anomaly, of odd negative powers of the distance between two planets moving in the same plane," *CI Pub.*, no. 9, v. 4, 1907, p. 398-407.
92. "On the construction of maps," *CI Pub.*, no. 9, v. 4, 1907, p. 408-418.
93. "Dynamic geodesy," *CI Pub.*, no. 9, v. 4, 1907, p. 419-452.
- *94. "Attraction of the homogeneous spherical segment," *AJM*, v. 29, 1907, p. 345-362.
- *95. "Subjective geometry," *AMS Bull.*, v. 14, 1908, p. 305-313.
- *96. "The Jovian evection in the lunar theory," *AJ*, v. 25, 1908, p. 193-196.
- *97. "Biographical memoir of Asaph Hall 1829-1907," *NAS Biog. Mem.*, v. 6, 1908, p. 241-309.
- *98. "Motion of a system of material points under the action of gravitation," *AJ*, v. 27, 1913, p. 171-182.
- *99. "The secular perturbations of the four outer planets," *AJ*, v. 28, 1913, p. 59-71.
- *100. "Hypergeometric series and Walker's table of the Leverrier coefficients," *AJ*, v. 28, 1914, p. 93-100.
- *101. Reviews of books by J. N. Stockwell in *Analyst*, 1882; and by Gylden in *AJ*, 1894.

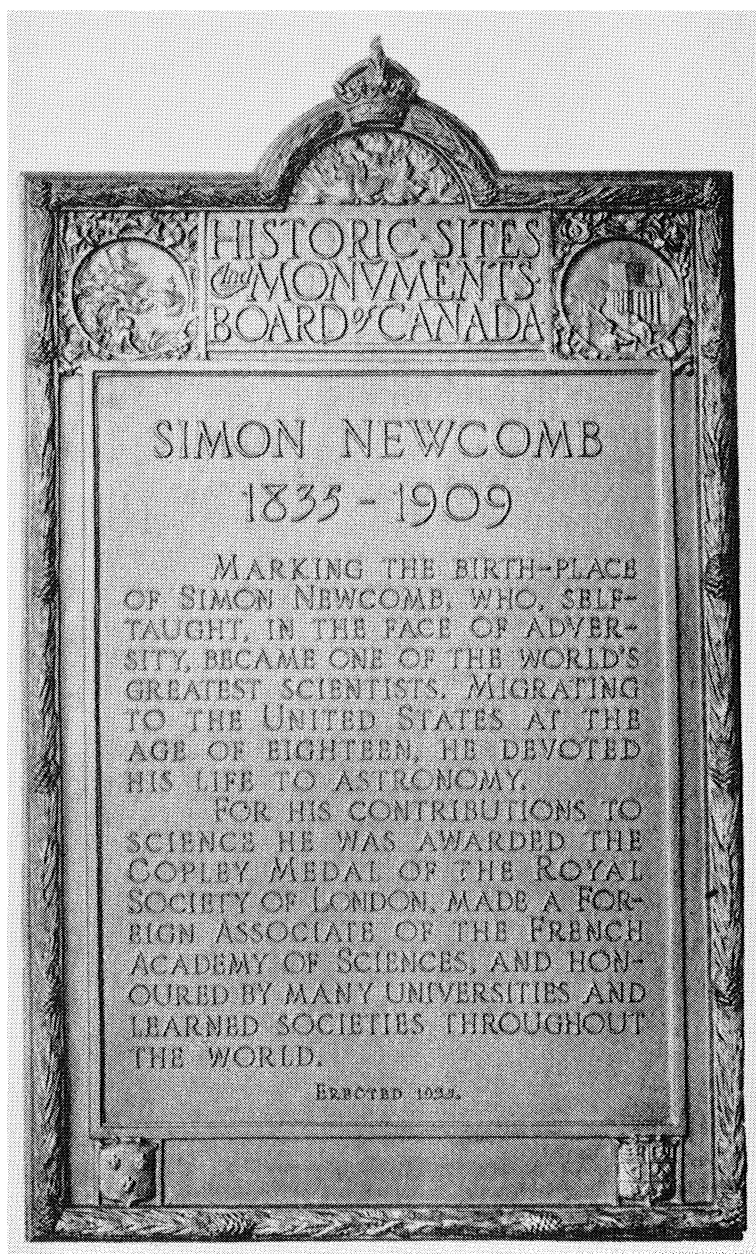
4. SIMON NEWCOMB

CURRICULUM VITAE.—B. Wallace Bridge, Nova Scotia, Can. 12 Mar. 1835; d. Washington, D.C. 11 July 1909. Taught by his father. Came to U.S. in 53. Teacher in a country school at Massey's Cross Roads, Md. 54, and in the village school at Sudlersville, Md. 55. Computer in Nautical Almanac Office, Cambridge, Mass. (Jan. 57-Sept. 61; office moved to Washington in 66). Prof. math. U.S. Navy (Sept. 61-Sept. 77; senior prof. math. and supt. Naut. Alm. Office Sept. 77-Mar. 97). Lect. in Columbian, afterwards George Washington, U. (73-84; prof. astr. 84-86). Prof. math. and astr. JHU (Oct. 84-Dec. 93; 98-00; prof. math. emeritus 00-09). Lect. U. California summer 07. Became citizen of U.S. probably sometime 57-61.

HONORS.—Expedition, directed by S. Newcomb and W. Ferrel, to observe total solar eclipse Lake Winnipeg, Can., July 60. Fellow AAcAS 60. Mem. NAS 69. In U.S. Govt. exped. solar eclipse to Des Moines, Ia. Aug. 69, to Gibraltar Dec. 70, to Separation, Wyo. July 78, and to Cape of Good Hope Dec. 82 (see Bibl. nos. 21, 26). Hon. LL.D. Columbian U. 74. Corresp. mem., sect. astr. Acad. des Sci., Institut de France 74. Awarded Gold Medal RAS for his "tables of Neptune and Uranus and other mathematical works" 74. Offered directorship Harvard Obs. 75. Hon. master of math. and Ph. Nat. D., U. Leyden 75; on the celebration of the 300th anniversary of its founding. Hon. LL.D. Yale U. 75. For. assoc. Royal Swedish Acad. Sci. 75. Corresp. mem. Imp. Acad. Sci., Leningrad 75. Corresp. mem. Royal Bavarian Acad. Sci. 76. P AAAAS 76; ret.



Simon Newcomb



TABLET IN MONUMENT ERECTED BY THE CANADIAN GOVERNMENT

add. "The course of nature" (no. 44). Assoc. Royal So. Sci., Upsala 77. For. mem. RS London 77. Mem. Amer. Phil. So. 78. For. mem. So. Dutch Sci., Haarlem, and awarded by this So. Huygens Medal 78; biennially "awarded to the individual who by his researches and discoveries or inventions during the previous twenty years had in the judgment of the Society distinguished himself in an exceptional manner in a particular branch of science." Hon. mem. Cambridge Phil. So. 78. P Phil. So. Wash. 79-80 and 08. Lect. (4 lects.) on political economy at Harvard U. 79-80. For. fellow RS Edinburgh 81. Chm. NAS advisory comm. on meteorology 81-84. One of three administrators for NAS of the Watson Fund providing means for supporting research and the award of the Watson Gold Medal 81-09; he was chm. board of trustees 87-09 (E. W. Brown received this medal in 37). Lowell Lect. (12 lects.) Boston 81-82; "History of astronomy." For. mem. Royal Physiographic So., Lund 81. Hon. mem. Royal Irish Acad. 82. VP NAS 83-89. Corresp. mem. Prussian Acad. Sci. 83. Hon. LL.D. Harvard U. 84. Corresp. mem. BAAS 84. Ed.-in-chief *AJM* 85-93, 99-00; assoc. ed. 78-79, 95-98, 01-08. P Amer. So. Psychical Research 85-86. Offered presidency U. California 85. Hon. Ph.D. U. Heidelberg, on the celebration of the 500th anniversary of its founding 86. Hon. mem. (at same time as Chrystal and Sylvester) of Assoc. for the Improvement of Geom. Teaching, afterward Math. Assoc., London 86. P Alumni Assoc., Lawrence Sci. School, Harvard U. 86. P Political Economy Club of Amer. 87. Russian emperor ordered portrait painted and placed in gallery of famous astronomers at the Pulkovo Obs. 87. Hon. LL.D. Columbia U. on the occasion of its centenary cel. 87. Hon. mem. Manchester Lit. and Phil. So. 87. Presented by U. Tokyo with pair bronze vases of exquisite workmanship 88. In recognition of his great services in securing for Pulkovo Obs. a large object glass, presented by the Czar of Russia with a rare vase of jasper 89. Awarded Copley Medal RS London, for contributions to the progress of gravitational astr. 89; the medal was accompanied by a check for £50. Hon. mem. N.Y. Acad. Sci. 91. One of 21 eminent scientific men elected Hon. mems. Royal Institution G.B., on the cel. of the Faraday centenary 91. Hon. mem. comm. organization Fifth Intern. Congress Geologists, Wash. 91. Hon. LL.D. U. Edinburgh 91. Hon. mem. Astr. and Phys. So. Toronto now RAS Can. 91. For. assoc. Royal Acad. Sci., Brussels 91. Hon. Sc.D. U. Dublin in cel. tercentenary of its founding 91. Hon. Ph. Nat. D. U. Padua in cel. tercentenary Galileo's appointment as prof. 92. Winner first prize \$150, of two "citizenship prizes" offered by the Anthropological So. of Wash. for the best essay on an assigned topic, "The elements which make up the most useful citizens of the United States" 94. Math. ed. *Science* 95-03. Awarded *AJ* prize of \$400 for the "most thorough discussion of the theory of the rotation of the earth with reference to the recently discovered variation of latitude" 95. Elected one of eight for. assoc. Acad. des Sci., Institut de France to succeed Helmholtz 95; first native Amer. since Franklin so honored. For. assoc. astr. sect. Acad. Lincei 95. Hon. mem. Imp. Acad. Sci., Leningrad 96. Officer Legion of Honor, France 96; authorized by Congress to receive this decoration (see *Congr. Records*, 3 Mar. 97) 96. Hon. LL.D. U. Glasgow 96. Hon. Sc.D. U. Cambridge 96. Hon. LL.D. Princeton U. 96. P AMS 97-98; ret. add. "The philosophy of hyperspace" (no. 112). Awarded the Schubert Prize (about \$460) by the Imp. Acad. Sci., Leningrad 97. Corresp. mem. Imp. Geographical So., Leningrad 97. At 21st anniversary cel. of founding JHU requested by faculty and friends to sit for portrait, painted by R. G. Hardie, to be given to the U.; reproduced in *AJM* 99. For. assoc. Italian So. Sci. (dei XL) 97. Hon. corresp. mem. Royal So. Arts 97. First recipient Bruce Gold Medal, from the ASP 97; the So. had to select recipient from nominees by directors of six observatories Berlin, Greenwich, Harvard, Lick, Paris, and Yerkes, but one name stood forward so prominently the So. could but set the seal of its approval upon the verdict of its peers. Cape Newcomb of the Hoyt Islands, Hubbard Bay, W. Greenland named after S. Newcomb (see *Nat. Geogr. Mag.*, v. 9, p. 3) 98. For. assoc. Royal Inst. Sci. Letters and Arts, Venice 98. Hon. mem. Colonial So. Mass. (one of nine) 98. Hon. mem. Royal Acad. Sci., Amsterdam, 98. Hon. D.C.L. Oxford U. 99. Assoc. corresp. mem. Royal Inst. of Sci. and Letters, Milan 99. For. corresp. Bureau of Longitudes, Paris 99. First P Astr. and Astrophys. So. (now Amer. Astr. So.) and reelected annually until he requested and insisted on relief from the duty 99-05. Hon. I.L.D. U. Cracow, Austria on the cel. of the 500th anniversary of its foundation 00. One of two receiving first award of Sylvester Prize of JHU, a bronze medallion of J. J. Sylvester, framed in oak 01; the

first impression of the tablet was presented to Lord Kelvin and the second "to Simon Newcomb, a distinguished astronomer, who has been a friend of the university from its inception, and who guided the affairs of the mathematical department." Hon. mem. Russian Astr. So. 01. Hon. mem. Royal So. New South Wales, Sydney 01. Hon. LL.D. JHU at the cel. of the 25th anniversary of its founding, "in recognition of his preeminent attainments and important discoveries in science," 02. Hon. mem. Astr. So. Mexico 02. Presented to King Vittorio Emanuele III of Italy 02. Hon. Math. D. U. Christiania in connection with the cel. of the centenary of the birth of Niels Henrik Abel 02; Newcomb went as delegate from NAS, and during the cel. was presented to King Oscar of Sweden and Norway. Appointed one of five mems. advisory comm. in astr. for the Carnegie Inst. 03; during 03-08 Newcomb received \$28,000 in grants towards expenses of his investigations. For. Secy. NAS 03-09. Mem. comm. Amer. Phil. So. to organize bicentenary cel. of Franklin's birth 03. Presented to King Edward VII of England 03. P Intern. Congress of Arts and Sci., Louisiana Purchase Exposition, St. Louis Sept. 04; as P of the Congress he made a special trip to Europe to secure cooperation of leading European men of sci. VP BAAS 04. Corresp. mem. Royal Acad. Sci., Vienna 04. Hon. LL.D. U. Toronto 04. Corresp. mem. Royal Acad. Sci., Turin 05. Corresp. mem. Nat. Inst. of Geneva, Switzerland 05. Knight of the Order Pour le Mérite for Sci. and Arts, Prussia 05; bill granting Newcomb permission to accept this decoration became law Apr. 06. P Cosmos Club, Wash. 06-07. Mem. Board of Overseers Harvard U. 06-09; first election to this body of a grad. of Lawrence Sci. School not already a grad. of the C. Hon. mem. Royal Acad. Sci., Letters and Arts, Padua 06. Commissioned rear-admiral U.S. Navy 06. Commander of the Legion of Honor, France 07. Hon. fellow (one of twelve) Phys. So., London 07. For. mem. So. Sci., Christiania 07. For. mem. Royal So. Sci., Göttingen 07. A VP and invited speaker fourth Intern. Congress Mathems., Rome, Apr. 08. Received in audience by Emperor William II Germany, and lunched with his Majesty and the Empress Aug. 08. VP Amer. Phil. So. 09. Medallion of Newcomb in the sci. panel of one of two bronze doors, designed and modeled by Louis Amateis, for the U.S. Capitol 10. Cut-stone monument with inserted bronze tablet, erected by The Historic Sites and Monuments Board of Canada on the site of Newcomb's birthplace, Wallace Bridge, Nova Scotia, unveiled 30 Aug. 35; see photograph of monument, and add. of R. C. Archibald, *Scripta Mathem.* v. 4, 1936. Bronze bust by Frederick MacMonnies unveiled in the Hall of Fame, N.Y.U. 28 May 36; received 78 out of 100 votes in 35.

BIOGRAPHICAL NOTES.—Simon Newcomb's ancestry was chiefly English, and in minor degrees Scotch, French, German, and Irish. His ancestors in every line had crossed the Atlantic long before the American Revolution, and the American descent was almost entirely through New England families. Simon Newcomb's paternal grandfather removed to Nova Scotia in 1761. His father John Burton Newcomb was a school teacher, and his gifted mother Emily Prince bore two daughters and five sons, of whom Simon was the eldest.

Since no other American scientist has ever accumulated such an extraordinary collection of honors as those listed above (and the list might have been considerably extended) an attempt will be made to record some brief suggestions as to reasons for such acclaim. (I shall often closely follow E. W. Brown's sketch which is especially valuable.) First of all it should be borne in mind that more than forty years have passed since Newcomb became president of the Society, and that in the same year he retired from his position as Superintendent of the Amer. Ephemeris and Nautical Almanac. This was before the founding of the Amer. Astr. So. and before many later extraordinary astronomical developments in Amer-

ica. His connection with the Nautical Almanac Office was for yet another forty years earlier, namely 1857–97. Even during the first decade of this period, with the Civil War and consequent disorganization of Govt. work, Newcomb began an investigation on the asteroids which resulted in one of his most important papers (no. 8). This virtually disposed of the explosion theory of Olbers put forward to account for the existence of these minor planets. Already at this time he displayed a grasp of the general principles of celestial mechanics and the methods of dealing with observations, always such a marked feature of all his researches. In 1869 he completed a four-year program of star observations, planned with great care and resting on its own foundations. Discussion of the observations revealed, as he had expected, the presence of systematic errors in existing catalogues of star positions. As his knowledge extended from the fixed stars to the moon, he was becoming more and more impressed with the confusion assailing exact astronomy because of the different values of the constants used by different observers. Two gigantic plans gradually matured in his mind. The one was a determination of all the constants of astronomy and their reduction to a homogeneous system, which would involve extended work on the theories of the planets and satellites. The second was the resolution of the lunar motions and the test of the law of gravitation which a comparison of the lunar theory would involve. The first plan was achieved, and the immense mass of work summarized in a little volume of 1897, *Elements of the Four Inner Planets and the Fundamental Constants of Astronomy* (no. 106). This gathers together his life work and constitutes his most enduring memorial. Leading up to results here won, are his publications, nos. 16, 27, 75, 98, 100, 104, 105, 111, 113, and 114. The theory was not the heaviest part of the work. All known observations had to be collected and compared. It was here that Newcomb's particular genius for the organization of huge masses of material, and his firm grasp of the facts which could be deduced from them, was given free play. The mutual perturbations of Jupiter and Saturn are so large that the problem of unravelling their motions is a much more difficult application of planetary theory than the other six large planets require. For the successful completion of Newcomb's scheme within his life time it was necessary that these two planets should be treated by another hand, and he enlisted the services of G. W. Hill who spent ten years on the work. Newcomb's determination of the solar parallax in 1862 (no. 18) as $8''.848$, he corrected to $8''.790$ in 1897. In order to fix the constant of aberration, a fresh determination of the velocity of light was carried through with Michelson (no. 82). Greatly increased facilities for observation were made possible in 1873 when he had secured a large refracting telescope for the Naval Obs. His founding of the remarkable series, *Astr. Papers prepared for the Use of the Amer. Ephemeris and Naut. Alm. (APAE)* made the results of latest research generally available.

As early as 1859 Newcomb compared observed places of the moon with those given in the Ephemerides, and his last, but one of his best, paper (no. 149) dealt with the motions of the moon and was finished only a month before his death. Other publications in this connection were nos. 19, 20, 23, 25, 39, 99, 145, and 146. In these his personal contributions were numerous and interesting, especially no. 39 in which he added observations carrying back the period dealt with by Hansen for at least 75 years. He had always hoped to prepare a new set of tables of the moon's motion but this was to be finely achieved by E. W. Brown at a later day.

One of Newcomb's rare excursions into pure theory is contained in "The general integrals of planetary motion" (no. 32) and it consists of an attempt to show how the coordinates of a planet, under the attraction of any finite number of planets, may be represented by trigonometric series. Poincaré has used this paper as a text for his investigations into the possibility of such developments (see Poincaré, *Les Méthodes Nouvelles de la Mécanique Céleste*, v. 2, 1893). Another very interesting and little known excursion into non-euclidean geometry (no. 36) was founded on the ideas of Riemann's celebrated doctoral dissertation, and is quoted extensively in Sir Robert Ball's article on measurement in the *Encycl. Brit.*, 9th ed. In the very first paper in *AJM* Newcomb proved (no. 42) a theorem, concerning geometry in fourth dimension, which is often quoted (see chap. I). Turning to Newcomb's other mathematical work, Cayley characterized the memoir on the perturbations of the moon (no. 25) as follows: "from the boldness of the conception and beauty of the result a very remarkable one, and constitutes an important addition to theoretical dynamics." Newcomb was the author of a series of school and college mathematical text-books (nos. 60, 61, 66, 67, 68, 77, 78, 91) which did not have a large sale, except in the case of the mathematical tables (no. 66) which went through many editions. He was, naturally, much interested in questions in the theory of probabilities and least squares (nos. 6, 7, 9, 10, 11, 28, 59, 86, 142). In an address before NYMS in 1893, on modern mathematical thought (no. 101), he began with a disclaimer of any right to be considered a mathematician in the modern sense of the word, but from the remarks which follow it is evident that he had not only read but had devoted much thought to modern ideas on hyperspace, group theory, projective geometry and the like. His presidential add. was on the philosophy of hyperspace (no. 112). We have noted above that he was editor-in-chief of *AJM* for a number of years and prof. of math. and astr. at JHU, where he was one of the first to receive appointment as lecturer on its opening in 1876. In many of the early years he served as examiner in math. and economics. Further indication of Newcomb's interest in the teaching of mathematics (see no. 95, 139) is furnished by the fact that he was chm. of the comm. of ten on math. in secondary education appointed in 1892 by

the comm. of the National Education Assoc. of the U. S. The report adopted had a large influence on the teaching of mathematics; the chairman's part in its preparation was considerable.

Among Newcomb's astronomical works reference may be made only to his remarkable *Popular Astronomy* (no. 40) which went through many editions and was translated into Norwegian, Russian and German; to his *Astronomy for Everybody* (no. 125) translated into Russian, German, Swedish, and Bohemian and still annually selling by the thousand in American department stores; to his *Compendium of Spherical Astronomy* (no. 137), still the best of its kind. In the field of Political Economy Newcomb published in 1865 at his own expense, *A Critical Examination of our Financial Policy during the Southern Rebellion* (no. 15) and during the next forty years he wrote many articles, and three other v., including a large work on *Principles of Political Economy* (nos. 33, 84, 85) which was several times reprinted. Newcomb was ranked high as an economist by Irving Fisher and President Hadley of Yale U. and there is little doubt that if he had chosen economics as the chief field of his endeavors he would have been among the foremost of modern economists. He was P Political Economy Club of America in 1887.

He discussed in print various questions connected with meteorology, aerial flight, occultism, life insurance, and a host of other topics. Stories (nos. 107, 130) and even a novel (no. 121) also flowed from his pen. In the novel, airships of the Zeppelin type are successfully employed. Newcomb was sceptical of the possibility of airplanes, since he failed to conceive of motors such as were developed soon after his death. Some samples of his collections of encyclopedia articles are indicated below (nos. 96, 122, 123, 131, 148).

He was indefatigable in his attendance at congresses, scientific meetings and academic functions. At many gatherings of this kind he was a singularly effective presiding officer, and entered upon such duties with pleasure. He rendered exceedingly valuable service in connection with several of the world's great telescopes, and his other contributions to the work of many observatories were great.

"Newcomb's work, driven by untiring energy and guided by philosophic intelligence for more than half a century, placed him at the head of his profession in America, and gave him membership in a small class of the most productive astronomers of all countries and all centuries. His influence upon the development of the science was exerted by speech and by letter as well as by published paper and volume. It was potent with beginners and assistants as well as with veterans and directors. It was applied with singleness of purpose, and solely in the interest of the science. Those who discussed astronomy with Newcomb had the impression of obtaining astronomy in the abstract, impersonal and disembodied, and

on that account his scientific associates often failed to understand his personality. A survey of Newcomb's activities leads to the view that he was intellectually a giant." (Campbell).

His favorite motto was, "Whatsoever thy hand findeth to do, do it with all thy might." That, irrespective of his surroundings, he could with all his might concentrate on any subject, explains, in part, the extraordinary extent of his achievements. In the honors showered upon him as a result of these, Newcomb always took a naive pleasure. He spoke French and German fluently and knew sufficient of the languages of Italy and Sweden to be able to travel in these countries with comfort. Accustomed from childhood to long walks he continued this form of exercise throughout life, walking daily several miles between the close of office hours and dinner. On Sundays the walks were much longer. Nothing delighted him more than his walking trips in Switzerland while he was abroad. Even when he was seventy years old he climbed to the chalet high up the side of the Matterhorn, a feat almost unprecedented for a man of his age. He was a lover of travel. Only intimates would know that he was full of fun and loved to romp with his children, when they were young. He read history and other literature extensively and could recite page after page of poetry. He delighted in art and never went abroad without spending many hours in famous galleries and enjoying paintings. Of music he knew nothing. In fact, he used to say that he did know enough to distinguish between Old Hundred and Yankee Doodle because the former was slow and the latter quick. He never went to the theater nor learned to play the usual card games, but he was an expert chess player and during an ocean voyage is known to have carried on four games simultaneously without reference to any chess boards. His wide and varied reading, combined with accurate memory and universal interest, made his conversation virile and enlightening. His wife was a granddaughter of F. R. Hassler, the first superintendent of the U. S. Coast Survey. One of Newcomb's grandsons is Hassler Whitney, professor of math. at Harvard U. and one of America's most gifted younger men (see *Scripta Mathem.*, v. 4, p. 284).

SOURCES.—E. W. Brown, *AMS Bull.*, v. 16. G. W. Hill, *Science*, n.s., v. 30. R. C. Archibald: (a) "Bibliography of his life and work," *NAS Mem.*, v. 17, 1924; (b) *Science*, n.s., v. 44, 1916, p. 871-878, list of honors, etc. A. Cayley, *RAS MN*, v. 34, 1874, p. 224-233. I. Fisher, *Econ. Journ.*, v. 19, 1909. M. Loewy, *Nature*, v. 60, 1899. W. W. Campbell, *NAS Mem.*, v. 17. H. H. Turner, *RAS MN*, v. 70. S. Newcomb, *Reminiscences of an Astronomer* (no. 128). B. M. Newcomb, *Andrew Newcomb 1618-1686 and his Descendants*, New Haven, Conn., 1923. Mrs. S. N. Merrick (S. Newcomb's sister), *McClure's Mag.*, v. 35, 1910, with many illustrs. Carnegie Inst., *Year Books*, nos. 1-8, 1902-09. Information from Dr. Anita McGee, daughter of S. Newcomb.

BIBLIOGRAPHY

I have elsewhere given Newcomb's Bibliography in great detail, 542 items: 319 under the general heading of "astronomy," 35 under "mathematics," 42 under "economics," 146 under "miscellaneous." Some of these items, apart from his 35 books, are quite extensive, for example

the 73 cyclopedia articles in no. 96 below. Others are very brief like his first publication (no. 1), a letter to a newspaper, and an anonymous note on B. Peirce (no. 31). In the present Bibliography nearly 400 items have been omitted, but an attempt has been made to preserve sufficient to suggest everything which is of outstanding significance, or which is of special interest from a mathematical point of view, and to illustrate the extraordinary diversity of Newcomb's interests and activities. The first three items (nos. 1-3) are given simply because they are the first three, although the first had interesting repercussions (see no. 94). All of his books and all foreign translations of items have been listed. Samples of his anonymous reviews and editorial notes have also been included; of the latter in the *Nation*, authorship was determined from the editorial file in New York City nearly thirty years ago. All items are here arranged chronologically regardless of topics.

1. "Velocity of meteors. Motion of bodies impelled by a single center of force," *National Intelligencer*, Wash., May 26, 1855, col. 2.

2. "Elements and ephemeris of the fifty-fourth asteroid" (with T. H. Safford), *AJ*, v. 5, 1858, p. 162.

3. "Elliptic elements of comet, 1858, V," *AJ*, v. 5, 1858, p. 178.

4. "On a method in dynamics," *AJ*, v. 5, 1858, p. 121-127.

5. "Note on differentiation," *Runkle's Math. Mo.*, v. 1, 1859, p. 396-397.

6. "Notes on the theory of probabilities," *Runkle's Math. Mo.*, v. 1, 1859, p. 136-139, 233-235, 331-335, 349-350; v. 2, 1860, p. 134-140, 272-275; v. 3, 1861, p. 68, 119-125, 341-349.

7. "Solutions of problems in probabilities," *Runkle's Math. Mo.*, v. 1, 1859, p. 349-350.

8. "On the secular variations and mutual relations of the orbits of the asteroids," *AAcAS Mem.*, n.s., v. 5, 1860, p. 123-152.

9. Solution of prize question: "Two rods 2 and 4 feet long, respectively, having their middle points connected by a string 1 foot in length are thrown up; show that the chance of their crossing is $1/2 + 2/\pi^2$," *Lady's and Gentleman's Diary*, 1860, p. 67-68.

10. "On the objections raised by Mr. Mill and others against Laplace's presentation of the doctrine of probabilities," *AAcAS Proc.*, v. 4, 1860, p. 433-440.

11. Solution of the problem: "Two great circles are drawn at random on a sphere. What is the probability that their mutual inclination, taken less than 90° , will be contained between any given limits, as n and m ?" *Runkle's Math. Mo.*, v. 3, 1860, p. 68-69.

12. "On the mathematical theory of heat in equilibrium," *Runkle's Math. Mo.*, v. 2, 1860, p. 346-351.

13. "Modern theoretical astronomy," *N. Amer. Rev.*, v. 93, 1861, p. 367-390. [Anonymous.]

14. "Investigation of the dynamical theory of gases," *AAcAS Proc.*, v. 5, 1861, p. 112-114.

15. *A Critical Examination of Our Financial Policy during the Southern Rebellion*, New York, 1865, 222 p.

16. *An Investigation of the Orbit of Neptune, with General Tables of its Motion*, Wash., 1866, 6+111 p.

17. "Our financial future," *N. Amer. Rev.*, v. 102, 1866, p. 100-135.

18. *An Investigation of the Distance of the Sun and of the Elements which depend upon it, from the Observations of Mars made during the Opposition of 1862, and from other Sources*, Washington, 1867, 29 p.

19. "On Hansen's theory of the physical constitution of the moon," *AAAS Proc.*, v. 17, 1868, p. 167-171; abridged in *AJS*, s. 2, v. 46, 1868, p. 376-378, and *Phil. Mag.*, s. 4, v. 37, 1869, p. 32-35.

20. "Comparaison de la théorie de la lune de M. Delaunay avec celle de M. Hansen," *CR Paris*, v. 46, 1868, p. 1197-1200.

21. *Report on Observations of the Total Eclipse of the Sun, Aug. 7, 1869*. Conducted under the direction of Commodore B. F. Sands, Wash., 1869, 214 p. (reports from ten scientists; S. Newcomb's report, p. 5-22); *Wash. Obs.*, 1867, app. 2, 1870.

22. "Aperçu d'une méthode directe et facile pour effectuer le développement de la fonction perturbative et de ses coefficients différentiels," *CR Paris*, v. 70, 1870, p. 385-388.

23. "Sur les inégalités de la lune dues à l'action des planètes," *CR Paris*, v. 71, 1870, p. 384–386.
24. "The let-alone principle," *N. Amer. Rev.*, v. 110, 1870, p. 1–33.
25. "Théorie des perturbations de la lune qui sont dues à l'action des planètes," *Journ. d. Mathém.*, s. 2, v. 16, 1871, p. 321–368; abstract in *CR Paris*, v. 72, 1871, p. 403–406.
26. *Reports on Observations of the Total Solar Eclipse of December 22, 1870* [at Gibraltar], Wash., 1871, 132 p. (S. Newcomb's report, p. 5–24, is one of five); *Wash. Obs.*, 1869, app. 1, 1872.
27. *An Investigation of the Orbit of Uranus, with General Tables of its Motion*, Wash., 1873 7+288 p.
28. "A mechanical representation of a familiar problem" [in least squares], *RAS MN*, v. 33, 1873, suppl., p. 573.
29. "The coming transit of Venus," *Harper's Mag.*, v. 50, 1874, p. 25–35.
30. "Exact science in America," *N. Amer. Rev.*, v. 119, 1874, p. 286–308.
31. [Note on Benjamin Peirce], *Nation*, v. 18, 1874, p. 157. [Anonymous.]
32. "On the general integrals of planetary motion," Wash., 1874, vii+31 p.
33. "The ABC of finance, or The money question familiarly explained to every-day people in nine short and easy lessons," *Harper's Weekly*, v. 19, 1875, p. 1018–1019, 1042; v. 20, 1876, p. 10, 30–31. *The ABC of Finance; or, The Money and Labor Questions Familiarly Explained to Common People, in Short and Easy Lessons*. (Harper's Half-Hour Series, v. 32), New York, c. 1877, p. 7–115; another ed., 1878, p. 7–115 [Preface: "A part of these 'lessons' appeared some time since in *Harper's Weekly*. The unexpected favor with which they were received, by being reprinted, in whole or in part, by newspapers in various sections of the country, has suggested their reproduction in a more permanent form. They are now completed, by the addition of several chapters bearing on the labor questions of the present day"].
34. "Life insurance," *Intern. Rev.*, v. 2, 1875, p. 353–370.
35. "Who are friends of negro suffrage?" *Nation*, v. 24, 1877, p. 53–54. [Anonymous editorial]
36. "Elementary theorems relating to the geometry of a space of three dimensions and of uniform positive curvature in the fourth dimension," *Crelle's J.*, v. 83, 1877, p. 293–299.
37. "Life insurance failures," *Nation*, v. 24, 1877, p. 157–158. [Anonymous editorial]
38. *Astronomy* by R. S. Ball . . . specially rev. for America by S. Newcomb (Handbooks for Students and General Readers), New York, 1878, 13+154 p.
39. "Researches on the motion of the moon . . . Part I—Reduction and discussions of observations of the moon before 1750." Wash., 1878, 280 p. For part II, see no. 149.
40. *Popular Astronomy*, New York, 1878, 16+566 p.+5 maps of stars; 2d ed., 1879, 18+572 p.+maps of stars; 3d ed., 1880; 4th ed. rev., 1882, 18+577 p. (reprinted 1883); 5th ed., 1886, 18+578 p.; 6th ed., 1890; 7th ed., [1893]; 8th ed., 1896, 18+578 p.; small eds. in 1909, 1910, 1911, 1912, 1918; 1880–82 a "School Edition" was issued in America; London, 1878, 566 p.; 2d ed., 1883, 580 p.; 2d ed. rev., 1910, 600 p.
German edition: *Populäre Astronomie*, Leipzig, 1881, 16+742 p.; 2d ed., 1892, 20+748 p.; 3d ed., [rev.], 1905, 10+748 p.; 4th ed., 1911, 16+722 p.; 5th ed., 1914, 12+835 p.; 6th ed., 1921, 12+889 p.; 7th ed., 1922, 14+902 p.
Norwegian trans.: *Omrids af Astronomien. Efter S. Newcombs Populære Astronomi* . . . Udgivet af Selskabet for folkeoplysningens fremme som første tellægshefte til Folkvennen for 1887. (*Outline of Astronomy. According to* [that is, abridged from] *S. Newcomb's Popular Astronomy*. Published by the So. for the Advancement of Popular Education as the first supplementary part to *Folkvennen* for 1887), Kristiania, 1887, 339 p.+1 plate.
Russian trans.: *Astronomiâ v obščeponiâtnom izloženii, dopolnennââ* G. Fogelem, s. 195 ris. [Astronomy in popular presentation, supplemented by G. Fogel, with 195 charts and illustrations]. from the 2d German ed., St. Petersburg, 1896.
41. "Astronomy," "Galaxy," "Gravitation," "Probability, theory of, or calculus of probability," *Johnson's New Universal Cycl.*, 1878.
42. "Note on a class of transformations which surfaces may undergo in space of more than three dimensions," *AJM*, v. 1, 1878, p. 1–4.

43. "An advertisement for a new religion," *N. Amer. Rev.*, v. 127, 1878, p. 44-60.
44. "The course of nature," *AAAS Proc.*, v. 27, 1878 (1879), p. 1-28; *Kansas City Rev.*, v. 2, 1878, p. 356-367, 392-396; *Pop. Sci. Mo. Suppl.*, no. 18, 1878, p. 481-493; *Journ. Sci.*, s. 3, v. 1, 1879, p. 64-89; with title "Simplicity and universality of the laws of nature," *Independent*, v. 30, 1878, p. 5-8. AAAS ret. P add. 22 Aug. 1878.
45. *On the Recurrence of Solar Eclipses, with Tables of Eclipses from B.C. 700 to A.D. 2300*, Wash., Bureau of Navigation, Navy Dept., 1879, 55 p.; *APAE*, 1882, v. 1, pt. 1, 1879. ("A considerable part of the work of constructing the tables [was] performed by John Meier," Preface.)
46. "The Nautical Almanac," U. S. Naval Inst., *Proc.*, v. 5, 1879, p. 33-49; *Side-lights on Astronomy*, 1906, p. 191-215.
47. *Astronomy for Schools and Colleges* (with E. S. Holden), New York, 1879, 11+512 p.; 2d ed. rev. "for students and general readers," 1880; 3d ed. rev. "for high schools and colleges," 1880; 4th ed. rev., 1883, 12+512 p.; 5th ed., 1885; 6th ed., 1887, 12+512 p.; other reprints or eds. 1888, 1893, 1897, 1902, 1907. (American Science Series) [With the publication in 1883 of *Astronomy* (American Science Series, Shorter Course) this work was called *Astronomy* (American Science Series, Advanced Course)].
48. "The silver conference and the silver question," *Intern. Rev.*, v. 6, 1879, p. 309-333.
49. "Law and design in nature," *N. Amer. Rev.*, v. 128, 1879, p. 537-542.
50. "Evolution and theology—a rejoinder," *N. Amer. Rev.*, v. 128, 1879, p. 647-663.
51. *Observations of the Transit of Venus, Dec. 8-9, 1874, made and reduced under the direction of the Commission created by Congress, Part I—General Discussion of Results*, Wash., 1880, 157 p.
52. "A method of developing the perturbative function of planetary motion," *AJM*, v. 3, 1880, p. 193-209.
53. "The fundamental definitions and propositions of geometry with special reference to the syllabus of the Association for the Improvement of Geometrical Teaching," *Nature*, v. 21, 1880, p. 293-295.
54. "The organization of labor," *Princeton Rev.*, May 1880, p. 393-410; Sept. 1880, p. 231-246.
55. "Principles of taxation," *N. Amer. Rev.*, v. 131, 1880, p. 142-156.
56. "Biographical memoir" [of Joseph Henry], *A Memorial of Joseph Henry*, Wash., 1880, p. 441-473; *Smithsonian Misc. Coll.*, no. 356, v. 21, 1881, p. 441-473; *NAS Biog. Mem.*, v. 5, 1905, p. 1-35.
57. "Modern scientific materialism," *Independent*, v. 32, Dec. 9, 1880, p. 1, cols. 1-3; Dec. 23, p. 1, cols. 1-4; Dec. 30, p. 3, cols. 1-3; v. 33, Jan. 13, 1881, p. 3, cols. 2-4; Jan. 27, p. 2-3, cols. 3-4, 1-2.
58. "The relation of scientific method to social progress," Wash., 1880, 15 p.; Wash. Phil. So., *Bull.*, v. 4, 1881, p. 40-52; *Smithsonian Misc. Coll.*, v. 25; *Side-lights on Astronomy*, 1906, p. 312-329. Wash. Phil. So. P add., Dec. 4, 1880.
59. "Note on the frequency of use of the different digits in natural numbers," *AJM*, v. 4, 1881, p. 39-40.
60. *Algebra for Schools and Colleges* (Newcomb's Mathematical Course), New York, 1881, 11+454 p.; other eds. or reprints 1881, 1882, 1883, 1884, 1885, 1887, 1888, 1889, 1895, 1896, 1903; latest rev. ed., 14+546 p.; *Answers*, New York, 1889, 25 p. *Key to Algebra for Schools and Colleges* (Newcomb's Mathematical Course), New York, 1882, 283 p.; 2d ed., 1885, 2+297 p.; 3d ed., 1889.
61. *Elements of Geometry* (Newcomb's Mathematical Course), New York, 1881, 8+399 p.; other eds. or reprints 1882, 1884, 1887, 1888, 1891; latest rev. ed., 10+399 p.

62. "Show that $\log \left(1 - \frac{2n}{1+n^2} \cos x \right) = -n^2 + \frac{1}{2}n^4 - \frac{1}{3}n^6 + \dots - 2n \cos x - \frac{1}{2}2n^2 \cos 2x$

$$- \frac{1}{3}2n^3 \cos 3x - \dots = \sum_{i=1}^{i=\infty} (-1)^i \frac{n^{2i}}{i} - \sum_{i=1}^{i=\infty} \frac{2n^i}{i} \cos ix," \text{ ETR, v. 36, 1881, p. 116, question}$$

no. 6859.

63. "Catalogue of 1098 standard clock and zodiacal stars, prepared under the direction of Simon Newcomb," *APAE*, v. 1, 1882, pt. 4, 1882, p. 147-314.
64. "Discussion and results of observations on transits of Mercury, from 1677 to 1881," *APAE*, v. 1, 1882, pt. 6, 1882, p. 363-487.
65. "A small telescope and what to see with it," *Harper's Mag.*, v. 64, 1882, p. 523-536; *Side-lights on Astronomy*, 1906, p. 76-105 (under title "Making and using a telescope").
66. *Elements of Plane and Spherical Trigonometry with Logarithmic and Other Mathematical Tables and Examples of Their Use and Hints on the Art of Computation* (Newcomb's Mathematical Course), New York, 1882, 6+160+6+80+104 p.; other eds. or reprints 1882, 1883, 1887, 1889, 1893, 1898, 1902; *Elements of Trigonometry* [as a separate work], 6+168 p., 1882, 1883, 1887, 1889, 1906; *Logarithmic and Other Mathematical Tables, with Examples of Their Use and Hints on the Art of Computation*, 6+80+104 p., 1882 (April and Nov.), 1886, 1887, 1889, 1892, 1893, 1895, 1896, 1898, 1901, 1905, 1908, 1912, 1914, 1916, 1918, 1919, 1921.
67. *Elements of Plane Geometry and Trigonometry, with Four-Place Logarithmic and Trigonometric Tables*, New York, 1882, 7+335 p. ["The present work comprises most of Part I of the author's *Elements of Geometry* and the essentials of the first parts of his trigonometry, followed by a set of four-place logarithmic tables." Preface.]
68. *A School Algebra* (Newcomb's Mathematical Course), New York, 1882, 8+279 p.; other eds. or reprints 1882, 1883, 1887, 1888, 1889, 1891. Answers published in pamphlet form, for example in 1889, 25 p. *Key to School Algebra*, New York, 1883; another ed. 1889.
69. "Remarks on the doctrine of limits," *Analyst*, v. 9, 1882, p. 114-115.
70. "The moon," *Encycl. Brit.*, 9th ed., v. 16, 1883, p. 798-803.
71. "On Hell's alleged falsification of his observations of the transit of Venus in 1769," *RAS MN*, v. 43, 1883, p. 371-381.
72. *Astronomy* (American Science Series, Shorter Course) (with E. S. Holden), New York, 1883, 10+338 p.; 2d ed. rev. and enl., 1884, 10+352 p.; other eds. or reprints 1885, 1887, 1889, 1890, 1892, 1896, 1907. [In 1892 the series title was changed to (American Science Series, Briefer Course).] [*Elementary Astronomy* by E. S. Holden, New York, 1889, 15-446 p., was condensed from the above and no. 47.]
73. "A visit to Cetywayo," *Harper's Mag.*, v. 66, 1883, p. 86-89.
74. "The watchmaking industry in Switzerland," *Science*, v. 1, 1883, p. 296-297.
75. "Development of the perturbative function and its derivatives in sines and cosines of multiples of the eccentric anomaly and in powers of the eccentricities and inclinations," *APAE*, 1891, v. 3, pt. 1, 1884, p. 1-200.
76. "On the motion of Hyperion—a new case in celestial mechanics," *APAE*, 1891, v. 3, pt. 3, 1884, p. 345-371.
77. *Elements of Analytic Geometry* (Newcomb's Mathematical Course), New York, 1884, 8+357 p.; other eds., or reprints 1885 (Jan. and July), 1889, 1892, 1895.
78. *Essentials of Trigonometry, Plane and Spherical, with Three and Four Place Tables, Logarithmic and Trigonometric* (Newcomb's Mathematical Course), New York, Holt, 1884, 6+187 p.; other eds. or reprints 1890, 1895, 1899; p. 167-187 reprinted in 1905 under title: *Three and Four Place Logarithmic and Trigonometric Tables*.
79. "Psychic force," *Science*, v. 4, 1884, p. 372-374.
80. "Psychical research," *Science*, v. 4, 1884, p. 510-511.
81. "Can ghosts be investigated?" *Science*, v. 4, 1884, p. 525-527.
82. "Measures of the velocity of light, made under direction of the Secretary of the Navy during the years 1880-'82," *APAE*, v. 2, 1891, pt. 3, 1885, p. 107-230+7 plates. "Introduction" reprinted in *Sid. Mess.*, v. 5, 1886, p. 15-18, 68-73.
83. "The Georgia wonder-girl and her lessons," *Science*, v. 5, 1885, p. 106-108.
84. *Principles of Political Economy*, New York, 1886 [c. 1885], 16+548 p.; reprinted 1887, 1890, 1895.
85. "A plain man's talk on the labor question," *Independent*, v. 38, 1886, p. 581-582, 613, 646-647, 680, 718, 748, 782, 811-812, 877-878, 942-943, 1006, 1036-1037, 1067-1068, 1103, 1133-1134, 1165. *A Plain Man's Talk on the Labor Question*, New York, 1886, 195 p.

86. "A generalized theory of the combination of observations so as to obtain the best result," *AJM*, v. 8, 1886, p. 343-366.
87. *Annual Address of the President of the American Society for Psychical Research, Jan. 12, 1886*. [on thought-transference], Boston, 1886, 24 unnumbered p.
88. "The condition of the Coast Survey," *Nation*, v. 42, 1886, p. 208-209. [Anonymous editorial.]
89. "Mischievous philanthropy," *Forum*, v. 1, 1886, p. 348-357.
90. "Alvan Clark," *Nation*, v. 45, 1887, p. 149-150. [Anonymous editorial.]
91. *Elements of the Differential and Integral Calculus* (Newcomb's Mathematical Course), New York, 1887, 12+307 p.; other eds. or reprints 1889, 1892.
92. "The place of astronomy among the sciences—an address delivered at the dedication of the new observatory of the University of Syracuse, N.Y., Nov. 18, 1887," *Sid. Mess.*, v. 7, 1888, p. 14-20, 65-73.
93. "Discussion of the north polar distances, observed with the Greenwich and Washington transit circles with determinations of the constant of nutation," *APAE*, v. 2, 1891, pt. 6, 1891, p. 407-490.
94. "Formative influences," *Forum*, v. 11, 1891, p. 183-191; autobiographical sketch.
95. "(1) The teaching of mathematics, Elementary mathematics; (2) Mathematical teaching," *Ed. Rev.*, v. 4, 1892, p. 277-286; v. 6, 1893, p. 332-341.
96. "Algebra," "Algol," "Almanac," "Almucantar," "Altazimuth," "Analysis," "Angle," "Asteroids," "Astronomy," "Binary system," "Calculus," "Collimation," "Collimator," "Comets," "Composition of forces," "Curves," "Eclipse," "Ecliptic," "Energy," "Energy, conservation of," "Equation," "Falling bodies," "Fluxions," "Functions," "Geodesy," "Geometry," "Horizon," "Imaginary quantities," "Incommensurables," "Infinities and infinitesimals," "Interpolation," "Jupiter," "Light," "Limits," "Logarithms," "Magic squares," "Mars," "Mathematics," "Mercury," "Moon," "Nebular hypothesis," "Observatory," "Occultations," "Orbit," "Parallax," "Perturbations," "Photometry," "Planet," "Precession of the equinoxes," "Probability," "Progression," "Ptolemaic system," "Quadrature of the circle," "Quaternions," "Saturn," "Series," "Solar parallax," "Solar system," "Stars," "Sun," "Telescope," "Time," "Transit," "Transits of Venus and Mercury," "Trigonometry," "Trilinear coordinates," "Twilight," "Universe," "Venus," "Vulcan," "Year," "Zodiacal light," *Johnson's Universal Cycl.* [later *Universal Cycl. and Atlas*], New York, 1893-1895. [Simon Newcomb was the "Associate editor" for "astronomy and mathematics" in connection with this work.]
97. "A development of the perturbative function in cosines and multiples of the mean anomalies and of angles between the perihelia and common node and in powers of the eccentricities and mutual inclinations," *APAE*, v. 5, pt. 1, 1894, p. 1-48.
98. "Inequalities of long period stars and of the second order as to the masses in the mean longitudes of the four inner planets," *APAE*, v. 5, 1895, pt. 2, 1894, p. 49-96.
99. "Theory of the inequalities in the motion of the moon produced by the action of the planets," *APAE*, v. 5, 1895, pt. 3, 1894, p. 97-295.
100. "Secular variations of the orbits of the four inner planets," *APAE*, v. 5, pt. 4, 1894, p. 297-378.
101. "Modern mathematical thought," *NYMS Bull.*, v. 3, 1894, p. 95-107; *Nature*, v. 49, 1894, p. 325. Italian trans.: "Pensiero matematico moderno," *Rivista di Matem.*, v. 4, 1894, p. 121-134.
102. "On the mass of Jupiter and the orbit of Polyhymnia," *APAE*, v. 5, 1895, pt. 5, 1895, p. 379-449.
103. "Tables of the motion of the earth on its axis around the sun," *APAE*, v. 6, 1898, pt. 1, 1895, p. 7-169.
104. "Tables of the heliocentric motion of Mercury," *APAE*, v. 6, 1898, pt. 2, 1895, p. 171-270.
105. "Tables of the heliocentric motion of Venus," *APAE*, v. 6, 1898, pt. 3, 1895, p. 271-382.
106. *The Elements of the Four Inner Planets and the Fundamental Constants of Astronomy*. Supplement to the *American Ephemeris and Nautical Almanac* for 1897, Wash., 1895, 9+202 p.

107. "The wreck of the Columbia: a story," *Harper's Mag.*, v. 93, 1896, p. 466-475.
108. "The problems of astronomy," An add. at the dedication of the Flower Obs. at U. Pennsylvania, 12 May 1897. Lancaster, Pa., 1897, 20 p.; *Science*, v. 5, 1897, p. 777-785; extract, "The extent of the Universe," *Current Lit.*, v. 22, 1897, p. 560; extract, "Professor Newcomb on the distances of stars," *Nature*, v. 56, 1897, p. 139-140; *Smithsonian Report*, 1896, 1898, p. 83-92; *Side-lights on Astronomy* under title "The evolution of astronomical knowledge," 1906, p. 258-273. *The Skies and the Earth* by R. A. Proctor, S. Newcomb, C. Young, T. A. Huxley, G. Iles, C. Lyell, S. Shaler (Little Masterpieces of Science ed. by G. Iles), New York, 1892, p. 33-52. German trans.: "Die Probleme der Astronomie," *Himmel und Erde*, v. 10, 1897, p. 74-79, 126-135; *Naturw. Rundschau*, v. 12, 1897, p. 413-416, 429-431.
109. "Aspects of American astronomy," *Pop. Astr.*, v. 5, 1897, p. 351-367; *Science*, v. 6, 1897, p. 709-721; *Astrophys. J.*, v. 6, 1897, p. 289-309; *Smithsonian Report*, 1897, 1898, p. 85-99; *Side-lights on Astronomy*, 1906, p. 274-299; *Business Administration* [a textbook of La Salle Extension University, Chicago], ed. by M. La Follette, W. M. Handy, and C. Higgins, v. 7, 1909, p. 67-83. [An add. delivered at U. Chicago, 22 Oct. 1897, in connection with the dedication of the Yerkes Obs.]
110. "Catalogue of the fundamental stars for the epochs 1875 and 1900 reduced to an absolute system," prepared by and under the direction of Simon Newcomb, *APAE*, v. 8, pt. 2, 1898, p. 77-403; notes and errata by W. G. Thackeray, *RAS MN*, v. 63, 1902, p. 38.
111. "Tables on the heliocentric motion of Mars," *APAE*, v. 6, 1898, pt. 4, 1898, p. 383-586. [Concerning certain errors in these tables, see *RAS MN*, v. 70, 1910, p. 654.]
112. "The philosophy of hyperspace," *Science*, n.s., v. 7, 1898, p. 1-7; *Scientific Amer. Suppl.*, v. 45, 1898, p. 18450-18451; *AMS Bull.* v. 4, 1898, p. 187-195; *Pop. Astr.*, v. 6, 1898, p. 380-389. AMS P add. 29 Dec. 1897.
113. "Tables of the heliocentric motion of Uranus," *APAE*, v. 7, pt. 3, 1899, p. 287-416.
114. "Tables of the heliocentric motion of Neptune," *APAE*, v. 7, pt. 4, 1899, p. 417-471.
115. "The unsolved problems of astronomy," *McClure's Mag.*, v. 13, 1899, p. 248-259; *Side-lights on Astronomy*, 1906, p. 1-17; quoted in *About the Bible, Being a Collection of Extracts from the Writings of Eminent Biblical Scholars and Scientists of Europe and America*, comp. by C. L. Hammond, New York, 1900, p. 33-35.
116. "Has telepathy been established?" *Independent*, v. 51, 1899, p. 1730-1733.
117. "Chapters on the stars," *Pop. Sci. Mo.*, v. 57, 1900, p. 227-239, 376-389, 500-516, 638-659; v. 58, 1900, p. 3-27, 130-147; 1901, p. 307-323, 413-428, 449-466; French trans.: "Les étoiles variables" [v. 57, p. 638-659 above], and "Étude du ciel" [v. 58, p. 413-428 above], *Ciel et Terre*, v. 22, 1901, p. 281-290, 305-317; v. 23, 1903, p. 561-574, 592-599; articles collected, rev., and expanded in book form: *The Stars: A Study of the Universe*, New York, 1901, 11 + 333 p.; reprinted 1902 (Feb. and June), 1904, 1906, 1908 (no. 9 in Science Series ed. by J. M. Cattell and F. E. Beddard); London, 1901; 2d ed. (The Progressive Science Series), London, 1902. Dutch trans.: *De Sterren . . .* Leiden, 1903, 12+284 p. Japanese trans.: [*Study of the Universe, Stars and Planets, Astronomy*], Tokyo, 1906, 362 p.
118. *Elements of Astronomy*, New York, 1900, 240 p.; reprinted 11 times since 1907, in 1909, 1910, 1911, and 1918.
119. "An astronomer's friendship," *Atlantic Mo.*, v. 86, 1900, p. 688-693; *Side-lights on Astronomy*, 1906, p. 227-235 under title "An astronomical friendship." German trans.: "Eine Ehrenrettung nach hundert Jahren," *Wissenschaftliche Beilage zur Germania*, no. 16, 1901, p. 125-127.
120. "Professor Thomas Craig, Ph.D.," *AJM*, v. 22, 1900, one unnumbered page
121. *His Wisdom, the Defender: a Story*, New York, 1900, 7+328 p.
122. "Acceleration," "Algebra," "Algol," "Almanac," "Almucantar," "Altazimuth," "Analysis," "Angle," "Asteroids," "Astronomy," "Aurora," "Binary system," "Calculus," "Collimation," "Collimator," "Comets," "Composition of forces," "Curves," "Eclipse," "Energy," "Equation," "Falling bodies," "Fluxions," "Functions," "Geodesy," "Geometry," "Imaginary quantities," "Incommensurables," "Infinites," "Interpolation," "Jupiter," "Light," "Limits,"

"Logarithms," "Magic squares," "Mars," "Mathematics," "Mercury," "Moon," "Nebular hypothesis," "Observatory," "Occultations," "Orbit," "Parallax," "Perturbations," "Photometry," "Planet," "Precession of the equinoxes," "Probability," "Progression," "Ptolemaic system," "Quadrature of the circle," "Quaternions," "Saturn," "Series," "Solar parallax," "Solar system," "Stars," "Sun," "Telescope," "Time," "Transit," "Transits of Venus," "Trigonometry," "Trilinear coordinates," "Twilight," "Universe," "Venus," "Vulcan," "Year," "Zodiacal light," *Universal Cycl. and Atlas*, newly rev. and enl., New York, 1901. [S. Newcomb was the "Associate editor" in "astronomy and mathematics."]

123. "Action and reaction," "Axiom" (in part), "Calculus," "Capacity" (in phys.), "Centre of mass or gravity," "Centrifugal force," "Density," "Dynamics," "Energy," "Equilibrium," "Ether," "Extension" (in phys.), "Finite" (in math.), "Force," "Geometry," "Gravitation," "Impenetrability," "Inertia" (in phys.), "Infinite" (in math.), "Infinitesimal" (in math.), "Infinity," "Kinetic," "Kinetics," "Latent heat," "Limits" (in math.), "Mass" (in phys.), "Matter," "Measurement," "Mechanical equivalent" (of heat), "Mechanics," "Mobility," "Movement" (of force), "Momentum," "Motion and rest" (in phys.), "Nebular hypothesis," "Parallelogram of forces," "Perpetual motion," "Personal equation," "Physical science," "Point" (in geom.), "Potential," "Ptolemaic theory," "Resultant," "Space" (in math.), "Statics," "Theory" (in science), "Unit" (of physical measurement), "Value" (in physical science), "Variable (and constant) quantity," "Vibration," "Vis viva," "Work," *Dictionary of Philosophy and Psychology*, ed. by J. M. Baldwin, New York, 1901-02.

124. "Astronomy," "Eclipse," "Moon," "Sun," "Telescope," *Encycl. Brit.*, 10th ed., 1902.

125. *Astronomy for Everybody: a Popular Exposition of the Wonders of the Heavens*, New York, 1902, 15+333 p. ("The present work grew out of articles contributed to *McClure's Magazine* a few years since on the unsolved problems of astronomy, total eclipses of the sun and other subjects." Preface.); London, 1903, 15+341 p.; cheap ed., 1907, 16+341 p.; other reprints 1919, 1923, and many of recent date.

Russian trans.: *Astronomiia dliu Vsekh . . .*, Odessa, 1905, 14+285 p.; 2d ed., 1911, 20+288 p. German trans.: *Simon Newcomb's Astronomie für Jedermann . . .* Jena, 1907, 8+364 p.; 2d ed., 1910, 10+366 p.+6 maps; 3d ed., 1920, 12+385 p.; 4th ed., 1921, 8+409 p., mit Titelbild, 3 Tafeln, 3 Sternkarten und 89 Abbildungen.

Bohemian trans.: *S. Newcombova Astronomia pro Každého . . .*, Prague, 1909, 391 p.+5 plates (Portrait).

Swedish trans.: *Newcomb Astronomi för Alla, en Populär Framställning av Himmelsföreteelserna*, Stockholm, 1909, 10+308 p.

126. "The fairyland of geometry," *Harper's Mag.*, v. 104, 1902, p. 249-252; *Side-lights on Astronomy*, 1906.

127. "The universe as an organism," *Science*, n.s., v. 17, 1903, p. 121-129; *Scientific Amer. Suppl.*, v. 55, 1903, p. 22694-22696; *Side-lights on Astronomy*, 1906, p. 300-311.

French trans.: "L'univers comme organisme," *Revue Scientifique*, s. 4, v. 19, 1903, p. 321-326.

German trans. (abridged): "Das Weltall als einheitlicher Organismus," *Astronomische Rundschau*, v. 5, no. 44, 1903, p. 113-119.

128. *The Reminiscences of an Astronomer*, Boston, 1903, 12+424 p.

129. "An account of Professor Runkle's *Mathematical Monthly*," *AMM*, v. 10, 1903, p. 130-133.

130. "The end of the world: a story," *McClure's Mag.*, v. 21, 1903, p. 3-14.

Japanese trans. by Kuroiwa Ruiko in daily newspaper *Yorodzu Choho*, Tokyo, May 6-25, 1904.

131. "Asteroids," "Astronomy," "Astronomy: History," "Astronomy: Practical," "Astronomy: Theoretical," "Aurora Borealis," "Clock," "Geodesy," "Gravitation," "Horizon," "Mercury," "Parallax," "Refraction," "Saturn," "Scintillation," "Solar System," "Stars," "Sun," "Time," "Time: Measurement of," "Transits," "Universe," *Encycl. Amer.*, 1904. (S. Newcomb was the "department and advisory editor" in astronomy for this work.)

132. "The extent of the universe," *Harper's Mag.*, v. 109, 1904, p. 795-801; *Side-lights on Astronomy*, 1906, p. 60-65; *Harvard Classics*, ed. by Charles W. Eliot; *Scientific papers: phys.*,

chem., astr., geology, with introd., notes, and illus., v. 30, 1910, p. 323–326.

133. "The mariner's compass," *Harper's Mag.*, v. 108, 1904, p. 422–427; *Side-lights on Astronomy*, 1906, p. 140–154.

134. "The evolution of the scientific investigator," *Congress of Arts and Science, Universal Exposition, St. Louis, 1904*, ed. by H. J. Rogers, v. 1, Boston, 1905, p. 135–147 [Introd. add. as P Intern. Congress Arts and Sci., St. Louis Exposition, Sept. 19, 1904]; *Science*, v. 20, 1904, p. 92–96; *Scientific Amer. Suppl.*, v. 58, 1904, p. 24098–24100; *Pop. Sci. Mo.*, v. 66, 1904, p. 92–96; as pamphlet, St. Louis, Universal Exposition, 1904, 24 p.; *Smithsonian Report, 1904*, 1905, p. 221–233 ("reprinted from author's revised copy"); *Side-lights on Astronomy*, 1906, p. 236–257; *Engineering Ed., Essays for English*, selected and ed. by R. P. Baker, 1919, p. 3–28.

135. "Our antiquated method of electing a president," *N. Amer. Rev.*, v. 180, 1905, p. 9–18.

136. "Life in the universe," *Harper's Mag.*, v. 111, 1905, p. 404–408; *Side-lights on Astronomy*, 1906, p. 120–132.

137. *A Compendium of Spherical Astronomy with its Application to the Determination and Reduction of Positions of the Fixed Stars*, New York and London, 1906, 18+444 p.

138. *Side-lights on Astronomy and Kindred Fields of Popular Science: essays and addresses*, New York and London, 1906, 7+349 p. +portrait; reprinted 1909, 1914, 1920.

139. "Methods of teaching arithmetic," *Ed. Rev.*, v. 31, 1906, p. 339–350; *Nat. Educ. Assoc., Proc.*, 1906, p. 686–699.

140. *Investigation of Inequalities in the Motion of the Moon, Produced by the Action of the Planets* (assisted by F. E. Ross), (CI Pub. 72) 1907, 8+160 p.

141. "University athletics," *N. Amer. Rev.*, v. 185, 1907, p. 353–364; *College and the Future, Essays for the Undergraduate on Problems of Character and Intellect*, ed. by R. A. Rice, 1915 [one of 18 articles].

142. Problem: "A pack of cards of any specification is taken—say that there are p cards marked 1, q cards 2, r cards 3, and so on—and, being shuffled, is dealt out on a table; so long as the cards that appear have numbers that are in descending order of magnitude they are placed in one pack together—equality of number counting as descending order—but directly the descending order is broken a fresh pack is commenced, and so on until all the cards have been dealt. The probability that there will result exactly m packs or at most m packs is required," *RS Phil Trans.*, s. A, v. 207, 1908, p. 65; P. A. MacMahon, *Combinatory Analysis*, 1915, Section IV: "The Theory of Composition of Numbers," Chap. IV, "Simon Newcomb's problem," p. 187 f. See also Newcomb's letter about this problem in *Observatory*, 1925, p. 122–123.

143. "The prospect of aerial navigation," *N. Amer. Rev.*, v. 187, 1908, p. 337–347.

144. "The problem of aerial navigation," *Nineteenth Century*, v. 64, 1908, p. 430–442; *Living Age*, v. 259, 1908, p. 195–205.

145. "La théorie du mouvement de la lune, son histoire et son état actuel," *Rev. Générale des Sci. Pures et Appliquées*, v. 19, 1908, p. 686–691; *Intern. Congress Mathems.*, Rome, v. 1, 1909, p. 135–143; as pamphlet, Rome, 1908, 10 p.

146. Fluctuations in the moon's mean motion," *RAS MN*, v. 69, 1909, p. 164–169.

147. "Modern occultism," *Nineteenth Century*, v. 65, 1909, p. 126–139; *Living Age*, v. 260, 1909, p. 387–398.

148. "Astronomy, Descriptive," "Astrophysics," "Comet," "Eclipse" (four of five sections), "Ecliptic," "Gravitation" (in part), "Jupiter: Satellites," "Latitude," "Light: Velocity," "Mars," "Moon," "Orbit," "Parallax," "Planet," "Planets: Minor," "Refraction: Astronomical Refraction," "Saturn," "Solar system," "Time: Standard," "Uranus (astronomy)," "Venus (astronomy)," "Zodiacal light," *Encycl. Brit.*, 11th ed., v. 2, 1910, p. 800–808, 819; v. 6, 1910, p. 759–763 +plates; v. 8, 1910, p. 891–895; v. 12, 1910, p. 384–385; v. 15, 1911, p. 564–565; v. 16, 1911, p. 267–268, 623–626; v. 17, 1911, p. 761–765; v. 18, 1911, p. 154–155, 802–807 +plates; v. 19, 1911, p. 385–387; v. 20, 1911, p. 164–165, 760–762; v. 21, 1911, p. 714–719 +plates, v. 23, 1911, p. 29; v. 24, 1911, p. 231–232; v. 25, 1911, p. 357–358; v. 26, 1911, p. 987–988, v. 27, 1911, p. 788–789, 1013–1014; v. 28, 1911, p. 998–1000.

149. "Researches on the motion of the moon, Part II. The mean motion of the moon and

other astronomical elements derived from observations extending from the period of the Babylonians until A.D. 1908," *APAE*, v. 9, pt. 1, 1912, 249 p. [Author's preface dated June 15, 1909. He died July 11, 1909.] See no. 39.

5. ROBERT SIMPSON WOODWARD

CURRICULUM VITAE.—B. Rochester, Mich. 21 July 1849; d. Washington, D. C. 29 June 1924. Received preparatory educ. at the acad. in his native town before entering U. Michigan (68-72; C. E. 72). Assist. engineer U. S. Lake Survey 72-82; assist. astronomer U. S. Venus commission 82-84; astronomer, geographer, and chief geographer U. S. Geol. Survey 84-90; assist. U. S. Coast and Geodetic Survey 90-93. Prof. mechanics Columbia U. (93-99; dean of school of pure science 95-04; prof. mechanics and math. phys. 99-04). P Carnegie Institution of Washington 13 Dec. 1904-1 Jan. 1921.

HONORS.—Assoc. ed. *AM* June 88-June 99. VP AAAS and chm. Sect. A, math. and astr. 89. Hon. Ph.D. U. Michigan 92. Assoc. ed. *Science* 94-24. Treas. AAAS 95-24. Treas. AMS 95-96. Mem. NAS 96. Assoc. fellow AACAS 96. VP AMS 97-98; P 99-00. P AAAS 01. P N. Y. Acad. Sci. 01. Mem. Amer. Phil. So. 02. Hon. LL.D. U. Wisconsin 04. Hon. Sc.D. Columbia U. 05. Hon. Sc.D. U. Pennsylvania 05. Starred *Amer. Men Sci.* 06. P Phil. So. Wash. 10. Hon. LL.D. U. Michigan 12. P Lit. So. Wash. 13-14. Hon. LL.D. JHU 15. P Wash. Acad. Sci. 15. Mem. Naval Consulting Board 15-24. Chm. Sect. on astr., meteorology, seismology, Second Pan-Amer. Scientific Congress, Washington, D. C. 16.

BIOGRAPHICAL NOTES.—Dr. Woodward was a son of Lysander and Peninah A. (Simpson) Woodward. His father, who was of New England ancestry, settled in Michigan about 1835. He was one of the most progressive farmers of the state, sought to apply scientific principles to the operation of his farm, and took a keen interest in public affairs. His mother belonged to a family prominent in the annals of Connecticut. Already in his primary triangulation work on the Great Lakes Dr. Woodward acquired what turned out to be a life-long interest in the earth as a whole—its shape, its tides, its atmosphere, and a host of geophysical problems, many of which still await solution. The service on the Venus Commission was under Asaph Hall, the discoverer of the satellites of Mars. Thus twelve years after graduation were spent in geodetic and astronomical work of the highest precision. It was during the next six years that Woodward wrote his most important scientific papers (e.g. nos. 19, 26, 27, 28). These contributions were geophysical, having in part to do with the deformation of the earth's surface as the result of the removal or addition of load over a large area, and in part with the secular cooling of the earth. He also studied the field methods for topographical mapping and for primary and secondary triangulation and put them on a practical engineering basis. During his years with the Coast and Geodetic Survey he worked on the problem of base-line measurement in primary triangulation, and he developed the iced-bar apparatus for measuring base-lines and calibrating steel tapes and was the first to prove that base-lines could be measured with sufficient accuracy by means of long steel tapes. This work was of fundamental importance to geodesy and resulted in the saving of much expense and

time in field work; also it placed the primary triangulation work of the Coast and Geodetic Survey on a higher plane than had been previously possible.

During the twelve years at Columbia he was remarkably successful both as teacher and as administrator. He had a most attractive, genial, and lovable personality, and his advice was being so constantly sought by students and members of the faculty, that he found it very difficult to pursue the mathematical work to which he had looked forward. He was a member of the Society from May 1891 and became successively its treasurer, vice-president and president. His *Higher Mathematics* (no. 43) edited in collaboration with Mansfield Merriman (1848–1925), in different forms attained to some popularity, and his own part has been translated into French since his death. More than one of his publications display power in applying mathematics to practical problems. Among the 80 mathematicians and 150 physicists arranged according to their rating by colleagues in 1903 Woodward was twenty-first in the first group and eleventh in the second (*Amer. Men Sci.*, 5th ed.).

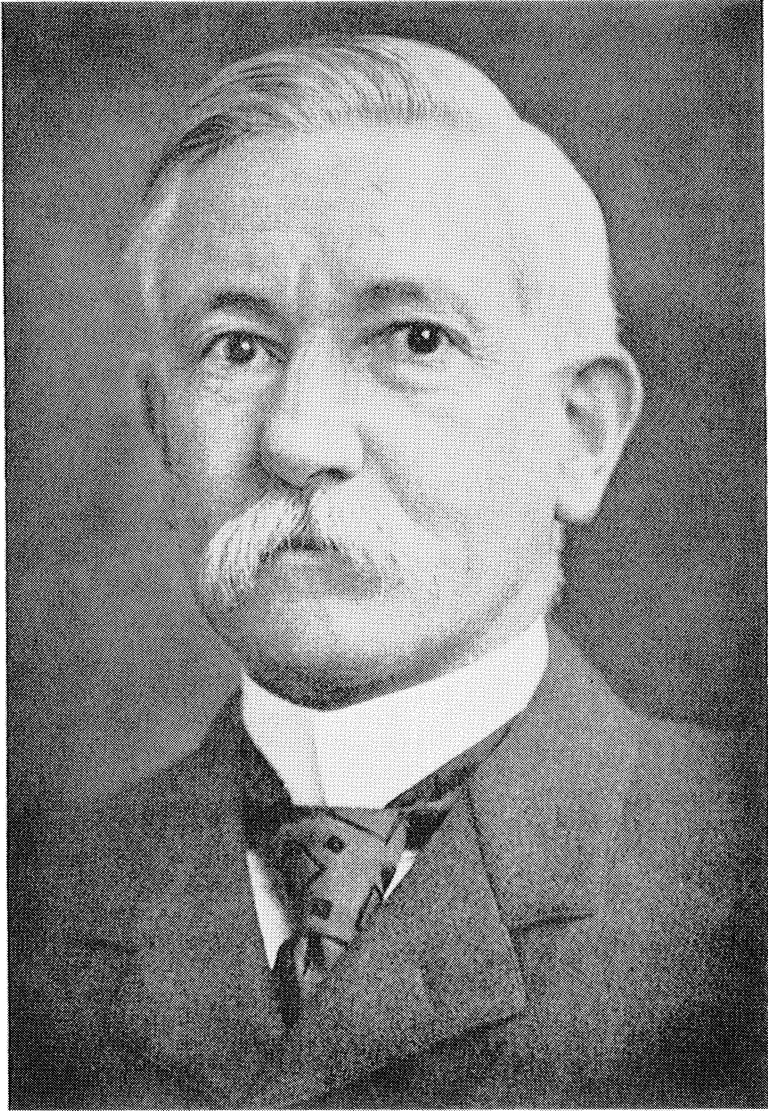
Andrew Carnegie gave bonds valued at more than ten million dollars to establish at Washington an Institution to promote study and research. Daniel C. Gilman, president emeritus of the JHU, was its first president, but he undertook the task only temporarily until the best man for the position could be selected. When Dr. Woodward became president, the Institution was only two years old and had still to determine the best policies to follow. At this critical period, his mature judgment and experience, his clarity of vision, common sense, enthusiasm, and geniality, led, after much travail, to the establishment on a firm foundation of an Institution which has very notably promoted learning in this country. On looking back over his years of activity, he states in his last report as president that "probably no other organization in the evolution of learning has been so beset by what Dr. Johnson called the anfractuositities of the human mind as the Carnegie Institution of Washington." Prof. J. M. Cattell reports that the late physicist, Prof. O. N. Rood, once said that "he liked to go to faculty meeting in order that he might sit and look at Woodward" (*Columbia U. Quart.*, v. 7).

Karl W. Woodward, professor of forestry at the U. New Hampshire is one of three sons of Dr. Woodward.

SOURCES.—F. E. Wright, memoir, bibl., portrait, *Geol. So. Amer., Bull.*, v. 37, 1926. F. E. Wright, *DAB*, v. 20, 1936. *Universities and their Sons*, Boston, v. 2, 1899, portrait. *Nat. Cycl. Amer. Biog.*, v. 13, 1906, portrait. *Who's Who in Amer.*, v. 12, 1922. *Amer. Men Sci.*, 3d and 5th eds.

BIBLIOGRAPHY

1. "Determination of the errors of graduation of Troughton and Simms theodolite number 2," App. E, *U. S. Lake Survey Report for 1875*, 5 p.
2. "Constants of Troughton and Simms theodolite number 3," App. 7, *U. S. Lake Survey Report for 1879*, 7 p.



R.S. Woodward

1900

3. *Primary Triangulation of the United States Lake Survey*, Professional Papers, Corps of Engineers, U. S. Army, no. 24, chap. 16–20, 24–25, 1882, 288 p.

4. "On the actual and probable errors of interpolated values derived from numerical tables by means of first differences," *Analyst*, v. 9, 1882, p. 143–149, 169–175.

5. "Results of some experiments made to determine the variations in length of certain bars at the temperature of melting ice" (with E. S. Wheeler, A. R. Flint, and W. Voigt), *AJS*, s. 3, v. 25, 1883, p. 448–459; abstract in *Zeitsch. f. Instrumentenkunde*, v. 3, 1883, p. 322–324.

6. "The special treatment of certain forms of observation equations" (abstract), Wash. Phil. So., *Bull.*, v. 6, 1883, p. 156–157; *Smithsonian Misc. Coll.*, v. 33, 1888, Art. 1.

7. "Note on the optical formula expressing the relation of conjugate distances, and on the theory of stadia," *Van Nostrand's Engin. Mag.*, v. 30, 1884, p. 473–476.

8. "On variations in latitude" (abstract), Wash. Phil. So., *Bull.*, v. 8, 1885, p. 10.

9. "Some practical features of a field time determination with a meridian transit," Wash. Phil. So., *Bull.*, v. 8, 1886, p. 55–58; *Smithsonian Misc. Coll.*, v. 33, 1888, Art. 3.

10. "On the errors incident to values interpolated by means of first differences from tables of logarithms, natural trigonometric functions, etc.," *AM*, v. 2, 1886, p. 54–59.

11. "On the rate of recession of Niagara Falls, as shown by results of a recent survey" (abstract), *AAAS Proc.*, v. 35, 1886, p. 222.

12. "Is the ocean surface depressed?" *Science*, v. 7, 1886, p. 570–571.

13. "On the form and position of the sea-level as dependent on superficial masses symmetrically disposed with respect to a radius of the earth's surface," *AM*, v. 2, 1886, p. 97–103, 121–131; v. 3, 1887, p. 11–26.

14. "On the free cooling of a homogeneous sphere, of initial uniform temperature in a medium which maintains a constant surface temperature," *AM*, v. 3, 1887, p. 75–88.

15. "On a method of computing the secular contraction of the earth" (abstract), *AAAS Proc.*, v. 37, 1887, p. 59.

16. "On the conditioned cooling and the cubical contraction of a homogeneous sphere," *AM*, v. 3, 1887, p. 129–144.

17. "On a method of determining the emissivity of a metallic bar cooling or heating in air" (abstract), *AAAS Proc.*, v. 37, 1888, p. 84.

18. "On the diffusion of heat in a homogeneous rectangular mass, with special reference to bars used as standards of length," *AM*, v. 4, 1888, p. 101–127; abstract in *AAAS Proc.*, v. 37, 1888, p. 79.

19. *On the Form and Position of the Sea Level, with Special Reference to its Dependence on Superficial Masses Symmetrically Disposed about a Normal to the Earth's Surface* (U. S. Geol. Survey, *Bull.* no. 48), Wash., 1888, 88 p.; 50th Congress, 2d Session, House, Misc. doc. 138; abstract in *AAAS Proc.*, v. 37, 1888, p. 79.

20. "On the variation of terrestrial density, gravity, and pressure, according to the Laplacian law" (abstract), Wash. Phil. So., *Bull.*, v. 11, 1889, p. 580.

21. "Mathematical theory of the stratum of no strain and its applications to the earth" (abstract), Wash. Phil. So., *Bull.*, v. 11, 1889, p. 602.

22. "Some mechanical conditions of the earth's mass" (abstract), Wash. Phil. So., *Bull.*, v. 11, 1889, p. 532–533.

23. "Some of the greater problems of physical geology," Wash. Phil. So., *Bull.*, v. 11, 1889, p. 537.

24. Administrative report, Div. of geography, U. S. Geol. Survey, *Report 1886–87*, 1889, p. 121–124.

25. Administrative reports, Math. div., U. S. Geol. Survey, *Report 1887–88*, p. 68–71; *1888–89*, pt. 1, p. 106–108; *1889–90*, pt. 1, p. 128–129; 1889–91.

26. *Latitudes and Longitudes of Certain Points in Missouri, Kansas, and New Mexico* (U. S. Geol. Survey, *Bull.* no. 49), Wash., 1889, 133 p.; 50th Congress, 2d session, House, Misc. doc. 138.

27. *Formulas and Tables to Facilitate the Construction and Use of Maps* (U. S. Geol. Survey, *Bull.* no. 50), Wash., 1889, 124 p.; 50th Congress, 2d session, House, Misc. doc. 138.

28. "The mathematical theories of the earth," AAAS *Proc.*, v. 38, 1889, p. 49-69; *Science*, v. 14, 1889, p. 167-172; *AJS*, s. 3, v. 38, 1889, p. 337-355; *Amer. Geologist*, v. 4, no. 5; Smithsonian Inst., *Annual Report 1890*, Wash., 1891, p. 183-200. Add. VP AAAS and chm. Sect. A 28 Aug. 1889.
29. "Concerning thermometers," part II (abstract), AAAS *Proc.*, v. 38, 1889, p. 135-136. [Part I of abstract was by W. R. Rogers.]
30. "The effects of the atmosphere and oceans on the secular cooling of the earth" (abstract), AAAS *Proc.*, v. 39, 1890, p. 90.
31. (a) "On the deformation of the geoid by the removal, through evaporation, of the water of Lake Bonneville"; (b) "On the elevation of the surface of the Bonneville basin by expansion due to change of climate"; App. B and C of G. K. Gilbert, *Lake Bonneville* (U. S. Geol. Survey, *Monographs*, v. 1), 1890, (a) p. 421-424; (b) p. 425-426.
32. *Report on Astronomical Work of 1889 and 1890. Fixation of the 105th meridian in El Paso County, Texas* (U. S. Geol. Survey, *Bull.* no. 70), Wash., 1890, 79 p.; 52d Congress, 1st session, House, Misc. doc. 21.
33. "Preliminary account of the iced-bar base apparatus of the U. S. Coast and Geodetic Survey," *AJS*, s. 3, v. 45, 1893, p. 33-53.
34. "Recent experience on the U. S. Coast and Geodetic Survey in the use of long steel tapes for measuring base lines" (with discussion), *Amer. So. Civil Engin., Trans.*, v. 30, pt. 2, 1893, p. 81-107, 638-652.
35. "On the measurement of the base lines at Holton, Indiana and at St. Albans, West Virginia 1891 and 1892," Reports of the measurement of Holton base, by A. T. Mosman, R. S. Woodward, and O. H. Tittmann, assists., and of the St. Albans base by R. S. Woodward, assist., U. S. Coast and Geodetic Survey, *Report for 1892*, 1893, App. 8, p. 329-503.
36. *Smithsonian Geographical Tables* (*Smithsonian Misc. Coll.*, v. 35), 1894, 3+v-cv+182 p. Also 3d ed. (*Smithsonian Misc. Coll.*, v. 854), 1906.
37. "An historical survey of the science of mechanics," *Science*, n.s., v. 1, 1895, p. 141-157.
38. "On the condition of the interior of the earth" (with discussion), (abstract), *N.Y. Acad. Sci., Trans.*, v. 14, 1895, p. 72-76. Add. *N.Y. Acad. Sci.*, Nov. 1894.
39. "On the measurement of horizontal angles," *Engin. So. School of Mines, Columbia C., Proc.*, 1895.
40. "Mechanical interpretation of the variations of latitudes," *AJ*, v. 15, 1895, p. 65-72, 88.
41. "Systems of mechanical units" (abstract), *N.Y. Acad. Sci., Trans.*, 1895.
42. "A course of study in the physical sciences. Mechanics," *SPEE Proc.*, v. 3, 1896, p. 229-241.
43. *Higher Mathematics. A Text-book for Classical and Engineering Colleges* (ed. with M. Merriman), New York, 1896, xi+576 p.; 2d ed. rev., 1898. This v. contains 11 chaps. by 11 authors, including Woodward, "Probability and theory of errors," chap. 10, p. 467-507. After 1898 these chaps. were reprinted as the first 11 v. in the Series *Mathematical Monographs*, and a number of the v. went through several eds. Of Woodward's chap. the v. was no. 7 and the 4th ed. appeared in 1906, iii+[7]-47 p. French translation by A. Sallin, *Calcul des Probabilités et Théories des Erreurs*, Paris, 1930, vii+56 p.
44. *History of the Smithsonian Institution, 1846-1896*, Wash., 1897, "Mathematics," p. 561-570.
45. "The *Annals of Mathematics*," *Alumni Bull., U. of Va.*, v. 3, 1897, p. 71-72.
46. "Notice of De Volson Wood," *Science*, n.s., v. 6, 1897, p. 204-206; *SPEE Proc.*, v. 5, 1898, p. 325-329.
47. "The mass of the earth's atmosphere," *Science*, n.s., v. 6, 1897, p. 819.
48. "Modification of the Eulerian cycle due to inequality of the equatorial moments of inertia of the earth" (abstract), AAAS *Proc.*, v. 46, 1897, p. 60.
49. "Integration of the equations of motion of a non-rigid mass for the case of equal principal moments of inertia" (abstract), AAAS *Proc.*, v. 46, 1897, p. 61.
50. "On the gravitational constant and the mean density of the earth," *AJ*, v. 18, 1898, p. 121-122.

51. "A national observatory," *Science*, n.s., v. 9, 1899, p. 470-471.
52. "The century's progress in applied mathematics," *AMS Bull.*, v. 6, 1900, p. 133-163; *Science*, n.s., v. 11, 1900, p. 41-51, 81-92. AMS P add. 28 Dec. 1900.
German trans.: "Die Fortschritte der angewandten Mathematik im letzten Jahrhundert," *Naturw. Rundschau*, v. 5, 1900, p. 249-252, 262-266, 273-276.
Polish trans. by S. Dickstein, "Postepy matematyki stosowanej w XIX stuleciu," *Wiadomości Matematyczne*, v. 5, 1909, p. 17-51.
53. Address of president of AAAS, *Science*, n.s., v. 12, 1900, p. 12-15.
54. "Observation and experiment," *Science*, n.s., v. 13, 1901, p. 521-530; *N. Y. Acad. Sci., Annals*, v. 14, 1901, p. 69-84. P add. *N. Y. Acad. Sci.* 25 Feb. 1901.
55. "The effects of secular cooling and meteoric dust on the length of the terrestrial day," *AJ*, v. 21, 1901, p. 169-175.
56. "The progress of science," *Science*, n.s., v. 14, 1901, p. 305-315; *Pop. Sci. Mo.*, v. 59, 1901, p. 513-525; *Nature*, v. 64, 1901, p. 498-502. P add. AAAS 27 Aug. 1901.
57. "Measurement and calculation," *Science*, n.s., v. 15, 1902, p. 961-971. Also *N.Y. Acad. Sci., Annals*, v. 15, p. 22-39. P add. *N.Y. Acad. Sci.* 24 Feb. 1902.
58. "Education and the world's work of today," Commencement address read at Rose Polytechnic Institute, June 11, 1903, *Terre Haute Evening Gazette*, June 11, 1903; *Science*, n.s., v. 18, 1903, p. 161-169.
59. "The international conference of arts and science," *Science*, n.s., v. 18, 1903, p. 302-303.
60. "A new method of integrating one of the differential equations of the theory of heat diffusion," *Phys. Rev.*, v. 16, 1903, p. 176-177.
61. "William Harkness, 1837-1903," *Wash. Acad. Sci., Proc.*, v. 5, 1904, p. 381-383.
62. "The unity of physical science," *Science*, n.s., v. 20, 1904, p. 417-426; *Congress of Arts and Science, Universal Exposition, St. Louis, 1904*, v. 4, 1906, p. 3-14.
63. "Academic ideals," address at the opening exercises of Columbia University, September 28, 1904, 10 p. Also *Science*, n.s. v. 21, 1905, p. 41-46.
64. Reports as president of Carnegie Institution of Washington, *Yearbook*, no. 4-19, 1905-20, 409 p.; extracts in *Science*, n.s., v. 23, 25, 39, 45, 46, 50, 1906-19.
65. "Joseph Henry," *Pop. Sci. Mo.*, v. 70, 1907, p. 299-300, with portrait.
66. "The point of view in teaching engineering mathematics," *Science*, n. s., v. 28, 1908, p. 134-138.
67. "Our educational opportunities and how to use them," Commencement address at Carnegie Technical Schools, Pittsburgh, 1908.
68. "Conduct of scientific work under United States Government," Message from the President of U. S., transmitting report of the NAS (prepared by a comm., R. S. Woodward, chm.), Wash., Govt. Printing Office, 1909, 5 p.; 60th Congress, 2d session, House, doc. 1337; *Science*, n.s., v. 29, 1909, p. 217-220.
69. "The atmosphere," *Mount Weather Obs., Bull.*, v. 2, 1910, pt. 5, p. 1-11.
70. "The orbits of freely falling bodies," *AJ*, v. 28, 1913, p. 17-29; semi-popular art., *Science*, n.s., v. 38, 1913, p. 315-319.
71. "The laws of falling bodies" (abstract), *Wash. Acad. Sci., Journ.*, v. 3, 1913, p. 426.
72. "Note on the orbits of freely falling bodies," *Science*, n.s., v. 41, 1915, p. 492-495.
73. "Compressibility of the earth's mass" (abstract), *Wash. Acad. Sci., Journ.*, v. 5, 1915, p. 251.
74. "The earth" (abstract), *Wash. Acad. Sci., Journ.*, v. 5, 1915, p. 554.
75. "Extraction of square roots of numbers" (abstract), *Wash. Acad. Sci., Journ.*, v. 6, 1916, p. 299-300.
76. Pan American Scientific Congress, [Second, Washington, D.C.] *Proc.*, v. 2, *Astronomy, Meteorology, Seismology*, Washington, D.C., 1917. Woodward was chm. of this sect. and the large v. contains his "Foreword," and the reports of his numerous remarks.
77. "The calculus of harmonics and preharmonics and their application in hydromechanics" (abstract), *Wash. Acad. Sci., Journ.*, v. 12, 1922, p. 268.

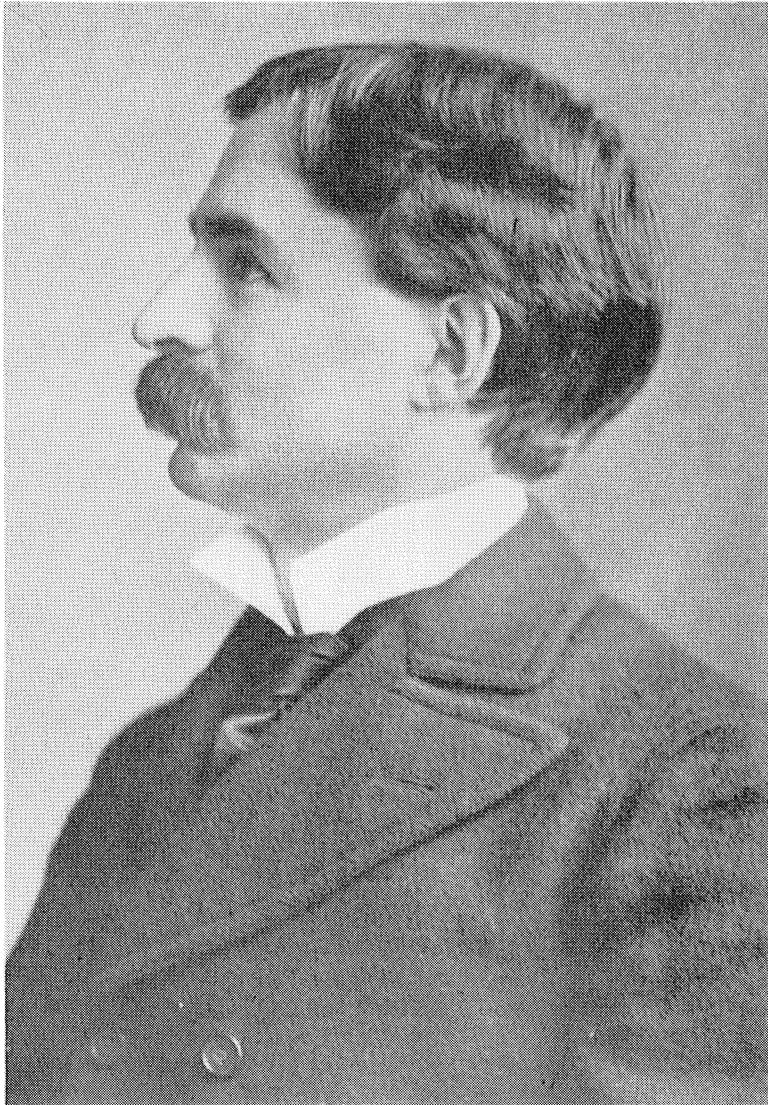
78. "Alfred Goldsborough Mayer," *Science*, n.s., v. 56, 1922, p. 68.
 79. "The compressibility of the earth" (abstract), *Wash. Acad. Sci., Journ.*, v. 13, 1923, p. 44.
 80. "Some extensions in the mathematics of hydromechanics," *NAS Proc.*, v. 9, 1923, p. 13-18.
 81. Reviews of books by Tisserand and Byerly in *AM*, v. 6-8, 1891-94; by Abbe in *NYMS Bull.*, v. 2, 1893; by Ziwet, Greenhill, Hancock, Glazebrook, Routh, Appell, Du Bois, Tait, Wright, Perry, Klein and Sommerfeld, Love, von Helmholtz, Poincaré, of Memoirs presented to Cambridge Phil. So. on occasion of jubilee of Sir G. G. Stokes, of books by Reynolds, Hoskins, Slate, W. W. Johnson, Wernicke, and Riemann in *Science*, n.s., v. 1-14, 1895-1901.

6. ELIAKIM HASTINGS MOORE

CURRICULUM VITAE.—B. Marietta, O. 26 Jan. 1862; d. Chicago, Ill., 30 Dec. 1932. At Woodward high school in Cincinnati prepared (76-79) for Yale U. (79-85; A.B. 83; Ph.D. 85). At U. Berlin (85-86). Instr. at acad., Northwestern U. (86-87). Tutor math. Yale U. (87-89). Assist. prof. Northwestern U. (89-91; assoc. prof. 91-92). Prof. math. U. Chicago (92-32; head of dept. 96-31).

HONORS.—VP Intern. Math. Congress Chicago 93; ed. (with Bolza, Maschke and H. S. White) of *Mathematical Papers read at the . . . Congress*, pub. by AMS 96. VP AMS 98-00. Hon. Ph.D. U. Göttingen 99. Ed. *AMS Trans.* 99-07. Mem. NAS 01. Assoc. fellow AAAS 01. P AMS 01-02. Chm. comm. advising Carnegie Inst. in relation to original research math. 02. Hon. LL.D. U. Wisconsin 04. Chm. algebra and analysis sect. Congress of Arts and Sci., Universal Exposition, St. Louis 04; G. A. Bliss was secy. of this sect. Mem. Amer. Phil. So. 05. Starred *Amer. Men Sci.* 06. Colloq. lect. AMS, New Haven 06; "Introduction to a form of general analysis" (Bibl. no. 47). Mem. ed. comm. *CMP Rend.* 09-14. Lect. Clark U. on 20th anniversary of founding, "The rôle of postulational methods in mathematics" Sept. 09; hon. Math. D. conferred. Hon. Sc.D. Yale U. 09. VP AAAS and chm. Sect. A 11; ret. add. "On the foundations of the theory of linear integral equations" (no. 49). VP Fifth Intern. Congress Mathems., Cambridge, Eng., 12. Hon. corresp. mem. BAAS 12. Chm. board eds. U. Chicago Sci. Series 14-29. Mem. ed. board *NAS Proc.* 15-20. Mem. Nat. Comm. on Math. Requirements, MAA, J. W. Young chm. 18-23. Hon. Sc.D. U. Toronto 21. P AAAS 21; ret. add. "What is a number system," unpub. Eliakim Hastings Moore Fund of AMS established 22; on the occasion of the 25th anniversary meeting of the Chicago group. Hon. Sc.D. Northwestern U. 27. Eliakim Hastings Moore Distinguished Service Professorship established at U. Chicago 29; L. E. Dickson first incumbent. Portrait painted by Ralph Clarkson presented to U. Chicago by Prof. Moore's former students and placed in Eckhart Hall 30.

BIOGRAPHICAL NOTES.—Prof. Moore's grandfather Eliakim Hastings Moore, a banker and treasurer of Ohio U. at Athens, O., was a county officer and collector of internal revenue, and a congressman. Eliakim Hastings the younger served as messenger in Congress during one summer vacation while his grandfather was there. His father was a Methodist minister, David Hastings Moore, and his mother was Julia Carpenter Moore of Athens. The family moved from place to place while E. H. Moore was young, but a considerable part of his childhood was spent in Athens, where one of his playmates was Martha Morris Young, sister of the lamented Prof. J. W. Young of Dartmouth C., who was afterwards to become his wife. His father D. H. Moore, besides being a preacher, was successively a captain, major, and lieutenant colonel in the Civil War; president of Cincinnati Wesleyan C.; an organizer and first Chancel-



E. A. Moore

1902

lor of the U. Denver; and bishop of the Methodist Episcopal Church in Shanghai with jurisdiction in China, Japan and Korea. (This paragraph and much of what follows is taken from sketches written by G. A. Bliss.)

While E. H. Moore was still in high school, Ormond Stone, then director of the Cincinnati Observatory, and later founder of the *AM*, secured him as an emergency assistant. Stone had a high appreciation of mathematics and inspired his young assistant with a first interest in that science. One of Moore's friends at this time was Carl Barus (1856–1935), afterwards to become the distinguished physicist, but then variously employed, in particular as organ pumper for his father. In his reminiscences he tells of initiating Moore "into the art of the organ pumper. Strange as it may seem, in after life we often met at scientific gatherings and we received the honorary doctorate on the same day at Clark U. Who knows what my instruction in organ pumping may have done for Professor Moore?" At Yale H. A. Newton (1830–96), prof. of math. and scientist of distinction, first inspired in him the spirit of research, and was so deeply impressed with the young mathematician's ability he made it possible for him to spend a year in Germany where he studied most of the time at U. Berlin. Here Weierstrass (then 70 years old) and Kronecker were lecturing. The latter especially made a deep impression on Moore as he did on Fine a little earlier, and later.

President Harper had a remarkable capacity for picking young men of genius for the U. Chicago which first opened in the autumn of 1892. Moore was appointed professor and acting head (permanent head four years later) of the department of mathematics. He persuaded the President to associate with him from the very first two unusually fine scholars Oskar Bolza (1857–) and Heinrich Maschke (1853–1908), both former students at U. Berlin and doctors from U. Göttingen. Bolza made it a condition of his acceptance of a call to U. Chicago, that Maschke should receive an appointment at the same time. These three men supplemented one another remarkably. Moore was a fiery enthusiast, brilliant, and keenly interested in the popular mathematical research movements of his day; Bolza, a product of the meticulous German school of analysis led by Weierstrass, was an able, and widely read research scholar; Maschke was more deliberate than the other two, sagacious, brilliant in research, and a most delightful lecturer on geometry. During the period 1892–1908 the U. Chicago was unsurpassed in America as an institution for the study of higher mathematics. At this time such men as Birkhoff and Veblen carried on advanced work at Chicago. "In the lecture room Professor Moore's methods defied most established rules of pedagogy. Such rules, indeed, meant nothing to him in the conduct of his advanced courses. He was absorbed in the mathematics under discussion to the exclusion of everything else, and neither clock time nor meal time brought the discussion to a close. His discourse ended when some instinct told him that his topic

for the day was exhausted." For the *élites* he was enormously inspiring, and among the ablest mathematicians of our country at the present time those who drew their chief inspiration from Prof. Moore are numerous.

The following list of those (31) whose thesis work for the doctorate was done under his direction, 1896–1929, is a very distinguished one: L. E. Dickson, H. E. Slaught, D. N. Lehmer, W. Findlay, O. Veblen, T. E. McKinney, G. D. Birkhoff, N. J. Lennes, F. W. Owens, H. F. MacNeish, R. P. Baker, T. H. Hildebrandt, Anna J. Pell (Mrs. A. L. Wheeler), A. D. Pitcher, R. E. Root, E. W. Chittenden, W. L. Hart (under Moore and F. R. Moulton), M. G. Gaba, C. R. Dines, Mary E. Wells, E. J. Moulton, A. R. Schweitzer, V. D. Gokhale, E. B. Zeisler, J. P. Ballantine, C. E. Van Horn, R. E. Wilson, M. H. Ingraham, R. W. Barnard, H. L. Smith, F. D. Perez.

In chapters VII and V are to be found details concerning the AMS Chicago Section in which Moore figured so prominently, being chairman from its organization in 1897 through 1902; and concerning his remarkable services as editor-in-chief of the *Transactions* during the first seven years of its publication, two of them while P of the Society. He was a prominent organizer of the scientific congress at the World's Columbian Exposition, 1893. At the Universal Exposition of 1904 in St. Louis he was chm. of one of the sections in mathematics. In 1916 by his advice and encouragement he gave great assistance to H. E. Slaught, who was mainly responsible for the founding of the MAA. Besides being long chm. of the board of eds. of U. Chicago Science Series, he was also joint ed. of the U. Chicago Mathematical Series, consisting of secondary school texts. His attempt to help even lower grades is illustrated by his *Grammar School Arithmetic by Grades*, 1897 (no. 19). In his ret. add. as P AMS in 1902 (no. 38) Moore devoted the first part to an illuminating description of his conception of the logical structure of pure and applied mathematics, but the latter part was a discussion of the pedagogical methods, in primary and secondary schools, colleges, and universities, by which one might hope to establish such concepts in the minds of students. The address was prepared at a time when repercussions of the Perry movement in England had started nation-wide discussion of mathematical teaching in this country, and Moore was greatly interested in a laboratory method of instruction for college students.

Turning now to his mathematical research publications, we find that they fall roughly into the following four groups: Geometry (nos. 1–4, 25, 34, 36, 40, 63, 69), 1885–1913; Groups, numbers, algebra (nos. 6, 7, 10, 11, 13, 14, 15, 16, 17, 20, 21, 22, 23, 24, 26, 29, 35, 39, 41, 44, 50, 57, 58, 59, 73, 74, 75, 78), 1892–1922; Theory of functions (nos. 5, 8, 9, 12, 18, 27, 28, 31, 32, 33, 43, 54, 60, 61, 62, 67, 72, 77), 1890–1926; Integral Equations (nos. 46, 47, 49, 51, 52, 53, 56, 64, 65, 68, 70, 71), 1906–1935. This indicates the sequence of his major interests. His studies in algebra and the theory of groups fell in the period of his greatest activity as a writer, while in-

tegral equations and general analysis were his absorbing interest during the latter part of his life when he published least. For general analysis he never lost his enthusiasm.

In geometry, the papers dealt with questions in algebraic geometry, Moore's first mathematical interest, and postulational foundations. It is of special interest that at this time he freely used the theory of linear systems of curves, then of fundamental value, and displayed both skill and power in manipulation of such systems, and discovered elegant results. Hilbert's book of 1899 on the foundations of geometry, and earlier work of Pasch and Peano, as well as of Hilbert, inspired Moore and his disciples to important activity. Moore deftly dealt with independence questions in Hilbert's axioms and gave a new formulation of a system of axioms for n -dimensional geometry, using points only as undefined elements instead of the points, lines, and planes of Hilbert in the three-dimensional case (nos. 34, 36). In algebra Moore's paper at the Chicago Congress of 1893 (no. 14) contained a generalization of the modular group, a statement and proof for the first time of the interesting and important theorem which says that every finite field is a Galois field, and a characterization of a doubly-infinite system of so-called simple groups, only a few of which had been known before. Moore's power in analysis was first displayed in his paper on transcendently transcendental functions (no. 18), which is a model of clarity and elegance and gives evidence of his increasing interest and ingenuity in mathematical generalizations. The subject of space-filling curves of Peano and Hilbert (*MA*, v. 36, 38) was delightfully illuminated in the first number of *AMS Trans.* by an often quoted paper "On certain crinkly curves" (no. 27). His papers on improper definite integrals (31, 32, 33) were important and timely contributions in the period before that of the later and more effective integration theories of Borel and Lebesgue. But the theories of integral equations and general analysis were the subjects which most captivated Moore's exploratory interests. In the years following 1900 the fundamental papers of Fredholm and Hilbert attracted wide attention. Moore saw that the equations which they studied, as well as corresponding and more elementary ones well known in algebra, must be special instances of a much more general linear equation, and he set about the construction of a general theory which should include them all. His guiding principle, as often stated, was that "the existence of analogies between central features of various theories implies the existence of a general abstract theory which includes the particular theories and unifies them with respect to these central features." This principle was the dominant note of his colloq. lectures (no. 47; reviewed by G. D. Birkhoff, with a list of corrections, *AMS Bull.*, v. 17, p. 414-423); these lectures of 1906 were not published until after a related paper (no. 46). In these publications and two later ones (nos. 49, 51) Moore gave in essential outline his first theory of

general analysis and his generalization of preceding theories of linear equations. [An admirable summing up of this theory was given by Bolza in his "Einführung in E. H. Moore's 'General Analysis' und deren Anwendung auf die Verallgemeinerung der Theorie der linearen Integralgleichungen," *DMV, Jahr.*, v. 23, 1914, p. 248–303.] His attack was highly postulational and original, especially in the fact that the postulates applied to classes of functions rather than to individual ones. He was able to secure for his general theory most of the results which are of interest in the more special cases, but some of them eluded him. The attempts which he made in order to complete the theory in these respects led to such complexities that finally, about 1915, he turned from his first method to a second more constructive theory of similar character, but with a much simpler basis. The results which he attained are to be found partly in his memoirs, and partly in mss. With Prof. R. W. Barnard's able cooperation a definitive edition is soon to be available (no. 56) to the scholar desiring to familiarize himself with an extraordinary conception. The ideas here set forth do not, on the whole, seem to have won as general acceptance as the widely differing methods of Banach and his school.

Prof. Moore was an extraordinary genius, "vivid, imaginative, sympathetic," foremost leader in freeing American mathematicians from dependence on foreign universities, and in building up a vigorous American School, drawing unto itself workers from all parts of the world.

SOURCES.—G. A. Bliss, (a) *AMS Bull.*, v. 39, p. 831–838 and v. 40, p. 501–514 (the best discussion of Moore's scientific work); (b) with L. E. Dickson, NAS, *Biog. Mem.*, v. 17, 1936, with portrait. O. Bolza (a) *Aus meinem Leben*, Munich, 1936; (b) "Heinrich Maschke: his life and work," *AMS Bull.*, v. 15, p. 85–95. H. E. Slaught, *AMM*, v. 40, 1933. L. E. Dickson, *Science*, n.s. v. 77, 1933, p. 79–80. *Nat. Cycl. Amer. Biog.*, v. 12, 1904. *Who's Who in Amer.*, v. 17, 1932. *Amer. Men Sci.*, 4th ed. 1927.

BIBLIOGRAPHY

1. "Extensions of certain theorems of Clifford and Cayley in the geometry of n dimensions," *Conn. Acad. Arts and Sci., Trans.*, v. 7, 1885, p. 9–26. Doctoral diss.
2. "Note on space divisions" (with C. N. Little), *AJM*, v. 8, 1886, p. 127–131.
3. "Algebraic surfaces of which every plane-section is unicursal in the light of n -dimensional geometry," *AJM*, v. 10, 1888, p. 17–28.
4. "A problem suggested in the geometry of nets of curves and applied to the theory of six points having multiply perspective relations," *AJM*, v. 10, 1888, p. 243–257.
5. "Note concerning a fundamental theorem of elliptic functions, as treated in Halphen's *Traité*, vol. 1, pages 39–41," *CMP Rend.*, v. 4, 1890, p. 186–194.
6. "Concerning triple systems," *MA*, v. 43, 1893, p. 271–285.
7. "The group of holoedric transformations into itself of a given group," *AMS Bull.*, v. 1., 1894, p. 61–66.
8. "Concerning the definition by a system of functional properties of the function $f(z) = (\sin \pi z)/\pi$," *AM*, v. 9, 1895, p. 43–49.
9. "On a theorem concerning p -rowed characteristics with denominator 2," *AMS Bull.*, v. 1, 1895, p. 252–255.
10. "Concerning triple systems," *CMP Rend.*, v. 9, 1895, p. 86.
11. "Concerning Jordan's linear groups," *AMS Bull.*, v. 2, 1895, p. 33–43.

12. "A note on mean values," *AMM*, v. 2, 1895, p. 303-304.
13. "On an interesting system of quadratic equations" (with E. C. Ackermann), *AMM*, v. 3, 1896, p. 38-41.
14. "A doubly-infinite system of simple groups," *Intern. Congress Mathems.*, Chicago, 1896, p. 208-242; abstract, *NYMS Bull.*, v. 3, 1893, p. 73-78.
15. "A two-fold generalization of Fermat's theorem," *AMS Bull.*, v. 2, 1896, p. 189-199.
16. "Tactical memoranda I-III," *AJM*, v. 18, 1896, p. 264-303.
17. "Concerning the abstract groups of order $k!$ and $(k!/2)$ holoeidrically isomorphic with the symmetric and the alternating substitution-groups on k letters," *LMS Proc.*, v. 28, 1896, p. 357-366.
18. "Concerning transcendently transcendental functions," *MA*, v. 48, 1897, p. 49-74.
19. *Grammar School Arithmetic*, by Grades, ed. by E. H. Moore, New York, etc., 1897, 344 + xvi p.
20. "The decomposition of modular systems of rank n in n variables," *AMS Bull.*, v. 3, 1897, p. 372-380.
21. "Concerning regular triple systems," *AMS Bull.*, v. 4, 1897, p. 11-16.
22. "An universal invariant for finite groups of linear substitutions: with application in the theory of the canonical form of a linear substitution of finite period," *MA*, v. 50, 1898, p. 213-219.
23. "Concerning Abelian-regular transitive triple systems," *MA*, v. 50, 1898, p. 225-240.
24. "Concerning the general equations of the seventh and eighth degrees," *MA*, v. 51, 1899, p. 417-444.
25. "The cross-ratio group of $n!$ Cremona transformations of order $n-3$ in flat space of $n-3$ dimensions," *AJM*, v. 22, 1900, p. 279-291.
26. "A fundamental remark concerning determinantal notations with the evaluation of an important determinant of special form," *AM*, s. 2, v. 1, 1900, p. 177-188.
27. "On certain crinkly curves," *AMS Trans.*, v. 1, 1900, p. 72-90, 507.
28. "A simple proof of the fundamental Cauchy-Goursat theorem," *AMS Trans.*, v. 1, 1900, p. 499-506.
29. "Concerning Klein's group of $(n+1)!$ n -ary collineations," *AJM*, v. 22, 1900, p. 336-342.
30. "The undergraduate mathematical curriculum," Report of discussion at summer meeting AMS, June 1900, *AMS Bull.*, v. 7, 1900, p. 15-16.
31. "Concerning Harnack's theory of improper definite integrals," *AMS Trans.*, v. 2, 1901, p. 296-330.
32. "On the theory of improper definite integrals," *AMS Trans.*, v. 2, 1901, p. 459-475.
33. "Concerning Du Bois-Reymond's two relative integrability theorems," *AM*, s. 2, v. 2, 1901, p. 153-158.
34. "On the projective axioms of geometry," *AMS Trans.*, v. 3, 1902, p. 142-158.
35. "A definition of abstract groups," *AMS Trans.*, v. 3, 1902, p. 485-492.
36. "The betweenness assumptions," *AMM*, v. 9, 1902, p. 152-153.
37. Report (with F. Morley, and O. Stone) of Advisory Comm. on Math., Carnegie Inst., *Yearbook*, v. 1, 1902, p. 232-236.
38. "On the foundations of mathematics," *AMS Bull.*, v. 9, 1903, p. 402-424; *Science*, n.s., v. 17, 1903, p. 401-416; Nat. Council Teachers Math., *Yearbook*, v. 1, 1926, p. 32-57. AMS ret. P add. 29 Dec. 1902; extracts from this address in *Math. Supplement, School Sci.*, v. 1, 1903, (a) "Pure and applied mathematics," p. 25-28; (b) "Elementary mathematics," p. 57-63; (c) "The secondary schools and the laboratory method," p. 101-108.
39. "The subgroups of the generalized finite modular group," *U. Chicago Decennial Pub.*, v. 9, 1903, p. 141-190.
40. "On doubly infinite systems of directly similar convex arches with common base line," *AMS Bull.*, v. 10, 1904, p. 337-341.
41. "On a definition of abstract groups," *AMS Trans.*, v. 6, 1905, p. 179-180.
42. "The cross-section paper as a mathematical instrument," *School Sci. and Math.*, v. 6, 1906, p. 429-450; *School Rev.*, v. 14, 1906, p. 317-338.

43. "Note on Fourier's constants," *AMS Bull.*, v. 13, 1907, p. 232-234.
44. "The decomposition of modular systems connected with the doubly generalized Fermat theorem," *AMS Bull.*, v. 13, 1907, p. 280-288.
45. Problems proposed in *AMM*: Algebra, nos. 284, 285, 286, v. 14, 1907, p. 110; Calculus, no. 421, v. 24, 1917, p. 31; no. 2726, v. 25, 1918, p. 303; 2843, v. 27, 1920, p. 326; 2884, v. 28, 1921, p. 139; problem solved: Algebra, no. 485, v. 18, 1925, p. 78.
46. "On a form of general analysis with application to linear differential and integral equations," *Intern. Congress Mathems.*, Rome, v. 2, 1909, p. 98-114.
47. "Introduction to a form of general analysis," *New Haven Math. Colloq. (AMS Colloq. Pub.)*, v. 2), 1910, p. 1-150.
48. "A generalization of the game called Nim," *AM*, s. 2, v. 11, 1910, p. 93-94.
49. "On the foundations of the theory of linear integral equations," *AMS Bull.*, v. 18, 1912, p. 334-362. Add. VP AAAS and chm. Sect. A 29 Dec. 1911.
50. "A mode of composition of positive quadratic forms," *BA Report*, Dundee, v. 82, 1913, p. 413.
51. "On the fundamental functional operation of a general theory of linear integral equations," *Intern. Congress Mathems.*, Cambridge, v. 1, 1913, p. 230-255.
52. Definition of limit in general integral analysis," *NAS Proc.*, v. 1, 1915, p. 628-632.
53. "On power series in general analysis," *MA*, v. 86, 1922, p. 30-39.
54. "A general theory of limits" (with H. L. Smith), *AJM*, v. 44, 1922, p. 102-121.
55. (a) *Vectors, Matrices and Quaternions*, (b) *Hermitian Matrices of positive Type in General Analysis*, by E. H. Moore, class lectures by R. W. Barnard, Chicago, 1926, mimeographed copy, 449 p.
56. *General Analysis, Part I* (with R. W. Barnard), Philadelphia, 1935, vi+231 p. (*Amer. Phil. So., Mem.*, v. 1); part II is to be pub. in 1938.
- The following are titles of more significant abstracts or unpublished addresses in *AMS Bull*
57. "A two-parameter class of solvable quintics, in which the rational relations amongst the roots, by threes, do not contain the parameters," v. 4, 1898, p. 364.
58. "On the sub-groups of abelian groups," v. 5, 1899, p. 382-383.
59. "On the generational determination of abstract groups," v. 6, 1900, p. 379-380.
60. "On the uniformity of continuity," v. 7, 1901, p. 245.
61. "On double limits," v. 7, 1901, p. 257.
62. "Concerning the second mean-value theory of the integral calculus," v. 8, 1901, p. 19-20.
63. "On Hilbert's plane arguesian geometry," v. 8, 1902, p. 202.
64. "On the theory of systems of integral equations of the second kind," v. 12, 1906, p. 280.
65. "Homogeneous distributive functional operations of degree n ," v. 13, 1907, p. 217-219.
66. "The role of postulational methods in mathematics," v. 16, 1909, p. 41
67. "Multiplicative interrelations of certain classes of sequences of positive terms," v. 18, 1912, p. 444-445.
68. "On nowhere negative kernels," v. 19, 1913, p. 287-288.
69. "On the geometry of linear homogeneous transformations of m variables," v. 19, 1913, p. 457-458.
70. "On a class of continuous functional operations associated with the class of continuous functions on a finite linear interval," v. 20, 1913, p. 70-71.
71. "Report on integral equations in general analysis," v. 21, 1915, p. 430.
72. "On a definition of the concept: limit of a function," v. 22, 1916, p. 439-440.
73. "On properly positive Hermitian matrices," v. 23, 1916, p. 66-67.
74. "On the reciprocal of the general algebraic matrix," v. 26, 1920, p. 394-395.
75. "On the determinant of a Hermitian matrix of quaternionic elements," v. 28, 1922, p. 296.
76. "What is a number system?" v. 29, 1922, p. 91.
77. "Introduction to a theory of generalized Hellinger integrals," v. 32, 1926, p. 224.
- See also:
78. "Concerning a congruence group of order 360 contained in the group of linear fractional substitutions," *AAAS Proc.*, v. 41, 1892, p. 62.

7. THOMAS SCOTT FISKE

CURRICULUM VITAE.—B. New York City 12 May 1865. Early educ. at the Old Trinity Church School, N.Y., and in Pingry School, Elizabeth, N.J., before entering Columbia U. (82–88, except 87; A.B. 85; A.M. 86; Ph.D. 88); assist. in math. 85–88, spending six months of 87 at U. Cambridge, England. Tutor in math. Columbia U. (88–91; instr. 91–94; adjunct prof. 94–97; prof. 97–36; executive officer of the dept. 15–28; prof. emeritus 36–). In charge of math. at Barnard C. (89–95; acting dean 99). Secy. College Entrance Exam. Board (01–36).

HONORS.—FOUNDER AMS 88. Secy. AMS 88–95. Treas. AMS 90–91. Ed.-in-chief AMS *Bull.* Oct. 91–Jan. 99. VP AMS 98–01. Joint ed. AMS *Trans.* 99–05. P AMS 03–04. P Assoc. Teachers Math., Middle States and Md. 05–06. Starred *Amer. Men. Sci.* 06. First chm. Council of Amer. Federation of Teachers of Math. and Nat. Sci. 06–07. Examiner N.Y. State Educ. Dept. 09–11. Chm. AMS Semi-centennial Comm. 28–38.

BIOGRAPHICAL NOTES.—Prof. Fiske is a son of Thomas Scott and Clara (Pittman) Fiske. His father, whose business career was mainly in New York City, was a member of an old New Hampshire family which originated in this country with William Fiske from Suffolk county, England, who settled in Wenham, Mass. in 1637. Prof. Fiske's mother was also of English descent. The first secretary of the College Entrance Exam. Board, organized in 1900, was Prof. N. M. Butler, and when he resigned in 1901 (he became president at Columbia U. in 1902) he was anxious that Prof. Fiske should take over the work and regard this as an appreciable portion of his duties as a professor promoting the cause of education. Prof. Fiske continued this service until his retirement as Executive Secretary and Treasurer on 28 Oct. 1936. Under his guidance the Board grew from a small organization examining in one year 973 candidates prepared at 249 schools for admission to 21 colleges, to the present world organization which in a single year at its maximum examined 23,478 candidates prepared at 1,959 schools seeking admission to 206 colleges. During his long, devoted and very notable service the usefulness of the Board steadily increased.

Elsewhere in this volume an attempt has been made to suggest the enormous debt which the Society owes to its able Founder, whose enthusiastic activities on her behalf during the first fifteen years of her existence, were so unremitting and so wise.

SOURCES.—*Nat. Cycl. Amer. Biog.*, v. 12, 1904. *Universities and their Sons*, v. 2, 1899. *Who's Who in Amer.*, v. 19. *Who's Who in New York*, 1917–18. A. A. Fiske, *The Fiske Family. A History of the Family . . . of William Fiske, senior, of Amherst, N.H.*, 2d ed., Chicago, 1867, p. 157. F. C. Pierce, *Fiske and Fisk Family*, Chicago, 1896, p. 220, 333.

BIBLIOGRAPHY

1. "Notes on modern higher algebra," *MM*, n.s., v. 19, 1889, p. 89–91.
2. "Weierstrass's elliptic integral," *AM*, v. 6, 1891, p. 7–11.
3. "On certain space and surface integrals," *AM*, v. 6, 1891, p. 61–63; 1892, p. 131.
4. Reports of meetings and notes, *NYMS Bull.*, v. 1–3, 1891–94, 44 p.
5. Translation: "Picard's demonstration of the general theorem upon the existence of integrals of ordinary differential equations," *NYMS Bull.*, v. 1, 1891, p. 12–16.
6. "On the doubly infinite products," *NYMS Bull.*, v. 1, 1891, p. 61–66.

7. Trans.: "The teaching of mathematics at Göttingen," *NYMS Bull.*, v. 3, 1893, p. 80-88.
8. Reports of meetings and notes, *AMS Bull.*, v. 1-2, 1894-96, 11 p.
9. "The [first] summer meeting of the American Mathematical Society," *AMS Bull.*, v. 1, 1894, p. 1-6.
10. "The second summer meeting of the American Mathematical Society," *Science*, n.s., v. 2, 1895, p. 394-397; *AMS Bull.*, v. 2, 1895, p. 1-7.
11. "Functions of a complex variable," *Higher Mathematics* ed. by M. Merriman and R. S. Woodward, New York, 1896, chapter VI, p. 226-302; 2d ed. 1898; 3d ed. 1900; reissued as no. 11 of *Mathematical Monographs*, New York, 1907, v+99 p.
12. "The third summer meeting of the American Mathematical Society," *Science*, n.s., v. 4, 1896, p. 441-444.
13. "The straight line as a minimum length," *Science*, n.s., v. 4, 1896, p. 533.
14. "The length of a curved line," *Science*, n.s., v. 4, 1896, p. 724.
15. "The Buffalo colloquium," *AMS Bull.*, v. 3, 1896, p. 49-59.
16. "Reply to Professor Halsted," *Science*, n.s., v. 4, 1896, p. 917-918.
17. "Note on the integration of a uniformly convergent series through an infinite interval," *AMS Bull.*, v. 3, 1897, p. 223-224.
18. "Annual reports of the secretary of the College Entrance Examination Board," *Ed. Rev.*, 1902-10.
19. Editor, *Examination Questions Set by the College Entrance Examination Board*, Boston, 1902-36, 35 v. Also *Quinquennial Volumes of Examinations Set by the College Entrance Examination Board, 1901-1935*, Boston, 1905-35, 7 v.
20. "Mathematical progress in America," *Science*, n.s., v. 21, 1905, p. 209-215; *AMS Bull.*, v. 11, 1905, p. 238-246. *AMS ret. P add. 29 Dec. 1904.*
21. "The theory of limits," Dept. Math., H. S. Teach. Assoc., N. Y. City, *Proc. 1905-1906*, 1906, p. 10-14.
22. "The College Entrance Examination Board," *N.Y. Evening Post*, June 20, 1906, p. 7.
23. "Entrance examinations," *Amer. Med. Assoc., Bull.*, v. 6, 1911, p. 81-84.
24. "Entrance examinations," *Amer. Med. Assoc., Journ.*, v. 56, 1911, p. 1541-1542.
25. Annual reports of the secretary of the College Entrance Exam. Board, 1911-1936, New York, 26 v.
26. "Examinations in mathematics other than those set by the teacher for his own classes," *ICT Math., Amer. Report*, Committee no. VII, 1911, p. 7-9.
27. "The College Entrance Examination Board—an analysis of the examinations of 1911," *Ed. Rev.*, v. 43, 1912, p. 155-167.
28. "Relations between the Association and the Society," *AMM*, v. 23, 1916, p. 296-297.
29. Editor, *Comprehensive Examinations Set by the College Entrance Examination Board, 1916-1924*, Boston, 1916-24, 9 v.
30. "Emory McClintock," *AMS Bull.*, v. 23, 1917, p. 353-357.
31. *Four-place mathematical tables for secondary schools and college entrance examinations* (with W. R. Longley), New York, 1925, 15 p.
32. Editor, *The Work of the College Entrance Examination Board, 1901-1925. Anniversary volume*, New York, 1926, ix+300 p.
33. "Frank Nelson Cole," *AMS Bull.*, v. 33, 1927, p. 773-777.
34. "Abelian functions," *Nat. Encycl.*, v. 1, 1933, p. 9.
35. "Elliptic functions," *Nat. Encycl.*, v. 4, 1933, p. 103.
36. "Functions of real and complex variables," *Nat. Encycl.*, v. 4, 1933, p. 454-455.
37. "The influence of the College Entrance Examination Board on the schools," *School and Society*, v. 37, 1933, p. 814.
38. "College entrance examinations in mathematics," *School and Society*, v. 38, 1933, p. 9.
39. Reviews of books by Chapman in *NYMS Bull.*, 1892; by Fisher, Briot and Bouquet trans. by Boyd, Proctor, Gould, Hall, Nicholson, Bass, and Perry in *AMS Bull.*, 1897-98; by



Thomas B. Fiske

1895

Halphen in *School of Mines Quart.*, 1889; by Cajori in *Ed. Rev.*, 1891; by Edwards, Van Velzer, Shutts, Beman and Smith, and Forsyth in *Science*, 1896-1901.

8. WILLIAM FOGG OSGOOD

CURRICULUM VITAE.—B. Boston, Mass. 10 Mar. 1864. Graduated at the Boston Latin School (82) and at Harvard U. (A.B. 86, *summa cum laude* and second in a class of 286; A.M. 87); Harris and Parker fellow from Harvard at U. Göttingen (87-89) and at U. Erlangen (89-90; Ph.D. 90). Instr. math. Harvard U. (90-93; assist. prof. 93-03; prof. 03-33; emeritus 33-). Prof. math. National U. Peking (34-36).

HONORS.—Colloq. lect. AMS 98. Mem. AAAS 99 (resigned 02). Ed. *AM* 99-02. Contributor to *Encyk. d. Math. Wiss.* 01; "Allgemeine Theorie der analytischen Funktionen" (see Bibl. no. 26). VP AMS 03. Mem. NAS 04. P AMS 05-06. Corresp. mem. Kharkov Math. So. 08. Mem. Amer. Sect. Intern. Comm. Teaching Math. 08-20. Hon. LL.D. Clark U. 09. Mem. comm. eds. *CMP Rend.* 09-17. Hon. mem. Calcutta Math. So. 10. Ed. *AMS Trans.* 10. Colloq. lect. AMS 13. Mem. Amer. Phil. So. 15. Acting dean graduate school of arts and sci. Harvard U. 22 (Feb.-July). Corresp. mem. So. Sci. Göttingen 22. Chm. Comm. of the College Entrance Exam. Board, on college entrance requirements in math. 22-23. For. mem. Leop.-Carol. deutsche Akad. Naturf. in Halle 24.

BIOGRAPHICAL NOTES.—Prof. Osgood is a son of William and Mary Rogers (Gannett) Osgood and a descendant of John Osgood of the county of Hampshire, England, who came to Ipswich, Mass. in 1638. His mother was of English ancestry. His return from Germany was at the time of a great revival in American mathematical study, with emphasis on rigorous discussion of many concepts. During the next dozen years especially were his contributions (including more than a score of publications) of a very notable character. In 1903 when mathematicians chose 80 leaders in research the first three were, in order, E. H. Moore, Hill, Osgood (*Amer. Men Sci.*, 5th ed., p. 1269). Then, and for many years later, his influence was exerted not only through publications but also through his students whose interests he ever whole-heartedly promoted in painstaking fashion. His teaching of the second course in Differential and Integral Calculus was such as soon to quadruple the number in regular attendance. Text-books (Bibl. nos. 36, 59 and part of 64) resulted from experience thus gained; so also his works, analytic geometry (no. 58) and mechanics (no. 74), were developed through experience in the classroom. The following four students were prepared for their doctorate under his direction, 1901-13: C. W. McG. Black, L. D. Ames, E. H. Taylor, and G. R. Clements (under Bouton and Osgood).

Prof. Osgood's first important paper was the one on non-uniform convergence and the integration of series term by term (nos. 8, 11). The result was general and altogether new; and the ideas were akin to those which later led to Borel's definition of measure. Schoenflies reports at length on this paper, in his Bericht (*DMV Jahr.*, v. 8, 1900, p. 225-233). In paper no. 21 the last word was spoken on the conformal map of the interior of a simply connected plane region on a circle; the most general

case of boundary points was discussed later (no. 43). Whether a simple plane Jordan curve can be included in a region of arbitrarily small area, appears not to have been settled before Osgood's example answered the question in the negative (no. 29). The notes in no. 18 were novel and led to extensive and important applications by Hartogs; in practice the theorems have important practical applications. In the calculus of variations the converse theorem, formulated and proved in no. 24, was novel and has been taken seriously by later writers; compare, e.g., Hadamard, *Calcul des Variations*, p. 281 f. Whether the three equations

$$w=f_1(u,v), \quad z=f_2(u,v), \quad t=f_3(u,v)$$

where f_1, f_2, f_3 are analytic at (u_0, v_0) define a locus that can also be represented in the form $F(w, z, t) = 0$, when F is analytic at (w_0, z_0, t_0) was raised, and answered for the first time, in the negative, in no. 48. The question of the dimensionality of a locus represented analytically by several simultaneous analytic equations in the complex domain is one to which the answer is not immediately obvious. The result is needed in the simplified proof of the Riemann-Weierstrass theta theorem and was given in no. 69.

Quite different from such studies is that of the motion of the gyroscope: Let a rigid body have dynamical symmetry about an axis; let one point of the axis be fixed in space; and let the angular velocity of the body about the axis be constant. What couple will be required to make the axis describe a given cone at a given rate? What cone will the axis describe, if the couple is given? A direct answer to these questions is given by a certain pair of equations in no. 61.

When the *Funktionentheorie* (no. 35) was begun, in 1901, there was no comprehensive treatment of the field, in which all the tools of ordinary modern analysis were rigorously used. Such a general treatment necessarily had to overlap parts of a number of excellent treatments of special topics. But it was necessary to organize the material as a whole, and to fill many gaps, some small, some large. Most of these gaps in the literature were not pointed out as such, nor published in special monographs. But it is significant that Weierstrass's second implicit function theorem (v. 21, second ed., p. 131) can be proved in a single page of text, after the general theory of implicit functions has been systematically developed up to a certain natural conclusion, including the systematic development of the idea of the irreducibility of an analytic function *im Kleinen*, independent of any particular choice of coordinate axes. Again, the theorems about functions which behave meromorphically at every point of a complex n -dimensional space, closed by a suitable infinite region, are new. The second part of v. 2 had for its object a simple and rigorous treatment of the algebraic functions and their integrals. Weierstrass had used uniformization *im Kleinen*: $w=f(t)$, $z=\phi(t)$, and Klein and Poincaré had pointed out that the automorphic functions yield a uniformization *im Grossen* (the proofs were first given by Koebe), but a systematic use of



William Fogg Osgood

1896

a class of automorphic functions for treating questions *im Grossen* had not as yet been given. As a result a simplified statement and proof of the theorem of correspondence of Cayley and Noether came out. These threads were finally woven together into a proof of the theta theorem, in which there is a minimum of the formalism of the thetas with p arguments. The work, as a whole, is one of America's greatest contributions to the development of mathematics.

Professor Osgood's favorite recreation is touring in his motor car.

SOURCES.—*Nat. Cycl. Amer. Biog.*, v. 13, 1906. *Who's Who in Amer.*, v. 19. *Amer. Men Sci.*, 5th ed. *CMP Annuario Biografico, 1914*. I. Osgood, *A Genealogy of the Descendants of John, Christopher and William Osgood*, Salem, Mass., 1894, p. 143. *Harvard C. Class of 1886 Reports*, V, 1901; VI, 1907; VII, 1911 with portraits of 1886 and 1911; VIII, 1936. *Universities and their Sons*, v. 2, 1899, portrait. Personal information.

BIBLIOGRAPHY

1. *Zur Theorie der zum algebraischen Gebilde $y^m=R(x)$ gehörigen Abelschen Functionen*, Göttingen, 1890, 61 p. Doctoral diss.
2. "The symbolic notation of Aronhold and Clebsch," *AJM*, v. 14, 1892, p. 251-261.
3. "The system of two simultaneous ternary quadratic forms," *AJM*, v. 14, 1892, p. 262-273.
4. "Zur Differentiation des bestimmten Integrales nach einem Parameter," *MMP*, v. 7, 1896, p. 90-92.
5. "A geometric proof of a fundamental theorem concerning unicursal curves," *AMS Bull.*, v. 2, 1896, p. 168-173.
6. "Some points in the elements of the theory of functions," *AMS Bull.*, v. 2, 1896, p. 296-302.
7. "A geometrical method for the treatment of uniform convergence and certain double limits," *AMS Bull.*, v. 3, 1896, p. 59-86.
8. "Ueber die ungleichmässige Convergenz und die gliedweise Integration der Reihen," *GN*, 1896, p. 288-291.
9. "The international congress of mathematicians at Zürich," *AMS Bull.*, v. 4, 1897, p. 45-47.
10. *Introduction to Infinite Series*, Cambridge, 1897, iv + 71 p.; 2d ed. reprinted with corrections, 1902; 3d ed., reprint, 1910; other reprints in 1920, 1928, and 1936. French trans. by A. Sallin: *Séries Infinies. Exposé théorique et pratique illustré par de nombreux Exemples développés et des Exercices à résoudre empruntés à la Géométrie, la Mécanique, la Physique et l'Astronomie*, Paris, 1935, 88 p. ("Monographies de Mathématiques supérieures pures et appliquées" series, which contains also works of Byerly, Carmichael, G. H. Hardy, W. W. Johnson, Mordell, Running, Woodward). Examples 1 and 2 p. 78 of the trans. are incorrect although they are correct in the 2d and 3d eds., at least, of the original. The author's name is incorrectly given as "W. E. Osgood."
11. "Non-uniform convergence and the integration of series term by term," *AJM*, v. 19, 1897, p. 155-190.
12. "The law of the mean and the limits $0/0$, ∞/∞ ," *AM*, v. 12, 1898, p. 65-78.
13. "Example of a single-valued function with a natural boundary, whose inverse is also single-valued," *AMS Bull.*, v. 4, 1898, p. 417-424.
14. "Note on the generalization of Poincaré and Goursat's proof of a theorem of Weierstrass's," *AMS Bull.*, v. 5, 1898, p. 14-17.
15. "Supplementary note on a single-valued function with a natural boundary, whose inverse is also single-valued," *AMS Bull.*, v. 5, 1898, p. 17-18.
16. "Selected topics in the general theory of functions. Six lectures delivered before the Cambridge Colloquium, August 22-27, 1898," *AMS Bull.*, v. 5, 1898, p. 59-87. Compare no. 47.
17. "Beweis der Existenz einer Lösung der Differentialgleichung $dy/dx=f(x, y)$ ohne Hinzunahme der Cauchy-Lipschitz'schen Bedingung," *MMP*, v. 9, 1898, p. 331-345.

18. "Note über analytische Functionen mehrerer Veränderlichen," *MA*, v. 52, 1899, p. 462-464; Zweite Note, *MA*, v. 53, 1900, p. 461-464.
19. "Ueber einen Satz des Herrn Schönflies aus der Theorie der Functionen zweier reeller Veränderlichen," *GN*, 1900, p. 94-97.
20. "The undergraduate mathematical curriculum," Report of discussion at summer meeting AMS, June 1900, *AMS Bull.*, v. 7, 1900, p. 18-21.
21. "On the existence of the Green's function for the most general simply connected plane region," *AMS Trans.*, v. 1, 1900, p. 310-314; v. 2, 1901, p. 484-485.
22. "Sufficient conditions in the calculus of variations," *AM*, s. 2, v. 2, 1901, p. 105-129; Polish trans., *Wiadomości Matematyczne*, v. 5, 1901, p. 179-210.
23. "Note on the functions defined by an infinite series whose terms are analytic functions of a complex variable; with corresponding theorems for definite integrals," *AM*, s. 2, v. 3, 1901, p. 25-34; Polish trans., *Wiadomości Matematyczne*, v. 6, 1902, p. 325-337.
24. "On the existence of a minimum of the integral $\int_{x_0}^{x_1} F(x, y, y') dx$ when x_0 and x_1 are conjugate points, and the geodesics on an ellipsoid of revolution: a revision of a theorem of Kneser's," *AMS Trans.*, v. 2, 1901, p. 166-182, 486.
25. "On a fundamental property of a minimum in the calculus of variations and the proof of a theorem of Weierstrass's," *AMS Trans.*, v. 2, 1901, p. 273-295; v. 3, 1902, p. 500.
26. "Allgemeine Theorie der analytischen Funktionen: a) einer und b) mehrerer komplexen Crössen," *Encyk. d. Math. Wiss.*, v. II-2, 1901, p. 1-114. French trans.: "Fonctions analytiques, exposé d'après l'article allemand de W. F. Osgood . . . par P. Boutroux . . . et Jean Chazy . . .," *Encycl. d. Sci. Mathém.*, tome 2, v. 2, fasc. 1, 1911, p. 94-96. Only these pages of the introduction were ever published.
27. "Problems in infinite series and definite integrals; with a statement of certain sufficient conditions which are fundamental in the theory of definite integrals," *AM*, s. 2, v. 3, 1902, p. 129-146.
28. Introduction to "The logarithm as a direct function" by J. W. Bradshaw, *AM*, s. 2, v. 4, 1903, p. 51.
29. "A Jordan curve of positive area," *AMS Trans.*, v. 4, 1903, p. 107-112.
30. "The integral as the limit of a sum, and a theorem of Duhamel's," *AM*, s. 2, v. 4, 1903, p. 161-178.
31. "On the transformation of the boundary in the case of conformal mapping," *AMS Bull.*, v. 9, 1903, p. 233-235.
32. "Complex variable, theory of functions of a," *Encycl. Amer.*, New York, v. 4, 1903-05.
33. "On a gap in the ordinary presentation of Weierstrass's theory of functions," *AMS Bull.*, v. 10, 1904, p. 294-301.
34. "The calculus in our colleges and technical schools," *AMS Bull.*, v. 13, 1907, p. 449-467. AMS ret. P add. 27 Apr. 1907.
35. *Lehrbuch der Funktionentheorie*, v. 1, Leipzig, 1907, 642 p.; 2d ed., 1912, XII+766 p.; 3d ed., 1920, "fast unveränderter anastatischer Nachdruck," XII+766, p.; 4th ed., 1923; 5th ed., 1928, 818 p.; v. 2, 1924, VI+242 p.; 2d ed., 1929, VII+307 p.; v. 2, 1932, IX+378 p.
36. *A First Course in the Differential and Integral Calculus*, New York, 1907, xv+423 p.; twice reprinted. Rev. ed. with additions, 1909, xvi+462 p.; 17 times reprinted without changes.
37. "On the differentiation of definite integrals," *AM*, s. 2, v. 9, 1908, p. 119-122.
38. "On Cantor's theorem concerning the coefficients of a convergent trigonometric series, with generalizations," *AMS Trans.*, v. 10, 1909, p. 337-346.
39. [Introductory note to new ed. F. Klein's *Lectures on Mathematics* delivered in 1893], New York, 1911.
40. *Report of the American Commissioners of the International Commission on the Teaching of Mathematics* (with D. E. Smith and J. W. A. Young), ICT Math., *Amer. Report*, Wash., 1912, (U. S. Bureau of Educ., *Bull.*, 1912, no. 14) 84 p. These authors were also the eds. of many other reports of the series.
41. "A condition that a function in a projective space be rational," *AMS Trans.*, v. 13, 1912, p. 159-163.

42. "Existenzbeweis betreffend Funktionen, welche zu einer eigentlich diskontinuierlichen automorphen Gruppe gehören," *CMP Rend.*, v. 35, 1913, p. 103-106.
43. "Conformal transformations on the boundaries of their regions of definition" (with E. H. Taylor), *AMS Trans.*, v. 14, 1913, p. 277-298.
44. "Zum Beweise des Picardschen Satzes: eine Ergänzung," *DMV Jahr.*, v. 22, 1913, p. 35-36.
45. "On the uniformization of algebraic functions," *AM*, s. 2, v. 14, 1913, p. 143-162.
46. "Sur une extension d'un théorème de Weierstrass et sur une restriction d'un autre théorème du même auteur," *CR Paris*, v. 156, 1913, p. 1591-1593.
47. "Topics in the theory of functions of several complex variables" (*AMS Colloq. Pub.*, v. 7), 1914, p. 111-230. Compare no. 16.
48. "On functions of several complex variables," *AMS Trans.*, v. 17, 1916, p. 1-8.
49. "On infinite regions," *AMS Trans.*, v. 17, 1916, p. 333-344.
50. "Note on functions of several complex variables," *AMS Bull.*, v. 22, 1916, p. 443-445.
51. "Factorization of analytic functions of several variables," *AM*, s. 2, v. 19, 1917, p. 77-95.
52. "Singular points of analytic transformations," *AMS Bull.*, v. 23, 1917, p. 404.
53. "Singular points of analytic transformations," *AMS Trans.*, v. 19, 1918, p. 251-274.
54. "Professor Bôcher's scientific start in life," *AMM*, v. 26, 1919, p. 262-263.
55. "The life and services of Maxime Bôcher," *AMS Bull.*, v. 25, 1919, p. 337-350.
56. "On a theorem of oscillation," *AMS Bull.*, v. 25, 1919, p. 216-221.
57. "Suggestions and advice to examiners in mathematics," College Entrance Exam. Board, *Annual Report*, 1920, p. 52-55.
58. *Plane and Solid Analytic Geometry* (with W. C. Graustein), New York, 1921, xvii+614 p. Has been reprinted 10 times.
59. *Elementary Calculus*, New York, 1921, ix+224 p. This book is still in print although it has been largely replaced by *Introduction to Calculus*, New York, 1922, xi+449 p. This is the preceding work with 7 new chapters added; it has been reprinted 9 times. Of the work the author states: "The present work is a revision of the author's *A First Course in the Differential and Integral Calculus* [see Bibl. no. 36]. The plan of treatment is essentially the same, but the presentation is fuller and the lists of exercises have been enlarged by problems of value to the student of good average ability."
60. "Charles Leonard Bouton" (with J. L. Coolidge and G. H. Chase), *AMS Bull.*, v. 28, 1922, p. 123-124.
61. "On the gyroscope," *AMS Trans.*, v. 23, 1922, p. 240-264.
62. Reports of W. F. Osgood, as chairman of a Commission on College Entrance Requirements, to the College Entrance Exam. Board: (a) *Report . . . upon Elementary Algebra, Advanced Algebra, and Plane Trigonometry*, New York, May 1922, 29 p.; *Revised Report*, May 1923, 28 p.; final *Report* (doc. no. 107, May 1923), 28 p. (b) *Report . . . on the Requirements in Geometry*, New York, July and Sept. 1922, 32 p.; final ed. (doc. no. 108), May 1923, 43 p. (c) *Report On the New Type of Examinations in Elementary Algebra prepared at the Request of the C.E.E.B. by the Institute of Educational Research, Teachers College, Columbia U.*, May 1923, 7 p.
63. "On Neumann's existence proof," *AM*, s. 2, v. 25, 1924, p. 238-240.
64. *Advanced Calculus*, New York, 1925, xvi+530 p.
65. "On the normal forms of differential equations," *AMS Trans.*, v. 27, 1925, p. 1-14.
66. "A letter from W. F. Osgood to F. S. Woods," *AMM*, v. 34, 1927, p. 205-206.
67. "Meromorphe Funktionen in einem beliebigen erweiterten Raume," *Leopoldina*, v. 4, 1929, p. 126-128.
68. Ed. of *A Short Table of Integrals* by B. O. Peirce, 3d rev. ed., Boston, 1929, 156 p.
69. "The locus defined by parametric equations," *AM*, s. 2, v. 32, 1931, p. 107-120.
70. "On the singular points in the problem of inversion," *AM*, s. 2, v. 33, 1932, p. 740-746.
71. "The number system after Dedekind," *AMS Bull.*, v. 41, 1935, p. 505-507.
72. *Functions of Real Variables*, Peking, Nat. U. Peking, 1936, xii+399 p. Reprinted with corrections, New York, Stechert, 1938.

73. *Functions of a Complex Variable*, Peking, Nat. U. Peking, 1936, viii+257 p. Reprinted with corrections, New York, Stechert, 1938.

74. *Mechanics*, New York, 1937, xv+495 p.

75. Reviews of books by Forsyth, Appell and Goursat, Gibson, and Goursat in *AMS Bull.*, 1895-1908; by Lamb in *Science*, 1898.

9. HENRY SEELY WHITE

CURRICULUM VITAE.—B. Cazenovia, N.Y. 20 May 1861. Prepared at Cazenovia Seminary (where his father was later teacher) for entrance to Wesleyan U. (A.B. 82; assist. in the astr. obs. 82-83; tutor in math. and registrar 84-87); teacher math. and chemistry in the Centenary Collegiate Institute, Hackettstown, N.J. (83-84); student U. Göttingen (87-90; Ph.D. 91); assist. in math. Clark U. (90-92); assoc. prof. pure math. Northwestern U. (92-94; prof. 94-05); prof. math. Vassar C. (05-36; lect. and prof. emeritus 36-). Visiting prof. Chicago U. 08, and Columbia U. 10, and 11. Assoc. physicist, U.S. Bureau of Standards summers 18, 19.

HONORS.—AMS Colloquium Founder 96. Assoc. ed. *AM* 99-05. VP AMS 01. Colloq. lect. AMS 03. Chm. math. sect. St. Louis Congress of Arts and Sci. 04. Starred *Amer. Men Sci.* 06. Ed. *AMS Trans.*, 07-14. P AMS 07-08. VP AAAS and chm. Sect. A 14. Mem. NAS 15. Hon. LL.D. Northwestern U. 15. AMS nominee mem. Div. Phys. Sci. NRC 18-21. Hon. Sc.D. Wesleyan U. 32.

BIOGRAPHICAL NOTES.—Prof. White was a son of Aaron White, who was a teacher of elementary mathematics and surveying in the Cazenovia Seminary, and Isadore Maria Haight. His first American ancestor, John White, came from Essex county, England, to Cambridge, Mass. in 1632, and subsequently became one of the original settlers of Hartford, Conn. As an editor and member of many important committees and officer of the Society, Prof. White's counsel was ever in the direction of maintenance of the highest ideals and standards. Elsewhere we have given details of his part in the founding (1896) of the AMS Colloquium Lectures. He has been a very regular attendant at meetings and many a mathematician will recall how such men as he, and Professors Morley and Pierpont, were interested in seeking him out as a young member, in making him feel very much at home, and in showing appreciation of his scientific achievements. In 1903 mathematicians rated according to merit the leaders in mathematical research. Nine of the first ten have been presidents of the AMS; Prof. White was eighth in this list. His research has been in the fields of theory of invariants, geometry of curves and surfaces, special types of (3, 3) correspondences, algebraic plane curves and twisted curves of low orders, homeomorphic sets of lines in a plane, relativity in mechanics. In his paper on semi-combinants as concomitants of affiliates (no. 6) there are novel definitions and developments of importance. Von Staudt had formulated the beautiful result that if two tetrahedrons have eight points of a twisted cubic for vertices, their eight faces osculate a second cubic curve. Somewhat resembling and underlying this is the following very elegant theorem of Prof. White (no. 32): If seven points on a twisted cubic be joined, two and two, by twenty-one lines, then any seven planes that



Henry B. White

1908

contain these 21 lines will osculate a second cubic curve. This theorem is more strictly fundamental than von Staudt's in that it concerns only seven points, six of which can be arbitrary (random) points of space; whereas von Staudt's relates to eight, two more than those sufficing for definition of the curve. In this respect the seven-point theorem is analogous to Pascal's on the plane six-point on a conic. But while Pascal's conclusion terminates with a lower figure, a line, this on seven-points concludes on the same higher level, namely a third order class-curve. It is thus doubtful which theorem is more justly to be rated as the analogue of Pascal's. At least von Staudt's can be deduced from White's but perhaps not conversely. Nos. 6 and 32 may claim basic originality to a higher degree than other items in the Bibliography. Compare A. B. Coble's Bibliography "A proof of White's porism" (no. 18), where it is remarked that White's theorem "furnishes perhaps the only important generalization of the Poncelet polygons."

In his treatise on *Plane Curves of the Third Order* (no. 42) the author confines himself almost entirely to the projective properties of non-singular cubics, and his presentation is clear, readable, and rigorous. His selection from a wealth of available material is judicious, and the whole constitutes "a stepping stone to many extensive and beautiful treatises on special themes." In reviewing the book Hilton referred to the "novelty of the elegant but highly condensed, symbolic notation." The aesthetic element, and happy choice of words, is noticeable in many of Prof. White's writings (e.g., no. 46).

He delights in music. Mrs. White was the composer Mary Gleason, and F. G. Gleason, 1848–1903, the composer, musician, and music-critic, was her brother. All friends recognize the aptness of the following characterization of Prof. White: "Wise, kind, the soul of courtesy."

SOURCES.—*Nat. Cycl. Amer. Biog.*, v. 14, 1917. A. C. White, 1632–1892. *Memorials of Roderick White and his wife Lucy Blakeslee of Paris Hill, N. Y.* . . . , Ithaca, N. Y., 1892. This work is supplementary to A. S. Kellogg, *Memorials of Elder John White*, Hartford, Conn., 1860. J. B. White, *Geneal. of Descendants of Thos. Gleason of Watertown, Mass.*, Haverhill, Mass., 1909. *N. E. Geneal. and Hist. So. Reg.*, v. 55, 1901. *Alumni Record of Wesleyan U.*, 5th ed., 1921. Diss. "Lebenslauf" (Bibl. no. 2). *Who's Who in Amer.*, v. 19. *Leaders in Educ.*, 1932. Personal information.

BIBLIOGRAPHY

1. "Ueber zwei covariante Formen aus der Theorie der abel'schen Integrale auf vollständigen singularitätenfreien Schnittcurven zweier Flächen," *MA*, v. 36, 1890, p. 597–601.
2. *Abel'sche Integrale auf singularitätenfreien, einfach überdeckten, vollständigen Schnittcurven eines beliebig ausgedehnten Raumes*, Halle, 1891, 90 p. Reprint with the addition of a special title page and "Lebenslauf" from K. Leop.-Carol. deutsche Akad. Naturf., *Nova Acta*, v. 57, 1891, p. 41–128. Doctoral diss.
3. "On generating systems of ternary and quaternary linear transformations," *AJM*, v. 14, 1892, p. 274–282.
4. "A symbolic demonstration of Hilbert's method for deriving invariants and covariants of given ternary forms," *AJM*, v. 14, 1892, p. 283–290.

5. "Reduction of the resultant of a binary quadric and n -ic by virtue of its semi-combinant property," *AMS Bull.*, v. 1, 1894, p. 11-15.
6. "Semi-combinants as concomitants of affiliates," *AJM*, v. 17, 1895, p. 235-265.
7. "Kronecker's linear relation among minors of a symmetric determinant," *AMS Bull.*, v. 2, 1896, p. 136-138.
8. "Numerically regular reticulations upon surfaces of deficiency higher than 1," *AMS Bull.*, v. 3, 1896, p. 116-121.
9. "The cubic resolvent of a binary quartic derived by invariant definition and process," *AMS Bull.*, v. 3, 1897, p. 250-253.
10. "Collineations in a plane with invariant quadric or cubic curves," *AMS Bull.*, v. 4, 1897, p. 17-23.
11. "Inflexional lines, triplets, and triangles associated with the plane cubic curve," *AMS Bull.*, v. 4, 1898, p. 258-260.
12. "The construction of special regular reticulations on a closed surface," *AMS Bull.*, v. 4, 1898, p. 376-382.
13. "Report on the theory of projective invariants: the chief contributions of a decade," *AMS Bull.*, v. 5, 1899, p. 161-175.
14. "Two elementary geometrical applications of determinants," *AM*, s. 2, v. 1, 1900, p. 103-107.
15. "Conics and cubics connected with a plane cubic by certain covariant relations," *AMS Trans.*, v. 1, 1900, p. 1-8.
16. "Plane cubics and irrational covariant cubics," *AMS Trans.*, v. 1, 1900, p. 170-181, 508.
17. "Note on a twisted curve connected with an involution of pairs of points in a plane," *AM*, s. 2, v. 3, 1902, p. 149-153.
18. "On twisted cubic curves that have a directrix," *AMS Trans.*, v. 4, 1903, p. 134-141.
19. "Twisted quartic curves of the first species and certain covariant quartics," *AM*, s. 2, v. 4, 1903, p. 116-120.
20. "The eleventh summer meeting of the American Mathematical Society" (with M. W. Haskell), *AMS Bull.*, v. 11, 1904, p. 55-68.
21. "Mathematics at the St. Louis congress, September 20, 22, and 24, 1904," *AMS Bull.*, v. 11, 1905, p. 358-363. See also *Congress of Arts and Sciences, Universal Exposition St. Louis, 1904*, ed. by H. J. Rogers, v. 1, 1905, p. 455.
22. "Linear systems of curves on algebraic surfaces," *Lectures on Mathematics* (AMS *Colloq. Pub.*, v. 1), 1905, p. 1-30. Abstract in *AMS Bull.*, v. 10, p. 120-124, 1903.
23. "Rational plane curves related to Riemann transformations," *AMS Bull.*, v. 12, 1906, p. 157-158.
24. "How should the college teach analytic geometry?" *AMS Bull.*, v. 12, 1906, p. 493-498.
25. "Triangles and quadrilaterals inscribed to a cubic and circumscribed to a conic," *AM*, s. 2, v. 7, 1906, p. 172-176.
26. "Two tetrahedron theorems," *AMS Bull.*, v. 14, 1908, p. 220-222.
27. "Bézout's theory of resultants and its influence on geometry," *AMS Bull.*, v. 15, 1909, p. 325-338. *AMS ret.* P add. 30 Dec. 1908.
28. "Note on Lüroth's type of plane quartic curves" (with Kate G. Miller), *AMS Bull.*, v. 15, 1909, p. 347-352.
29. "Triple-systems as transformations, and their paths among triads," *AMS Trans.*, v. 14, 1913, p. 6-13.
30. "The multitude of triad systems on 31 letters," *AMS Trans.*, v. 16, 1915, p. 13-19.
31. "The synthesis of triad systems Δt in t elements, in particular for $t=31$," *NAS Proc.*, v. 1, 1915, p. 4-6.
32. "Seven points on a twisted cubic curve," *NAS Proc.*, v. 1, 1915, p. 464-466.
33. "Forty years' fluctuations in mathematical research," *Science*, n.s., v. 42, 1915, p. 105-113. Add. before the Vassar Faculty Club Feb. 1914.

34. "A variable system of sevens on two twisted cubic curves," *NAS Proc.*, v. 2, 1916, p. 337-338.
35. "Poncelet polygons," *Science*, n.s., v. 43, 1916, p. 149-158. Add. VP AAAS and chm. Sect. A 30 Dec. 1915.
36. "Mathematics in nineteenth century science," *Science*, n.s., v. 43, 1916, p. 583-592.
37. "The complete enumeration of triad systems in 15 elements" (with F. N. Cole and L. D. Cummings), *NAS Proc.*, v. 3, 1917, p. 197-199.
38. "Complete classification of the triad systems on fifteen elements" (with F. N. Cole and L. D. Cummings), *NAS Mem.*, v. 14, 1919, no. 2, p. 5-89 [H.S.W., p. 5-26, 69-72].
39. "A property of two $(n+1)$ -gons inscribed in a norm-curve in n -space," *AMS Trans.*, v. 22, 1921, p. 80-83.
40. "The associated point of seven points in space," *AM*, s. 2, v. 23, 1922, p. 301-306.
41. "Serret's analogue of Desargues's theorem," *AMM*, v. 29, 1922, p. 111-112.
42. *Plane Curves of the Third Order*, Cambridge, Mass., 1925, xii+168 p.
43. "The Amherst colloquium," *AMS Bull.*, v. 35, 1929, p. 16-18.
44. "The plane figure of seven real lines," *AMS Bull.*, v. 38, 1932, p. 59-65.
45. "Construction of a groupless and headless triad system on 31 elements," *AMS Bull.*, v. 40, 1934, p. 829-832.
46. "Professor George D. Birkhoff, president of the American Association for the Advancement of Science," *Scientific Mo.*, v. 44, 1937, p. 191-193+portrait plate.
47. Reviews of books by Andoyer, Beutel, Böger, Brioschi, Coolidge, Cremona, E. B. Elliott, Fricke, Klein, Krazer, Osgood, B. M. Walker, H. Weber in *AMS Bull.*, 1898-1919; by G. T. Fechner in *Astrophys. J.*, 1899; by T. Smith and R. W. Chechire in *Science*, 1919.

10. MAXIME BÔCHER

CURRICULUM VITAE.—B. Boston, Mass. 28 Aug. 1867; d. Cambridge, Mass. 12 Sept. 1918. Graduating at the Cambridge (Mass.) Latin School he entered Harvard U. (83-88; A.B., *summa cum laude*, 88). Student at Harvard, Harris, and Parker fellow U. Göttingen (88-91; Ph.D. 91). Instr. math. Harvard U. (91-94; assist. prof. 94-04; prof. 04-18).

HONORS.—Full prize awarded by faculty U. Göttingen for essay and diss. (Bibl. no. 2) 91. One of first two Colloq. Lects. AMS 96; 6 lects. on "Linear differential equations and their applications", partly printed nos. 19, 24. Assoc. ed. *AM* 96-00; joint ed. 01-07, Sept. 11-June 14. Fellow AAAS 99. Contributor to *Encyk. d. Math. Wiss.* 00; "Randwertaufgaben bei gewöhnlichen Differentialgleichungen" (no. 33). VP AMS 02. Invited speaker Congress Arts and Sci. St. Louis 04; "The fundamental conceptions and methods of mathematics" (no. 48). Starred *Amer. Men Sci.* 06. Ed.-in-chief *AMS Trans.* 08-09, 11-13. Mem. NAS 09. P AMS 09-10. Invited lect. Intern. Congress Mathems., Cambridge, Eng. 12; "Boundary problems in one dimension" (no. 68). Harvard exchange prof. U. Paris 13-14; for lects. see no. 79. Mem. Amer. Phil. So. 16.

BIOGRAPHICAL NOTES.—Prof. Bôcher was a son of Ferdinand and Caroline (Little) Bôcher, and grandson of Ferdinand Jules of Caen, Normandy, France, who came frequently to America on business and died in St. Louis, Mo., but was never settled in this country although his son Ferdinand (1832-1902) happened to be born in New York. This son was for many years Prof. of modern languages at Harvard U., a man of all-round culture, and a great collector of books in the field of French literature, art, and history. Maxime's mother belonged to one of the oldest New England families, tracing her ancestry back to Thomas Little who joined the Plymouth Colony in its early days and in 1633 married Anne

Warren, daughter of Richard Warren, who came in the Mayflower company.

It was to the influence of his parents that the awakening of Bôcher's interest in science was due. He spent five years in the U. and his course was a broad one. Outside of mathematical work, especially under Byerly, B. O. Peirce, J. M. Peirce, and F. N. Cole, he took courses in Latin, chemistry, philosophy, zoology, physical geography and meteorology, Roman and mediaeval art, and music. In his senior year he won a second Bowdoin prize for an essay on "The meteorological labors of Dove, Redfield, and Espy" (no. 1). During six semesters as Harvard fellow at Göttingen he attended lectures by Klein, Schoenflies, Schur, Schwarz and Voigt, and he found of special interest the lectures on Lamé's functions which Klein delivered in 1889-90. This was suggestive in connection with his thesis, on developments of the potential function into series (no. 2), which won a prize from the U. Göttingen and was afterwards elaborated into a book (no. 13) containing important new original work. It was an able treatment calling for extensive knowledge of the theory of potential, of Dupin's cyclides and their generalization by Laguerre, Moutard and Darboux, of the use of elementary divisors, and dealing with important questions in Lamé's polynomials, Lamé's products, and boundary value problems of partial differential equations of physics. Thus at the very beginning Bôcher got into vital touch with the chief branches of mathematics. He was interested in all phases of the theory of ordinary linear differential equations with real independent variable. His surveys of work on boundary problems up to 1912 were well covered in his *Encyk.* article (no. 33) and Congress paper (no. 68) but in this field he wrote many other papers of which the most important appeared in the first two v. of *AMS Trans.* (nos. 31, 39, 42) where he greatly improved on methods of Sturm and attained to a maximum of generality. A survey of Bôcher's boundary problems for differential equations was made by R. G. D. Richardson (*AMS Bull.*, v. 26, p. 108-124) in his review of Bôcher's lectures at the Sorbonne (no. 79). In this v. is given the first complete discussion of the convergence of the series used in the method of successive approximations. In the field of fundamental existence theorems for linear differential equations (nos. 24, 26, 42, 43) he introduced new results, and the extended Green's functions in no. 35 turned out to be of great importance (see also no. 62). In his expository article on Fourier series (no. 53) he called attention to the remarkable phenomena exhibited by a Fourier's series near a point of discontinuity, previously noted by Gibbs, and called "Gibbs' phenomena" by Bôcher who gave the first adequate treatment. His contributions to the theory of the harmonic function in two dimensions are elegant and distinctly important (nos. 14, 25, 45, 54, 58). All of Bôcher's papers excel in simplicity and elegance and nearly all of them treat subjects of great importance to marked advantage. He never occupied himself



Maxime Böcher

1896

with an unimportant problem. How extensive and how useful his work was in one field, will be suggested by looking up the references under Bôcher's name in the index to Osgood's *Funktionentheorie*, v. 1. See also the references to Bôcher in indices of *Encyk. d. Math. Wiss.*, v. II.3.2 and III.2.2. In 1903 when the leading 80 mathematicians were listed the first four were Moore, Hill, Osgood, and Bôcher.

Bôcher's *Introduction to Higher Algebra* (no. 56), translated into German and Russian, was a remarkable pioneer work in English, which was long of great service to students (see reviews by A. Ranum, *AMS Bull.*, v.16; J. Tannery, *DB*, s. 2, v. 32). Yet another exceptional service was rendered by his *Introduction to the Study of Integral Equations* (no. 59; reviewed by G. A. Bliss, *AMS Bull.*, v. 16), the emphasis placed on the historical development of the subject being an interesting feature of the tract. Special attention should be drawn also to his little known pamphlet on regular points of linear differential equations of the second order (no. 19) used for a number of years in connection with one of his courses of lectures. Because of the clarity and care with which his elementary texts on analytic geometry and trigonometry were written they are still in demand (nos. 44, 75, 76).

Osgood has well written that "the standards of clearness, both in thought and expression, which characterize French men of letters and science, Bôcher made his own, not by a conscious effort but through an inner driving force which made it a part of his very nature to find suitable expression for his ideas." His lectures were so lucid, the difficulties of subjects were not perhaps as effectively assimilated by students as they would have been under a poorer teacher. He was by nature very reserved and he never gave way to enthusiasm. He was a puritan, and with the virtues he had also the faults of the puritan. There was no place in his world for human weakness; he respected only results. These same stern standards he applied equally to himself. For guiding students working on doctoral dissertations he was remarkably well equipped; the following 17 men did their theses under him, 1895–1919: J. W. Glover, M. B. Porter, F. H. Safford, D. F. Campbell, O. Dunkel, D. R. Curtiss, W. B. Ford, W. H. Roever, W. C. Brenke, F. Irwin, C. N. Moore, G. C. Evans, T. Fort, L. R. Ford, M. T. Hu, L. Brand, C. N. Reynolds (under Bôcher and Birkhoff).

Elsewhere in this v. we have told of Bôcher's connection with the founding of the *Transactions*, of which he was for five years a remarkably effective editor-in-chief. He was a fine critic, ever free with constructive suggestions. For many years he served as an assoc. ed. of *AM*. He was never very strong, and long he had to combat ill health. Finally he was cut off, almost in his prime.

Birkhoff has summed up: "In amount and quality his production exceeds that of any American mathematician of earlier date in the field of

pure mathematics. Because of this fact and the weight he has added to our mathematical traditions in other ways, Maxime Bôcher will ever remain a memorable personality in American mathematics."

SOURCES.—G. D. Birkhoff, "The scientific work of Maxime Bôcher," and W. F. Osgood, "The life and services of Maxime Bôcher," *AMS Bull.*, v. 25. Harvard, *Class of 1888 Report*, v. 6, 1909, v. 7, 1913 (with portraits in 1888 and 1913), and v. 8, 1920, with biog. notes by A. G. Webster. D. E. Smith, *DAB*, v. 2, 1929. W. F. Osgood, "Professor Bôcher's scientific start in life," *AMM*, v. 26, p. 262–263. *Who's Who in Amer.*, v. 10. *Nat. Cycl. Amer. Biog.*, v. 18, 1922. *Science*, n.s. v. 48, 1918, p. 534; minute, faculty Harvard U. Doctoral diss. "Lebenslauf" (no. 2).

BIBLIOGRAPHY

1. "The meteorological labors of Dove, Redfield and Espy," *Amer. Meteorological Journ.*, v. 5, 1888, p. 1–13.
2. *Ueber die Reihenentwickelungen der Potentialtheorie* (gekürzte Preisschrift), Göttingen, 1891, iv+66 p.+ "Lebenslauf." Doctoral diss. Elaborated in no. 13.
3. "On Bessel's functions of the second kind," *AM*, v. 6, 1892, p. 85–90.
4. "Geometry not mathematics" (letter to the ed.), *Nation*, v. 54, 1892, p. 131.
5. "On a nine-point conic," *AM*, v. 6, 1892, p. 132, 178.
6. "On some applications of Bessel's functions with pure imaginary index," *AM*, v. 6, 1892, p. 137–160.
7. "Collineation as a mode of motion," *NYMS Bull.*, v. 1, 1892, p. 225–231.
8. "A bit of mathematical history," *NYMS Bull.*, v. 2, 1893, p. 107–109.
9. "On the differential equation $\Delta u + k^2 u = 0$," *AJM*, v. 15, 1893, p. 78–83.
10. "Einige Sätze über projective Spiegelung," *MA*, v. 43, 1893, p. 598–600.
11. "Some propositions concerning the geometric representation of imaginaries," *AM*, v. 7, 1893, p. 70–72.
12. "Historical summary," W. E. Byerly, *An Elementary Treatise on Fourier's Series and Spherical, Cylindrical, and Ellipsoidal Harmonics*, . . . , Boston, 1893, Chap. IX, p. 267–275.
13. *Ueber die Reihenentwickelungen der Potentialtheorie*, mit einem Vorwort von F. Klein, Leipzig, 1894, viii+258 p. Elaboration of no. 2.
14. "Gauss's third proof of the fundamental theorem of algebra," *AMS Bull.*, v. 1, 1895, p. 205–209.
15. "Simplification of Gauss's third proof that every algebraic equation has a root," *AJM*, v. 17, 1895, p. 266–268.
16. "General equation of the second degree" (set of formulas on a card), Harvard U. Press, 1895.
17. "On Cauchy's theorem concerning complex integrals," *AMS Bull.*, v. 2, 1896, p. 146–149.
18. "Linear differential equations and their applications," (report by T. S. Fiske of a lect. at Buffalo Colloq.), *AMS Bull.*, v. 3, 1896, p. 52–55.
19. *Regular Points of Linear Differential Equations of the Second Order*, Cambridge, 1896, 23 p. Part of AMS Colloq. lects.; see also no. 24.
20. "On certain methods of Sturm and their application to the roots of Bessel's functions," *AMS Bull.*, v. 3, 1897, p. 205–213.
21. Introduction to "Examples of the construction of Riemann's surfaces for the inverse of rational functions, by the method of conformal representation," by C. L. Bouton, *AM*, v. 12, 1898, p. 1–2.
22. "The roots of polynomials which satisfy certain linear differential equations of the second order," *AMS Bull.*, v. 4, 1898, p. 256–258.
23. "The theorems of oscillation of Sturm and Klein," *AMS Bull.*, v. 4, 1898, p. 295–313; 365–376; v. 5, 1898, p. 22–43.
24. "Notes on some points in the theory of linear differential equations," *AM* v. 12, 1898, p. 45–53. Part of AMS Colloq. lects.; see no. 19.

25. "Note on Poisson's integral," *AMS Bull.*, v. 4, 1898, p. 424-426.
26. "On singular points of linear differential equations with real coefficients," *AMS Bull.*, v. 5, 1899, p. 275-281.
27. "An elementary proof that Bessel's functions of the zeroth order have an infinite number of real roots," *AMS Bull.*, v. 5, 1899, p. 385-388.
28. "Examples in the theory of functions," *AM*, s. 2, v. 1, 1899, p. 37-40.
29. "On regular singular points of linear differential equations of the second order whose coefficients are not necessarily analytic," *AMS Trans.*, v. 1, 1900, p. 40-52, 507.
30. "Some theorems concerning linear differential equations of the second order," *AMS Bull.*, v. 6, 1900, p. 279-280.
31. "Application of a method of D'Alembert to the proof of Sturm's theorems of comparison," *AMS Trans.*, v. 1, 1900, p. 414-420.
32. "On linear dependence of functions of one variable," *AMS Bull.*, v. 7, 1900, p. 120-121, 234.
33. "Randwertaufgaben bei gewöhnlichen Differentialgleichungen," *Encyk. d. Math. Wiss.*, v. 2-1, 1900, p. 437-463.
34. "The theory of linear dependence," *AM*, s. 2, v. 2, 1901, p. 81-96.
35. "Green's functions in space of one dimension," *AMS Bull.*, v. 7, 1901, p. 297-299.
36. "Certain cases in which the vanishing of the Wronskian is a sufficient condition for linear dependence," *AMS Trans.*, v. 2, 1901, p. 139-149.
37. "An elementary proof of a theorem by Sturm," *AMS Trans.*, v. 2, 1901, p. 150-151.
38. "Non-oscillatory linear differential equations of the second order," *AMS Bull.*, v. 7, 1901, p. 333-340.
39. "On certain pairs of transcendental functions whose roots separate each other," *AMS Trans.*, v. 2, 1901, p. 428-436; supplementary note, v. 18, 1917, p. 519-521.
40. "On Wronskians of functions of a real variable," *AMS Bull.*, v. 8, 1901, p. 53-63.
41. "Some applications of the method of abridged notation," *AM*, s. 2, v. 3, 1902, p. 45-51.
42. "On the real solutions of systems of two homogeneous linear differential equations of the first order," *AMS Trans.*, v. 3, 1902, p. 196-215.
43. "On systems of linear differential equations of the first order," *AJM*, v. 24, 1902, p. 311-318.
44. Rev. and enl. *The Elements of Plane Analytic Geometry* by George R. Briggs, New York, 1903, iv+191 p.
45. "Singular points of functions which satisfy partial differential equations of the elliptic type," *AMS Bull.*, v. 9, 1903, p. 455-465.
46. "On the uniformity of the convergence of certain absolutely convergent series," *AM*, s. 2, v. 4, 1903, p. 159-160.
47. Contribution to "Sprechsaal für die *Encyk. d. Math. Wiss.*," *Archiv d. Math. u. Phys.*, v. 7, 1904, p. 269.
48. "The fundamental conceptions and methods of mathematics," *AMS Bull.*, v. 11, 1904, p. 115-135; also in *Congress of Arts and Science, Universal Exposition, St. Louis, 1904*, ed. by H. J. Rogers, Boston, v. 1, 1905, p. 456-473. Add. delivered 20 Sept.
49. "A problem in statics and its relation to certain algebraic invariants," *AAcAS Proc.*, v. 40, 1904, p. 469-484.
50. "Linear differential equations with discontinuous coefficients," *AM*, s. 2, v. 6, 1905, p. 97-111.
51. "Sur les équations différentielles linéaires du second ordre à solution périodique," *CR Paris*, v. 140, 1905, p. 928-931.
52. "A problem in analytic geometry with a moral," *AM*, s. 2, v. 7, 1905, p. 44-48.
53. "Introduction to the theory of Fourier series," *AM*, s. 2, v. 7, 1906, p. 81-152.
54. "On harmonic functions in two dimensions," *AAcAS Proc.*, v. 41, 1906, p. 577-583.
55. "Another proof of the theorem concerning artificial singularities," *AM*, s. 2, v. 7, 1906, p. 163-164.

56. *Introduction to Higher Algebra* (prepared for publication with the coöperation of E. P. R. Duval), New York, 1907, xi+321 p.; reprinted 14 times, last in 1937.
 German trans.: *Einführung in die höhere Algebra*, by Hans Beck mit einem Geleitwort von E. Study, Leipzig and Berlin, 1910, xii+348 p.; 2d ed., 1925.
 Russian trans. from the German: *Vvedenie v Vysshūū Algebra*, ed. by A. G. Kurosh, preface by P. S. Alexandrov, Moscow and Leningrad, 1933, 291 p.
57. "On the small forced vibrations of systems with one degree of freedom," *AM*, s. 2, v. 10, 1908, p. 1-8.
58. "On the regions of convergence of power-series which represent two-dimensional harmonic functions," *AMS Trans.*, v. 10, 1909, p. 271-278.
59. *An Introduction to the Study of Integral Equations* (Cambridge Tracts Math. and Math. Physics, no. 10), Cambridge, England, 1909, vii+72 p.; 2d ed., 1914; repr. 1926.
60. "On semi-analytic functions of two variables," *AM*, s. 2, v. 12, 1910, p. 18-26.
61. "The published and unpublished work of Charles Sturm on algebraic and differential equations," *AMS Bull.*, v. 18, 1911, p. 1-18. AMS ret. P add. 28 Apr. 1911.
62. "Boundary problems and Green's functions for linear differential and difference equations," *AM*, s. 2, v. 13, 1911, p. 71-88.
63. "Graduate work in mathematics in universities and in other institutions of like grade in the United States. General report," U. S. Bureau of Educ., *Bull.*, no. 6, 1911, p. 7-20; *AMS Bull.*, v. 18, 1911, p. 122-137.
64. "On linear equations with an infinite number of variables" (with L. Brand), *AM*, s. 2, v. 13, 1912, p. 167-186.
65. "A simple proof of a fundamental theorem in the theory of integral equations," *AM*, s. 2, v. 14, 1912, p. 84-85.
66. "Applications and generalizations of the conception of adjoint systems," *AMS Trans.*, v. 14, 1913, p. 403-420.
67. "Doctorates conferred by American universities" (letter to the ed.), *Science*, n.s., v. 38, 1913, p. 546.
68. "Boundary problems in one dimension," *Intern. Congress Mathems.*, Cambridge, v. 1, 1913, p. 163-195.
69. "The infinite regions of various geometries," *AMS Bull.*, v. 20, 1914, p. 185-200 (see v. 22, 1915, p. 40).
70. "On Gibbs' phenomenon," *Crelle's J.*, v. 144, 1914, p. 41-47.
71. "Mathématiques et mathématiciens français," *Rev. Intern. de l'Enseignement*, v. 67, 1914, p. 20-31.
72. "Charles Sturm et les mathématiques modernes," *Revue du Mois*, v. 17, 1914, p. 88-104.
73. "On a small variation which renders a linear differential system incompatible," *AMS Bull.*, v. 21, 1914, p. 1-6.
74. "The smallest characteristic numbers in a certain exceptional case," *AMS Bull.*, v. 21, 1914, p. 6-9.
75. *Trigonometry with the Theory and Use of Logarithms* (with H. D. Gaylord), New York, 1915, ix+142 p.
76. *Plane Analytic Geometry with Introductory Chapters on the Differential Calculus*, New York, 1915, xiii+235 p.
77. "On the Wronskian test for linear dependence," *AM*, s. 2, v. 17, 1916, p. 167-168.
78. *Syllabus of a Brief Course in Solid Analytic Geometry*, Lancaster, 1916, 10 p.
79. *Leçons sur les Méthodes de Sturm dans la Théorie des Équations Différentielles Linéaires et leurs Développements Modernes, professées à la Sorbonne en 1913-1914.* (Recueillies et rédigées par G. Julia), (*Collection de Monographies sur la Théorie des Fonctions*, ed. Borel), Paris, 1917, vi+118 p.
80. "Concerning direction cosines and Hesse's normal form," *AMM*, v. 25, 1918, p. 308-310.
81. Reviews of books by Hayward, Bessell, Heffter, Schlesinger, Bailey and Woods, Nienglowski, Burkhardt, Picard, Gauss, Whittaker, Bromwich, Runge, d'Adhémar, Kowalewski, and Gibb in *AMS Bull.*, 1895-1916; by Pockels in *AM*, 1892; by Picard in *Science*, 1906.

11. HENRY BURCHARD FINE

CURRICULUM VITAE.—B. Chambersburg, Pa. 14 Sept. 1858; d. Princeton, N.J. 22 Dec. 1928. Student at C. of New Jersey later Princeton U. (76–84; A.B. 80; fellow in experimental sci. 80–81; tutor in math. 81–84; A.M. 83; assist. prof. 85–89; prof. 89–28; dean faculty 03–12; dean dept. sci. 11–28). Student at U. Leipzig (84–85; Ph.D. May 85); at U. Berlin (summer 85). Acting director Princeton U. Obs. 08–12.

HONORS.—VP AMS 92–93. Mem. Amer. Phil. So. 97. Starred *Amer. Men Sci.* 06. Hon. LL.D. Williams C. 09. Practically acting P Princeton U. under the nominal presidency of the senior member of the Board of Trustees from the time of Wilson's resignation in 10 to the appointment of President Hibben in 12. P AMS 11–12. By President Wilson offered appointment as U. S. Ambassador to Germany 13; Wilson also offered him a place on the Federal Reserve Board and recommended him as P JHU (see R. S. Baker, in "Sources" below); he was repeatedly invited to be P Mass. Inst. Tech. P Assoc. Math. Teachers of New Jersey 15–16. Henry Burchard Fine Research Professorship in Math. established by an endowment of \$200,000 from T. D. Jones 25; Prof. Veblen was the first incumbent, and on resigning from the U. in 33 he was succeeded by Prof. Lefschetz. Dedication in 31 of Henry Burchard Fine Memorial Hall for math., given to Princeton U., furnished and endowed by T. D. Jones and his niece Miss Gwethalyn Jones, including a portrait of Dean Fine by E. L. Ibsen.

BIOGRAPHICAL NOTES.—Dean Fine was a son of Lambert Suydam and Mary Ely (Burchard) Fine, and a great-great-grandson of Hendrick and Elizabeth (Lefferts) Fine who came to this country from Holland. His father (d. 1869) was a Presbyterian minister, and his mother in 1875 finally settled in Princeton, where by private study her son finished his preparation for the College, where he led his class each year. He specialized in classics which he later on expected to teach; he also began the study of Sanskrit and he was one of the small group who discussed philosophy with Dr. McCosh and enjoyed the impulse of his invigorating mind. His adoption of mathematics as a career was largely due to George Bruce Halsted (1853–1922), that extraordinary enthusiast for non-euclidean geometry. Halsted had graduated in Princeton in 1875 and after studying under Sylvester at The JHU spent the years 1878–81 in Princeton as "instructor in post-graduate mathematics." On graduation Fine was appointed a fellow in experimental science, did a certain amount of experimental work and even published a paper (Bibl. no. 1) in collaboration with W. F. Magie, subsequently professor of physics at Princeton and Fine's biographer (see "Sources"). But Fine was never really interested in experimental work and gladly changed to service as tutor in mathematics during the next three years. In March 1884 he and Magie sailed for Germany, and he went to Leipzig where he attended lectures and seminars of Klein, C. G. A. Mayer, C. G. Neumann (physics), F. H. Schur, and Wilhelm Wundt (philosophy). In a little more than a year he obtained his doctorate with a thesis (no. 4) on a topic approved by Klein but suggested by Study, later one of Fine's closest friends. Fine spent the following summer in Berlin, where he listened to Kronecker's lectures on the theory of elimination and was profoundly influenced by them (see nos. 15, 22); he had another period of study with Kronecker in the summer of 1891.

After taking up his life work at Princeton, Fine published a few re-

search papers (nos. 4-diss., 6, 10, 12), and another of some importance (no. 23) as late as 1916. But his time was mainly devoted to teaching, administration, and the logical exposition of elementary mathematics. His *Number System of Algebra treated Theoretically and Historically* (no. 14) which is devoted to an exposition of the logical foundations of analysis is still a very useful reference book on this subject, and has recently been reprinted. There followed three text-books for undergraduates, *A College Algebra*, 1905 (no. 17), *Coordinate Geometry*, 1909 (no. 21, with H. D. Thompson), and *Calculus*, 1927 (no. 27). In point of view of accuracy of statement and adequacy with which they present the subject the first and last are unexcelled. This was partly due to the fact that they had been printed or mimeographed in a preliminary form and used with classes for many years, and modified before publication as the result of such experience.

Fine became a member of the AMS in 1891 and was VP for the next two years; then at three different periods he served as member of the Council for eight years before he became P in 1911. During almost the whole period of his presidency of the Society he was also in reality acting President of Princeton U. As dean of the faculty during President Wilson's administration he contributed largely to the raising of academic standards. In the controversies which raged during this period on various questions of academic policy, he supported the President. These two men had been members of the editorial board of the *Princetonian* in their student days and from that time dated a life-long friendship based upon the respect which each had for the qualities of intellect and character of the other. When the preceptorial system of instruction was introduced at Princeton in 1905 Fine seized the opportunity of laying the foundations of a department of mathematics of first rank and this standing has been maintained ever since. But he had an important part in the choice of men in the other fields of science. In 1911 he became in letter what he was in fact—the dean of the departments of science. When it was decided in 1925 to organize a campaign for funds for the further development of research in the sciences, his was the guiding hand and he was chairman of the committee for this purpose. Largely because of the confidence which he inspired, the General Education Board offered Princeton U. a million dollars for research in pure science on condition that the U. raise two additional millions for the same purpose. The fund was completed in 1928, chiefly by the contributions of Mr. T. D. Jones, a life-long friend of Fine.

In early days Fine played the flute in the college orchestra and he was later active in bringing good concerts to Princeton. His knowledge of music was extensive, and during the year of his death he was commissioned to engage an organist and choirmaster for the new university chapel. He took keen interest in games and in the daily life of the undergraduates. For nearly the whole of his professional career he served on the



W. B. Frie

1911

university committee of athletics. Death was the result of an accident. In the uncertain evening light he was riding his bicycle on a road in the outskirts of Princeton and was struck from behind by an automobile, the driver of which failed to see that he was starting to make a left turn. He died early the next morning without having recovered consciousness.

Fine Hall today, the headquarters also of the School of Mathematics in the Institute for Advanced Study, is the greatest center of mathematical activity in this country, a magnificent memorial to one who was an exemplar of the highest type of scholar and teacher, and to a man, singularly genial and winning in personal intercourse, of serene strength, poise, and wisdom.

SOURCES.—W. F. Magie, (a) *DAB*, v. 6, 1931; (b) *Science*, n.s., v. 69, 1929. O. Veblen, (a) *AMS Bull.*, v. 35, 1929; (b) *Princeton Alumni Weekly*, 30 Oct. 1931. L. P. Eisenhart, "Henry Burchard Fine Memorial Hall," *Scientific Mo.*, v. 33, 1931; picture of Hall and portrait of Fine. R. S. Baker, *Woodrow Wilson Life and Letters*, v. 2-4, 1927-32. H. B. Fine, "Autobiographical sketch" in doctoral diss. (Bibl. no. 4). *Pr. Al. Wkly.*, 11 Jan. 1929, portrait, communications by J. G. Hibben, R. S. Baker, and others. G. D. Birkhoff, *Pr. Al. Wkly.*, 6 May 1927. *Who's Who in Amer.*, v. 15, 1928. *Nat. Cycl. Amer. Biog.*, v. 14, 1917.

BIBLIOGRAPHY

1. "On the shadows obtained during the glow discharge" (with W. F. Magie), *AJS*, v. 21, 1881, p. 394-395.
2. *Elements of Spherical Geometry, prepared for the Use of the Freshman Class, Princeton College*, Princeton, 1883, 30 p.
3. "A new demonstration of Cayley's theorem on the intersections of curves," *AAAS Proc.*, 1886, p. 73-74.
4. "On the singularities of curves of double curvature," *AJM*, v. 8, 1886, p. 156-177. Doctoral diss.
5. "The geometric meaning of singular solutions of differential equations of the second and higher orders," *AAAS Proc.*, 1887, p. 64.
6. "A theorem respecting the singularities of curves of multiple curvature," *AJM*, v. 9, 1887, p. 180-184; an extension to n dimensions of the results of no. 4.
7. *On the Forms of Number Arising in Common Algebra*, Boston, 1888, 45 p.
8. "Note on construction of elementary geometry," *Princeton U. Bull.*, v. 1, 1889, p. 52-53.
9. "Local examinations for entrance to college," *Princeton U. Bull.*, v. 2, 1889, p. 25-27.
10. "On the functions defined by differential equations, with an extension of the Puiseux polygon construction to these equations," *AJM*, v. 11, 1889, p. 317-328; abstract in *Princeton U. Bull.*, v. 1, 1889, p. 85-86.
11. "Descartes' Géométrie," *Princeton U. Bull.*, v. 3, 1890, p. 14-16.
12. "Singular solutions of ordinary differential equations," *AJM*, v. 12, 1890, p. 295-322.
13. *Euclid's Elements, Books I, II, and V* (with H. D. Thompson), Princeton, 1891, 82 p.
14. *The Number System of Algebra Treated Theoretically and Historically*, Boston and New York, Leach, Shewell and Sanborn, 1891, ix+131 p.; 2d ed., Boston, Heath, 1903, ix+132 p.; facsimile reprint of 1st ed., New York, Stechert, 1937, ix+131 p.
15. "Kronecker and his arithmetical theory of the algebraic equation," *NYMS Bull.*, v. 1, 1892, p. 173-184; abstract in *Princeton U. Bull.*, v. 4, 1892, p. 56-58.
16. "Elementary proof of a theorem of Fourier and Budan," *Princeton U. Bull.*, v. 13, 1901, p. 52-53.
17. *A College Algebra*, Boston, 1905, viii+595 p.

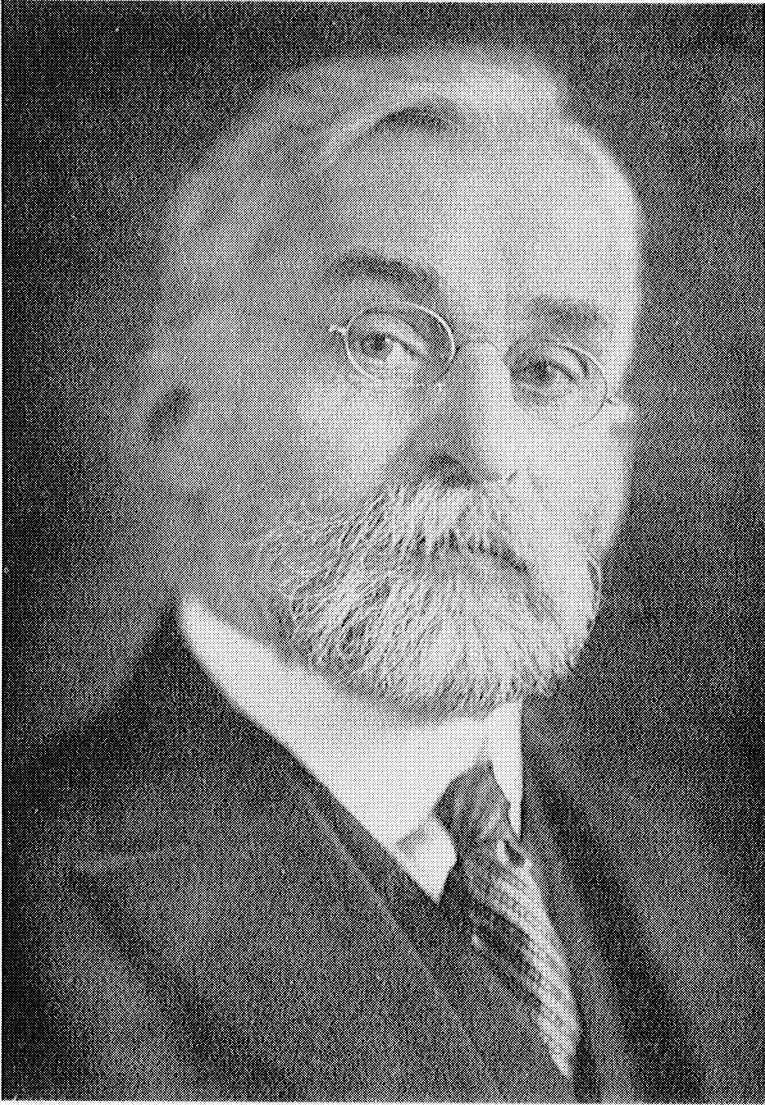
18. "Report on academic failures, February, 1906," *Princeton Alumni Weekly*, v. 6, 1906, p. 433.
19. "Address at the opening of college, September, 1906," *Princeton Alumni Weekly*, v. 7, 1906, p. 8-9.
20. "Liberal education and school and college life; address at the seventy-fifth anniversary of Peekskill Military Academy," published in a souvenir pamphlet by the Academy, 1908, p. 10-16.
21. *Coordinate Geometry* (with H. D. Thompson), New York, 1909, viii+300 p.+8 plates. Reprinted 1914.
22. "An unpublished theorem of Kronecker respecting numerical equations," *AMS Bull.*, v. 20, 1914, p. 339-358. AMS ret. P add. 30 Dec. 1913.
23. "On Newton's method of approximation," *NAS Proc.*, v. 2, 1916, p. 546-552.
24. "Ratio, proportion and measurement in the elements of Euclid," *AM*, s. 2, v. 19, 1917, p. 70-76.
25. "Note on a substitute for Duhamel's theorem," *AM*, s. 2, v. 19, 1918, p. 172-173. With special reference to Bliss (Bibl. no. 24).
26. *Differential and Integral Calculus*, Princeton, N.J., 1920, 192 p. Stenciled autographed notes; see President's *Annual report*, July 1, 1920. This edition was followed by one issued by the New Era Pub. Co., Lancaster, Pa., 1920.
27. *Calculus*, New York, 1927, viii+421 p.; preliminary ed., New York, 1926, 220 p.
28. Reviews of a book by D. A. Murray and of *Mathematical Papers Read at the International Mathematical Congress . . . Chicago* in *AMS Bull.*, 1896-1898.

12. EDWARD BURR VAN VLECK

CURRICULUM VITAE.—B. Middletown, Conn. 7 June 1863. Prepared at high school of Middletown, Conn., and Wilbraham Acad. to enter Wesleyan U. (80-84; A.B. 84; assist. in phys. lab. 84-85; A.M. 87; tutor math. 87-90; assoc. prof. 95-98; prof. 98-06). Graduate student JHU (85-87); at U. Göttingen (90-93; Ph.D. 93). Instr. U. Wisconsin (93-95; prof. 06-29; prof. emeritus 29-). Lect. in math. at Harvard U. second sem. 19-20.

HONORS.—AMS delegate Abel centenary celebration Oslo 02. Colloq. lect. AMS 03. Ed. *AMS Trans.* 05-10. Starred *Amer. Men Sci.* 06. Chm. Chicago Sect. AMS 07. VP AMS 09. Hon. LL.D. Clark U. 09; Osgood and E. H. Moore became doctors at the same time, in connection with the celebration of the 20th anniversary of the founding of Clark. Mem. NAS 11. VP AAAS and chm. Sect. A 12. P AMS 13-14. Hon. D. math. and phys. U. Groningen 14; on 300th anniversary of its founding. Hon. Sc.D. U. Chicago 16; on the quarter-centennial celebration of the founding of the U. Secy. local military Draft Board 17-18. Decorated by the French Govt. "Officier de l'instruction publique," in recognition of his services as teacher and investigator and for his work during the war 20. AMS nominee mem. Div. Phys. Sci. NRC 21-Dec. 23. Hon. LL.D. Wesleyan U. 25.

BIOGRAPHICAL NOTES.—Prof. Van Vleck is a son of the late John Monroe and Ellen Maria (Burr) Van Vleck, and a descendant of Tielman Van Vleeck of Amsterdam and Bremen who migrated to New Amsterdam in 1658, and was the founder of the first organized govt. at Bergen, afterwards a part of Jersey City. His father (1833-1912) taught mathematics and astronomy at Wesleyan U. for over fifty years, and during three different periods he was acting president of the U.; he was a vice-president of the AMS (1904), and the fine Van Vleck Observatory at Wesleyan U., erected in his memory by his brother, was dedicated in 1916 (see *Pop. Astr.*,



Edward B. Van Vleet

1912

v. 24, p. 407–418; and Bibl. no. 25 below). Two years of graduate study (the second as fellow in physics) at JHU, in the fields of mathematics, physics, and astronomy, under Craig, Newcomb, Rowland, and Story, led E. B. Van Vleck to the choice of the pursuit of mathematics rather than physics as a profession. As a result of five semesters at the U. Göttingen, under Burkhardt, Fricke, Schur, Schwarz, Voigt, Weber, and that “marvelous teacher Felix Klein,” his scientific knowledge was notably enriched. There were three events which had a marked influence on Van Vleck’s educational development. The first was a fourteen months’ trip in Europe in 1877–78 which roused a cultural interest in history, literature, but especially art. The second was the year at Wilbraham Academy where the exceptionally fine teaching in Greek, Latin, and mathematics stirred his enthusiasm and interest. The third was the period of his study under Klein. Thus broad and solid foundations were laid for later scientific and academic activities. Practically all of his publications have been in the fields of theory of functions and differential equations. Among the 80 leading mathematicians of the U. S. in 1903, Prof. Van Vleck was listed as no. 11.

At the fourth colloquium of the Society in 1903, he and two other students of his father (H. S. White and F. S. Woods) were the three lecturers, and their lectures form the first v. in this series. Prof. Van Vleck gave six lectures on topics of divergent series and continued fractions (no. 14) and thus rendered a notable service to young mathematicians, not only in setting forth the substantial foundation for a theory of the subjects, which had been laid by such men as Poincaré, Stieltjes, and Borel, but also by supplying a very complete bibliography of algebraic continued fractions, which was especially helpful to students of that time. His address on “The influence of Fourier’s series upon the development of mathematics,” as retiring chm. of Sect. A of AAAS (no. 21) was also delivered, in 1914, in French translation at the École Normale Supérieure, Paris, and again in Rome where it was translated into Italian and published. The study of certain functional equations for the θ -functions (no. 23) was in collaboration with the gifted student F. T. H’Doubler, and counted as the latter’s doctor’s thesis. H’Doubler was the first of four young men to receive their doctorate at Wisconsin under Prof. Van Vleck’s direction; the other three were T. M. Simpson, H. T. Davis, H. S. Wall. But more than one who got his degree at another institution, received valuable initial training under Professor Van Vleck. Elsewhere in this v. we have had occasion to comment on his service in contributing to the harmonious development of the AMS, at a critical period.

Traveling, and collecting Japanese prints, are his chief hobbies. His collection of these prints, numbering thousands of items, is very remarkable, and one of the major private collections. It is especially valuable for the study of Japanese art of all periods, from the end of the sixteenth

century to the present day. His only child, John Hasbrouck Van Vleck (see *America's Young Men . . . 1936-37*) is prof. of mathematical physics at Harvard U., and also a member of the NAS.

SOURCES.—*Who's Who in Amer.*, v. 19, 1936. "Vita" in doctoral diss. (Bibl. no. 1). *Alumni Record of Wesleyan U.*, 4th ed., 1911. *Nat. Cycl. Amer. Biog.*, v. A, 1930, portrait. *Amer. Men Sci.*, 5th ed., 1933. Personal information.

BIBLIOGRAPHY

1. "Zur Kettenbruchentwicklung hyperelliptischer und ähnlicher Integrale," *AJM*, v. 16, 1894, p. 1-91. Also reprinted with special title-page, contents, "vita," etc., iii+92 p. Göttingen Doctoral diss.
2. "On the roots of Bessel- and P-functions," *AJM*, v. 19, 1897, p. 75-85.
3. "On the polynomials of Stieltjes," *AMS Bull.*, v. 4, 1898, p. 426-438.
4. "On certain differential equations of the second order allied to Hermite's equation," *AJM*, v. 21, 1899, p. 126-167+9 plates.
5. "On the determination of a series of Sturm's functions by the calculation of a single determinant," *AM*, s. 2, v. 1, 1899, p. 1-13.
6. "On linear criteria for the determination of the radius of convergence of a power series," *AMS Trans.*, v. 1, 1900, p. 293-309, 509.
7. "On the convergence of the continued fraction of Gauss and other continued fractions," *AM*, s. 2, v. 3, 1901, p. 1-18.
8. "On the convergence of continued fractions with complex elements," *AMS Trans.*, v. 2, 1901, p. 215-233.
9. "On the convergence and character of the continued fraction $\frac{a_1z}{1 + \frac{a_2z}{1 + \frac{a_3z}{\dots}}}$," *AMS Trans.*, v. 2, 1901, p. 476-483.
10. "A determination of the number of real and imaginary roots of the hypergeometric series," *AMS Trans.*, v. 3, 1902, p. 110-131.
11. "On an extension of the 1894 memoir of Stieltjes," *AMS Trans.*, v. 4, 1903, p. 297-332.
12. "A sufficient condition for the maximum number of imaginary roots of an equation of the n-th degree," *AM*, s. 2, v. 4, 1903, p. 191-192.
13. "On the convergence of algebraic continued fractions whose coefficients have limiting values," *AMS Trans.*, v. 5, 1904, p. 253-262.
14. *Lectures on Mathematics*: "Selected topics in the theory of divergent series and of continued fractions," (*AMS Colloq. Pub.*, v. 1), 1905, p. 75-187; bibl. p. 167-187.
15. "A proof of some theorems on pointwise discontinuous functions," *AMS Trans.*, v. 8, 1907, p. 189-204.
16. "On non-measurable sets of points, with an example," *AMS Trans.*, v. 9, 1908, p. 237-244.
17. "A functional equation for the sine," *AM*, s. 2, v. 11, 1910, p. 161-165; additional note, v. 13, 1912, p. 154.
18. "On the preparation of college and university instructors in mathematics," *ICT Math., Amer. Report*, Committee XII, 1911, p. 42-61; *AMS Bull.*, v. 17, 1910, p. 77-100.
19. "On the extension of a theorem of Poincaré for difference equations," *AMS Trans.*, v. 13, 1912, p. 342-352.
20. "One-parameter projective groups and the classification of collineations," *AMS Trans.*, v. 13, 1912, p. 353-386.
21. "The influence of Fourier's series upon the development of mathematics," *Science*, v. 39, 1914, p. 113-124; add. VP AAAS and chm. Sect. A 30 Dec. 1913. Italian trans.: "L'influenza della serie di Fourier sullo sviluppo della matematica," *Bollettino della "Mathesis"*, Rome, v. 6, 1914, p. 157-174.

22. "The rôle of the point-set theory in geometry and dynamics," *AMS Bull.*, v. 21, 1915, p. 321-341; AMS ret. P add. 1 Jan. 1915.
23. "A study of certain functional equations for the θ -functions" (with F. T. H'Doubler), *AMS Trans.*, v. 17, 1916, p. 9-49.
24. "Current tendencies of mathematical research," *AMS Bull.*, v. 23, 1916, p. 1-3; address at the quarter-centennial celebration of the U. Chicago.
25. "Address of Edward B. Van Vleck at the dedication of the Van Vleck Observatory," *Pop. Astr.*, v. 24, 1916, p. 416-419.
26. "Haskins's momental theorem and its connection with Stieltjes's problem of moments," *AMS Trans.*, v. 18, 1917, p. 326-330.
27. *Our Right to Ship Munitions* (Approved by Comm. on Public Information, Wash.) (*U. of Wisconsin War Pamphlets*, no. 7), Madison, Wisc., 1918, 12 p.
28. "On the combination of non-loxodromic substitutions," *AMS Trans.*, v. 20, 1919, p. 299-312.
29. "Non-loxodromic substitutions and groups in n dimensions," *AMS Trans.*, v. 24, 1922, p. 255-273.
30. "On limits to the absolute values of the roots of a polynomial," *SMF Bull.*, v. 53, 1925, p. 105-125.
31. "On the location of roots of polynomials and entire functions," *AMS Bull.*, v. 35, 1929, p. 643-683; valuable bibl. p. 672-683. Add. at a symposium in Chicago Mar. 1929.
32. "Conformal representation," *Encycl. Brit.*, 14th ed., v. 6, 1929, p. 234-236.

13. ERNEST WILLIAM BROWN

CURRICULUM VITAE.—B. Hull, Eng. 29 Nov. 1866; d. New Haven, Conn. 22 July, 1938. Educ. at Hull and East Riding C., in preparation for Christ's C., Cambridge (84-87; A.B. 87, sixth wrangler in math.; fellow 89-95); U. Cambridge (A.M. 91; Sc.D. 97). Instr. math. Haverford C. (91-93; prof. applied math. 93-00; prof. math. 00-07). Prof. math. Yale U. (07-21; Sterling prof. math. 21-31; first Josiah Willard Gibbs prof. 31-32; Josiah Willard Gibbs prof. math. emeritus 32-38). Naturalized as citizen of U.S. 30 Jan. 22.

HONORS.—Fellow RS London 98; as British subjects, Brown and Morley were the only ex-presidents eligible to become fellows. Mem. Amer. Phil. So. 98. Joint ed. *AMS Trans.* 99-06. VP AMS 05. Starred *Amer. Men Sci.* 06. Mem council Amer. Phil. So. 06-08, 10-12, 14-16, 18-21. Seventh astronomer to be awarded gold medal of RAS for researches in the lunar theory (see presidential add. *RAS MN*, v. 67, p. 300-313) 07; the sixth astronomer to receive a similar award, in 87, was G. W. Hill. Hon. A.M. Yale U. 07. Eleventh recipient U. Cambridge Adams prize (80 pounds) "for an essay on some subject of pure mathematics, astronomy or other branch of Natural Philosophy" 07; essay, "The inequalities in the motion of the moon due to the direct action of the planets" (Bibl. no. 49); J. C. Maxwell (in 57) and J. J. Thomson (83) were second and sixth recipients. G. de Pontécoulant prize of 700 francs awarded by the Acad. des Sci., Institut de France, for advancing lunar knowledge (see report *CR Paris*, v. 149, p. 1200) 09. VP AAAS and chm. Sect. A 10; ret. add. "The relations between Jupiter and the asteroids" (no. 64). Joint ed. *AMS Bull.* 10-13. Hon. fellow Christ's C., Cambridge 11. Fellow AAAS 12. Assoc. ed. *AJ*, Albany, N. Y. 12-38. Hon. Sc.D. U. Adelaide 14; when guest there at a meeting of BAAS. Gold medal (with a silver copy) by RS London in recognition of his investigations in math astr. 14. Contributor to *Encyk. d. Math. Wiss.* 15; "Theorie des Erdmondes" (no. 83). P AMS 15-16; ret. add. "The relation of mathematics to the natural sciences" (no. 90). AMS nominee mem. Div. Phys. Sci. NRC July-Dec. 19. Fifteenth recipient of Bruce Gold Medal (see report ret. P ASP, *ASP Pub.*, v. 32, p. 85-92), choice based upon nominations of six observatories, Harvard, Yerkes, Lick, Greenwich, Paris, Cordova, 20; previous recipients were 1. S. Newcomb, 8. G. W. Hill, 9. J. H. Poincaré; Brown's add. following the presentation was "The problem of the moon's motion" (no. 95). VP Amer. Alpine Club 20-22. Chm. NRC comm. on celestial mechanics (other

mems. G. D. Birkhoff, A. O. Leuschner, H. N. Russell) 20 (see report in no. 98). Correspondent astr. sect., Acad. des Sci., Institut de France 21. Mem. NAS 23. VP Amer. Astr. So. 23-25. Corresp. mem. Royal Belgian Acad. Sci. Letters and Fine Arts 26. AMS Josiah Willard Gibbs Lect. 27. P Amer. Astr. So. 28-31. Hon. Sc.D. Yale U. 33; "in grateful and affectionate acknowledgment of the luster shed upon her by your brilliant scientific achievements during a long and distinguished service on her faculty" (Angell). Hon. Sc.D. Columbia U. 34. P Amer. Assoc. Variable Star Observers 34-36. Grants from Amer. Phil. So. of \$2000 to E. W. Brown for completing work on the motions of the moon, 35, and \$500 to E. W. Brown and W. J. Eckert for the verification of the polar coordinates which are used to predict the moon's place 38. Hon. LL.D. McGill U. 36. James Craig Watson Medal awarded by NAS (see report A. O. Leuschner, *Science*, n.s., v. 85, p. 433) 37.

BIOGRAPHICAL NOTES.—Prof. Brown, only son of William and Emma (Martin) Brown, was a rather delicate youth carrying on his studies with his father's hearty encouragement and support, but he emerged at college into sturdy manhood with strength for hard study and such vigorous exercise as rowing in college boats at races (see nos. 3, 24). His high standing as wrangler just as he became of age suggested talents of high order, later to mature and lead to most notable intellectual achievements. During a year of post-graduate work at Cambridge, his chief adviser, Prof. G. H. Darwin, recommended him to study G. W. Hill's classic paper, "Researches in the lunar theory" (see Hill's Bibl. no. 35), and thus he started in a field of research which was to occupy him for more than forty-five years. This first acquaintance with American mathematics was shortly before he came to America. Within a year of his advent his first scientific paper, "On the part of the parallactic inequalities in the moon's motion which is a function of the mean motions of the sun and moon," (no. 4) appeared in *AJM*; this was fourteen years after Hill's paper had been published in the same place. The extraordinary merit of Brown's rapid sequence of publications including a *Treatise on the Lunar Theory* (no. 11) is suggested by the fact that within seven years from his first paper he was elected a fellow of the RS London. Beginning with an extension of Hill's work, he was led gradually to a complete development of a lunar theory that includes the gravitational action of every particle of matter which can have a sensible effect on the moon's motion, so that any differences which appear between theory and observation may not be set down to want of accuracy in the completeness with which the theory is carried out. Every known force capable of calculation is included. Such was the stage that he had reached in 1907 (see the great memoirs of 1897-1908 listed in no. 18), when the RAS awarded him its gold medal, and he terminated his stay at Haverford, where he had been able to carry on his work under favorable conditions. But the Yale authorities recognized the importance of his work by arranging special facilities for its continuance, and undertook to provide the funds required for both the preparation and the publication of lunar tables, which appeared twelve years later (no. 94, review by J. Jackson, *Observatory*, v. 43), with a supplement in 1926.



Ernest W. Brown

1910

The first tables of the moon strictly so-called were those of Clairaut published in 1752. Successive efforts of the ablest mathematicians to explain the observed positions of our satellite culminated in Hansen's *Tables de la Lune* (1867). These tables long held the field unchallenged, practically, although since 1880 the need for something better than Hansen's theory in the nautical almanacs was strongly felt. Before Brown's theory could replace that of Hansen it was necessary for him to make his theory accessible in the form of tables. Hansen's approximate theory included 500 terms as against Brown's 1500 terms. Brown's Tables have been uniformly used in nautical almanacs of the world since 1923, and predicted the 1923 eclipse with surprising accuracy. The aim of the Tables was to get every coefficient in latitude and longitude, in connection with the rectangular coordinates of the moon, to 0."01. No error has since been found. One incidental fact proved in Brown's theory was that Newton's law of gravitation is accurate, so far as the moon is concerned, to one part in 25,000,000.

The third stage of his lunar theory, on which Brown was engaged when he died, had as its main objective the explanation of the minor discrepancies which have revealed themselves between the tabulated and the actual motion of the moon. Leuschner has summed up some of the outstanding results of his genius. "In 1907 he had produced the most accurate value of the secular term in the moon's mean motion, but there remained unexplained well-marked deviations in the longitude of a fairly systematic character. There were also unexplained departures in the motion of the perigee and of the node of the moon's orbit amounting to the really small trifles of 17" and -12", respectively, per century. These he has practically wiped out by the inclusion of still further significant terms in his expansions. This last achievement was an unexpected by-product of a remarkable investigation on the stellar problem of three bodies," only completed in 1937 (no. 180). "In 1924 he hit upon the real character of the occasional deviations in the longitude of the moon by correlating them with those of the sun and thereby was able to eliminate a gravitational cause external to the earth for the deviation of this type of the moon, sun, Mercury and Venus. This led to the discovery of the variability of the rotation of the earth and to the establishment of the moon as a more perfect time-piece than the earth. Of greatest importance are his demonstrations of the effect of the moon on the rate of the almost perfect Shortt clocks" (no. 157). His theory of the Trojan group of asteroids (no. 104) "is outstanding as regards originality and elegance of treatment and represents the observed motions of the planets of the group more perfectly than any other."

His contributions in the more general field of celestial mechanics have been very numerous. "Resonance in the solar system" was the title of his Gibbs lecture before the Society (no. 135) and he was successful in applying a general theory of resonance to explain the gaps in the distribution of the

mean motions of minor planets (nos. 105, 164). His work on Fourier series (nos. 128, 149), on the development of the perturbative functions (no. 166), his special forms of separate differential equations, which made it possible to integrate the equations for the stellar problem of three bodies (no. 179), and other contributions, mark a new epoch in the general theory of perturbations. His latest and very notable book, *Planetary Theory*, 1933 (no. 172), develops the methods for the calculation of the general orbit of a planet, with many novel, practical, and interesting procedures. And finally, we may refer to his conclusion arrived at after highly ingenious and strictly mathematical discussion, that the discovery of the planet Pluto was not based on theoretical predictions (nos. 150, 158). In 1903 mathematicians of the U. S. rated him as seventh among the first eighty.

In addition to achieving a monumental body of research Prof. Brown gave courses of lectures at Yale for many years, and the following 8 men wrote their doctoral dissertations under his direction, 1912–31: W. H. Willard, A. L. Daniels, T. H. Brown, H. B. Hedrick, W. L. Crum, P. Slavenas, D. B. Ames, W. J. Eckert. Dr. Hedrick was associated with him for many years in the preparation of the lunar tables. Dr. Eckert is a member of the faculty of Columbia U. and secy.-treas. of the remarkable astronomical Computing Bureau there, directed by an advisory council of the Amer. Astr. So. Prof. Brown was chm. of the board of managers of this Bureau to the close of 1937; see "The astronomical Hollerith-computing bureau," *ASP Pub.*, v. 49, 1937, p. 249 f.

Prof. Brown was generous in giving up time to writing popular articles (e.g., nos. 22, 29, 44, 45, 47, 106), to the writing of many reviews (no. 181), and to editorial work which included years of valued services in connection with both the Society's *Bulletin* and *Transactions*. We have more specifically referred to his service on the *Transactions* in chapter V.

Like Newcomb, Brown formerly delighted in high climbing on Swiss mountains. He also found recreation in music—we have listed his settings of Haverford songs (no. 34A). He used to sing in choruses and choirs and was at one time president of the Oratorio So. in New Haven. When he was being presented for his Yale doctorate W. L. Phelps spoke in part as follows: "His publications on lunar theory and celestial mechanics have given him an international reputation and have added glory to Yale. His Tables of the motion of the moon is a monumental work and has brought him a blizzard of degrees, medals, prizes and honors. He is an excellent chess player and an amateur humorist of high reputation. In his youth he expected to be a concert pianist, but later took up the music of the spheres. His versatility is additionally shown in that, although a specialist on the moon, in the year 1925 in the city of New Haven he arranged a personally conducted total eclipse of the sun."

To one surveying the Society's history a feeling of great pride must be engendered by the fact that among her presidents have been three great

men who worked on a common problem: Newcomb, that mighty watcher of the skies; Hill and Brown, the leaders among all mathematical astronomers who have achieved their careers in this country. Incidentally it may be remarked that the two latter, like the greatest mathematical astronomer of all time, were wedded to their intellectual interests alone. The same might be said of A. S. Eddington and Josiah Willard Gibbs.

SOURCES.—*Who's Who 1938*, London. *Who's Who in Amer.*, v. 19. *Nat. Cycl. Amer. Biog.*, v. 15, 1916. "Poggendorff," v. 4-6. Personal information. *New York Times*, 24 July 1938, section I, p. 29, portrait.

BIBLIOGRAPHY

1. [A popular article on the future of the earth's history], *Totteridge Park Mag.*, c. 1887-8.
2. "College and other totems," *Christ's C. Mag.*, v. 2, no. 6, 1888, p. 4-6.
3. "Records of the boat club," *Christ's C. Mag.*, 1889, v. 3, no. 10, p. 105-113; v. 4, no. 11, p. 23-30.
4. "On the part of the parallactic inequalities in the moon's motion which is a function of the mean motions of the sun and moon," *AJM*, v. 14, 1892, p. 141-160; summary, "On the part of the parallactic class of inequalities in the moon's motion, which is a function of the ratio of the mean motions of the sun and moon," *CPS Proc.*, v. 7, 1891, p. 220-221.
5. "Note on the lunar theory," *RAS MN*, v. 52, 1892, p. 408-409; v. 54, 1894, p. 471; v. 55, 1895, p. 3-6.
6. "On the errors produced in numerical calculations by the use of decimals," *Haverford C. Studies*, no. 11, 1892, p. 50-55.
7. "On the determination of a certain class of inequalities in the moon's motion," *RAS MN*, v. 52, 1892, p. 71-80.
8. "The elliptic inequalities in the lunar theory," *AJM*, v. 15, 1893, p. 244-263, 321-338.
9. "Investigations in the lunar theory," *AJM*, v. 17, 1895, p. 318-358.
10. "Co-education in the colleges and universities of the United States," *Cambridge [Eng.] Rev.*, v. 17, 1896, p. 330-331.
11. *An Introductory Treatise on the Lunar Theory*, Cambridge, 1896, xvi+292 p.
12. "Note on Hansen's lunar and planetary theories," *RAS MN*, v. 56, 1896, p. 52-53.
13. "Note on Mr. Stone's paper, 'Expressions for the elliptic coordinates of a moving point to the seventh order of small quantities'," *RAS MN*, v. 56, 1896, p. 370-371.
14. "On the application of the principal function to the solution of Delaunay's canonical system of equations," *LMS Proc.*, v. 27, 1896, p. 385-390.
15. "On the application of Jacobi's dynamical method to the general problem of three bodies," *LMS Proc.*, v. 28, 1896, p. 130-142.
16. "On certain properties of the mean motions and the secular accelerations of the principal arguments used in the lunar theory," *LMS Proc.*, v. 28, 1896, p. 143-155.
17. "On the theoretical values of the secular accelerations in the lunar theory," *RAS MN*, v. 57, 1897, p. 342-349.
18. "Theory of the motion of the moon; containing a new calculation of the expressions for the coordinates of the moon in terms of the time," *RAS Mem.*, v. 53, p. 39-116, 163-202; v. 54, p. 1-63; v. 57, p. 51-145; v. 59, p. 1-103, 1897-1908.
19. "On recent progress toward the solution of problems in hydrodynamics," *AAAS Proc.*, v. 47, 1898, p. 53-64; *Science*, n.s., v. 8, 1898, p. 641-651.
20. "On the mean motions of the lunar perigee and node," *RAS MN*, v. 57, 1898, p. 332-341.
21. "Note on the mean motions of the lunar perigee and node," *RAS MN*, v. 57, 1898, p. 566-567.
22. "Glimpses of English student life," *Haverfordian*, v. 20, 1899, p. 155-159.
23. "Note on the values of the coefficients of the terms of the third order in the new lunar theory," *RAS MN*, v. 50, 1899, p. 124-125.

24. "Rowing on the Cam," *Haverfordian*, v. 21, 1899, p. 19–23.
25. "On the solution of a pair of simultaneous linear differential equations, which occur in the lunar theory," *CPS Trans.*, v. 18, 1900, p. 94–106.
26. "On tide currents in estuaries and rivers," *AM*, s. 2, v. 1, 1900, p. 68–71.
27. "A possible explanation of the sun-spot period," *RAS MN*, v. 60, 1900, p. 599–606.
28. "Modern methods of treating dynamical problems and in particular the problem of three bodies," *AMS Bull.*, v. 8, 1901, p. 103–113; abridgement of four Colloq. Lects. before AMS, delivered at Cornell U. 21–24 Aug. 1901.
29. "A scramble up the Matterhorn," *Haverfordian*, v. 22, 1901, p. 141–146.
30. "On the small divisors in the lunar theory," *AMS Trans.*, v. 3, 1902, p. 159–185.
31. "The moons of Mars," *Philadelphia Public Ledger*, June 1903.
32. "On the formation of the derivatives of the lunar coordinates with respect to the elements," *AMS Trans.*, v. 4, 1903, p. 234–248.
33. "On the variation of the arbitrary and given constants in dynamical equations," *AMS Trans.*, v. 4, 1903, p. 333–350.
34. "On the verification of the Newtonian law," *RAS MN*, v. 63, 1903, p. 396–397.
- 34A. *Haverford College Song Book*, New York, 1903, Music for: (a) "Arms and the man," p. 4; (b) "It's a right little, tight little college," p. 6.
35. "The laws of gravitation," *Haverford C. Bull.*, v. 2, no. 3, 1904, p. 17–22.
36. "Moon," *Encycl. Amer.*, 1904; 1936 ed., v. 19, p. 423–427+2 plates.
37. "Note on George Gabriel Stokes," *Phys. Rev.*, v. 18, 1904, p. 58–62; *Smithsonian Reports for 1904*, 1905, p. 773–777+1 plate.
38. "On the completion of the solution of the main problem in the new lunar theory," *RAS MN*, v. 65, 1904, p. 104–108.
39. "On the degree of accuracy of the new lunar theory, and on the final values of the mean motions of the perigee and node," *RAS MN*, v. 64, 1904, p. 524–534.
40. "On the smaller perturbations of the lunar arguments," *AMS Trans.*, v. 5, 1904, p. 279–287, 551.
41. "The parallactic inequality and the solar parallax," *RAS MN*, v. 64, 1904, p. 534–535.
42. "The final values of the coefficients in the new lunar theory," *RAS MN*, v. 65, 1905, p. 276–296.
43. "On a general method for treating transmitted motions and its application to indirect perturbations," *AMS Trans.*, v. 6, 1905, p. 332–343.
44. "Sunspots and Weather," *Pop. Sci. Mo.*, v. 66, 1905, p. 505–514.
45. "With the British Association in South Africa," *Pop. Sci. Mo.*, v. 68, 1906, p. 5–20, 145–160.
46. "College men in the African gold mines," *Haverfordian*, v. 29, 1907, p. 51–52.
47. "The story of the moon," *American Friend*, v. 14, 1907, p. 292–294.
48. "Haverford and its future. Address to the class of 1907, Haverford College . . . Commencement Day, June 14, 1907," *Haverford C. Bull.*, v. 6, no. 3, 1908, 18 p.
49. *The Inequalities in the Motion of the Moon due to the Direct Action of the Planets. An Essay which obtained the Adams Prize in the University of Cambridge for the Year 1907*, Cambridge, 1908, xii+92 p.
50. [Letter], *Science*, n.s., v. 27, 1908, p. 350.
51. "On the lunar inequalities due to planetary action," *RAS MN*, v. 68, 1908, p. 148–170.
52. "On the lunar inequalities due to the motion of the ecliptic and the figure of the earth," *RAS MN*, v. 68, 1908, p. 450–455.
53. "New plans for tabulating the moon's longitude," *Science*, n.s., v. 30, 1909, p. 729.
54. "On an addition to the theoretical secular acceleration of the moon's mean motion," *RAS MN*, v. 70, 1909, p. 143–148.
55. "On an error in the new lunar theory," *RAS MN*, v. 70, 1909, p. 3.
56. "On the plans for new tables of the moon's motion," *RAS MN*, v. 70, 1909, p. 148–175.

57. "On the effects of certain magnetic and gravitational forces on the motion of the moon," *AJS*, v. 29, 1910, p. 529-539.
58. "Simon Newcomb," *Observatory*, v. 33, 1910, p. 222.
59. "Simon Newcomb," *AMS Bull.*, v. 16, 1910, p. 341-355.
60. "On a new family of periodic orbits in the problem of three bodies," *RAS MN*, v. 71, 1911, p. 438-454.
61. "On planetary librations," *AJ*, v. 27, 1911, p. 25-26.
62. "On the oscillating orbits about the triangular equilibrium points in the problem of three bodies," *RAS MN*, v. 71, 1911, p. 492-502.
63. "On the progress of the new tables of the moon's motion," *RAS MN*, v. 71, 1911, p. 639-650.
64. "The relations between Jupiter and the asteroids," *Science*, n.s., v. 33, 1911, p. 79-93. Add. VP AAAS and Chm. Sect. A 28 Dec. 1910.
65. "The transformation of the moon's latitude," *RAS MN*, v. 71, 1911, p. 651-660.
66. "On a device for facilitating harmonic analysis and synthesis," *RAS MN*, v. 72, 1912, p. 454-463.
67. "On librations in planetary and satellite systems," *RAS MN*, v. 72, 1912, p. 609-630.
68. "On the sum of a certain triple series," *AM*, s. 2, v. 13, 1912, p. 129-136.
69. "The longitude of the moon from 1750 to 1910," *RAS MN*, v. 73, 1913, p. 692-714.
70. "Periodicities in the solar system," *Intern. Congress Mathems.*, Cambridge, v. 1, 1913, p. 81-92.
71. "Sir George Darwin," *Scientific Mo.*, v. 32, 1913, p. 309-311.
72. "Address on cosmical physics (lunar theory)," *BAAS Report*, 1914, Australia, 11 p.; *Nature*, v. 94, p. 184-190; *Science*, n.s., v. 40, p. 389-401.
73. "Corrections of errors in the new lunar theory," *RAS MN*, v. 74, 1914, p. 424.
74. "The determination of the constants of the node, the inclination, the Earth's ellipticity, and the obliquity of the ecliptic from the Greenwich meridian observations of the moon, 1847-1901," *RAS MN*, v. 74, 1914, p. 552-568.
75. "George William Hill," *Nation*, v. 98, 1914, p. 540-541.
76. "The mean latitudes of the moon and sun," *RAS MN*, v. 74, 1914, p. 156-167.
77. "The perigee and eccentricity of the moon," *RAS MN*, v. 74, 1914, p. 396-424.
78. "Problems of the moon's motion," *Observatory*, v. 38, 1914, p. 206-211.
79. "The terms in the moon's motion depending on the node," *RAS MN*, v. 74, 1914, p. 392-396.
80. "The elements of the moon's orbit," *RAS MN*, v. 75, 1914, p. 508-516.
81. "G. W. Hill, 1838-1914," *RS Proc.*, London, v. 91A, 1915, p. xlii-li; reprinted: "George William Hill, 1838-1914," *AMS Bull.*, v. 21, 1915, p. 499-511.
82. "A simple and inexpensive apparatus for tidal analysis," *AJS*, v. 39, 1915, p. 386-390.
83. "Theorie des Erdmondes," *Encyk. d. Math. Wiss.*, v. VI-2, 1915, p. 667-728. "Übersetzt und mit einigen Zusätzen versehen von A. v. Brunn."
84. "George Howard Darwin (1845-1912)," *AAcAS Proc.*, v. 51, 1916, p. 863-864.
85. "George William Hill (1838-1914)," *AAcAS Proc.*, v. 51, 1916, p. 890-891.
86. "Simon Newcomb (1835-1909)," *AAcAS Proc.*, v. 51, 1916, p. 908-909.
87. "The scientific work of Sir George Darwin," G. H. Darwin, *Scientific Papers*, v. 5, Cambridge, 1916, p. xxxiv-lv.
88. "Biographical memoir of George William Hill, 1838-1914," *NAS Biog. Mem.*, v. 8, 1916, p. 273-309. Portrait.
89. "The moon's place at the solar eclipse of 1918, June 8," *AJ*, v. 30, 1917, p. 176-178.
90. "The relation of mathematics to the natural sciences," *AMS Bull.*, v. 23, 1917, p. 213-230. AMS ret. P add. 28 Dec. 1916.
91. "Mathematics for freshmen and sophomores," *Yale Alumni Weekly*, December 13, 1918.
92. "The position of the moon at the eclipse of 1918, June 8," *AJ*, v. 31, 1918, p. 112.

93. "On the determination of the secular acceleration of the moon's longitude from modern observations," *RS Proc.*, v. 96A, 1919, p. 69-70.
94. *Tables of the Motion of the Moon*, with assistance of H. B. Hedrick, 3 v., New Haven, 1919. Complement to "The tables of the motion of the moon, containing the remainder terms for the century 1800-1900, and errata in the tables," *Yale Obs., Trans.*, v. 3, part 5, 1926, p. 157-204.
95. "The problem of the moon's motion," *ASP Pub.*, v. 32, 1920, p. 93-104.
96. "The history of mathematics," *Scientific Mo.*, v. 12, 1921, p. 385-413. Lect. before Gamma Alpha frat., Yale U. 26 Feb. 1920.
97. "On the passage of a star through a nebula," *Astrophys. J.*, v. 53, 1921, p. 169-178.
98. "Celestial Mechanics. Report of the Committee on Celestial Mechanics" (with G. D. Birkhoff, A. O. Leuschner, H. N. Russell), *NRC Bull.*, no. 19, 1922, 22 p.
99. "The moon's mean motion and the new tables," *AJ*, v. 34, 1922, p. 52-54.
100. "The age of the earth from the point of view of astronomy," *APS Proc.*, v. 61, 1923, p. 283-285.
101. "Mathematics," L. L. Woodruff, *The Development of the Sciences*, New Haven, 1923, Chap. 1, p. 1-42.
102. "The general orbits of the asteroids of the Trojan group," *AJ*, v. 35, 1923, p. 69-80.
103. "On the applications of Delaunay's lunar theory to the eighth satellite of Jupiter," *AJ*, v. 35, 1923, p. 1-4.
104. "Theory of the Trojan group of asteroids, chapter I and chapters II to VI development of the theory and applications," *Yale Obs., Trans.*, v. 3, 1923, p. 1-47; v. 3, 1925, p. 81-133.
105. "An explanation of the gaps in the distribution of the asteroids according to their periods of revolution," *NAS Proc.*, v. 10, 1924, p. 248-253.
106. Numerous articles on the eclipse of January 24, 1925 in *Pop. Astr.*, and other journals and newspapers, 1924 and 1925.
107. "A celestial encounter," in N. G. Osborn, *History of Connecticut in Monographic Form*, 1925, p. 539-601.
108. "The eclipse observations at the Yale Observatory," *Pop. Astr.*, v. 33, 1925, p. 180-182.
109. "Eclipse investigations not requiring special equipment," *Scientific Amer.*, v. 132, 1925, p. 14-15.
110. "Eclipse of January 24, 1925," *Science*, n.s., v. 61, 1925, p. 10-12.
111. "The effect of varying mass on a binary system," *NAS Proc.*, v. 11, 1925, p. 274-279; correction, v. 12, 1926, p. 1-2.
112. "Gravitational forces in spiral nebulae," *Astrophys. J.*, v. 61, 1925, p. 97-113.
113. "On the stability of the Earth as a time keeper," Intern. Geophys. Congress, Madrid, 1925, 4 p.
114. "Tidal oscillations in Halemaumau, the lava pit of Kilauea," *AJS*, s. 5, v. 9, 1925, p. 95-112.
115. "The International Astronomical Union at Cambridge," *Pop. Astr.*, v. 33, 1925, p. 569-574.
116. "Comparison of the Greenwich and photographic positions of the moon, 1911-1917," *AJ*, v. 36, 1926, p. 153-155.
117. "Comparison of the Washington and Greenwich observations of the moon for 1923, 4, 5, with the new tables," *AJ*, v. 37, 1926, p. 29-32.
118. "Discussion of observations of the moon at and near the eclipse of 1925, January 24," *AJ*, v. 37, 1926, p. 9-19.
119. "The evidence for changes in the rate of rotation of the earth and their geophysical consequences, with a summary and discussion of the deviations of the moon and sun from their gravitational orbits," *Yale Obs., Trans.*, v. 3, 1926, p. 205-235 + 3 plates.
120. "Request for more observations of occultations," *BAA Journ.*, v. 37, 1926, p. 94-96; *Pop. Astr.*, v. 35, 1927, p. 17-20.
121. "Aufforderung zur Vermehrung der Beobachtungen von Sternbedeckungen; Bemerkungen für Beobachter mit beschränkter astronomischer Ausrüstung," *AN*, v. 229, 1927, cols. 225-228.

122. "Changes in the length of the day," *Nature*, v. 119, 1927, p. 200–202.
123. "The earth's rotation," *Observatory*, v. 50, 1927, p. 90.
124. "On Dr. Fotheringham's paper entitled 'Trepidation'," *RAS MN*, v. 87, 1927, p. 524–527.
125. "Request for more observations of occultations," *AJ*, v. 37, 1927, p. 99–100.
126. "Developments following from Newton's work," in *Sir Isaac Newton, 1727–1927. A Bicentenary Evaluation of His Work*, Baltimore, 1928, p. 111–124.
127. "Discussion of the moon's motion 1923–26," *AJ*, v. 38, 1928, p. 129–132.
128. "The Fourier expansions of $(1+a^2-2ak \cos \psi)^{-3}$," *RAS MN*, v. 88, 1928, p. 459–465.
129. "Gravitational motion in a spiral nebula," *Observatory*, v. 51, 1928, p. 277–286.
130. "Occultations: a report of progress," *Pop. Astr.*, v. 36, 1928, p. 282–284.
131. "Reductions of occultations observed in 1926," *AJ*, v. 38, 1928, p. 120–123.
132. "Reduction of the Washington meridian observations of the moon for the years 1923–6," *AJ*, v. 38, 1928, p. 125–129.
133. "A remainder formula and its use in the development of the disturbing function by harmonic analysis," *RAS MN*, v. 88, 1928, p. 624–634.
134. "The residuals from occultations of the years 1923–6," *AJ*, v. 38, 1928, p. 133–138.
135. "Resonance in the solar system, fifth Josiah Willard Gibbs lecture before the AMS, 28 Dec. 1927." *AMS Bull.*, v. 34, 1928, p. 265–289.
136. "The change from 7" to 6" for use with the occultations observed in 1929," *AJ*, v. 39, 1929, p. 109.
137. "Compilation and discussion of 418 occultations observed in 1927" (with D. Brouwer), *AJ*, v. 39, 1929, p. 97–109.
138. "Corrections to certain articles on occultations" (with D. Brouwer), *AJ*, v. 39, 1929, p. 96.
139. "The mean apparent error of the moon's longitude for 1927" (with D. Brouwer), *AJ*, v. 39, 1929, p. 32.
140. "Planetary theory with the true longitude as independent variable," *RAS MN*, v. 90, 1929, p. 3–17.
141. "Practical astronomy for amateurs," *Scientific Amer.*, v. 85, 1929, p. 426–427; reprinted, *RASC Journ.*, v. 24, 1930, p. 177–183.
142. "Applications of an expansion theorem to the development of the disturbing function," *NAS Proc.*, v. 16, 1930, p. 77–83.
143. "Compilation and discussion of 746 occultations observed in 1928" (with D. Brouwer), *AJ*, v. 40, 1930, p. 185–200.
144. "De como el aficionado ayuda a observar y calcular los movimientos de la luna," *Revista Astronomica*, v. 2, 1930, p. 201–207.
145. "The development of the disturbing function in multiples of the eccentric anomalies and in powers of the eccentricities and inclination to any order," *AJ*, v. 40, 1930, p. 19–23.
146. "The eclipse of April 25," *Science*, n.s., v. 71, 1930, p. 314.
147. "The expansion of the constant term of the disturbing function to any order," *AJ*, v. 40, 1930, p. 35–38.
148. "On a general method for the development of the disturbing function," *AJ*, v. 40, 1930, p. 19–23.
149. "On an extension of the Fourier theorem giving rapid methods for calculating the constant part and the coefficient of any periodic term in the disturbing function," *NAS Proc.*, v. 16, 1930, p. 150–156.
150. "On the predictions of trans-Neptunian planets from the perturbations of Uranus," *NAS Proc.*, v. 16, 1930, p. 364–371.
151. "Practical astronomy for amateurs. How the amateur astronomer is helping to observe and calculate the moon's motions," *RASC Journ.*, v. 24, 1930, p. 177–183.
152. "Preliminary value of the error of the moon's mean longitude for 1929" (with D. Brouwer), *AJ*, v. 40, 1930, p. 91.

153. "Theory of the eighth satellite of Jupiter" (with D. Brouwer), *Yale Obs., Trans.*, v. 6, 1930, pt. 4.
154. "The age of the earth from astronomical data," *NRC Bull.*, no. 80, 1931, p. 460-466.
155. "Analysis of records made on the Loomis chronograph by three Shortt clocks and a crystal oscillator" (with D. Brouwer), *RAS MN*, v. 91, 1931, p. 575-591.
156. "Compilation and discussion of 722 occultations observed in 1929," *AJ*, v. 41, 1931, p. 53-69.
157. "The lunar term in Shortt clocks" (with D. Brouwer), *Observatory*, v. 54, 1931, p. 166.
158. "On a criterion for the prediction of an unknown planet," *RAS MN*, v. 92, 1931, p. 80-101.
159. "On a method of solving Kepler's equation," *RAS MN*, v. 92, 1931, p. 104.
160. "The variation of latitude" (with W. D. Lambert and F. Schlesinger), *NRC Bull.*, no. 78, 1931, p. 245-277.
161. "When the state was icebound," *New Haven Journal Courier*, March 9, 1931. Also occasional unsigned editorials in the *Courier*.
162. "Compilation and discussion of 663 occultations observed in 1930" (with D. Brouwer), *AJ*, v. 41, 1932, p. 185-196.
163. "The development of the disturbing function with large values of the ratio of the distances," *RAS MN*, v. 92, 1932, p. 224-227.
164. "Elements of the theory of resonance illustrated by the motion of a pendulum," [Lects. at the Rice Institute 22-24 Apr. 1931], *RI Pamphlets*, v. 19, 1932, p. 1-60. Also reissued as a pamphlet in Cambridge, Eng., 1932, 60 p.
165. "Observation and gravitational theory in the solar system," *ASP Pub.*, v. 44, 1932, p. 21-40.
166. "Tables for the development of the disturbing function with schedules for harmonic analysis" (with D. Brouwer), *Yale Obs., Trans.*, v. 6, 1932, pt. 5. Also reissued Cambridge, Eng., 1933, 4 p. + p. 73-157.
167. "Time and its measurement," *Amer. Inst. Elec. Engin., Trans.*, v. 51, 1932, p. 523-526.
168. "George William Hill," *DAB*, v. 9, 1932, p. 32-33.
169. "Compilation and discussion of 859 occultations observed in 1931" (with D. Brouwer), *AJ*, v. 42, 1933, p. 181-193.
170. "The motion of the moon, 1923-1931," *RAS MN*, v. 93, 1933, p. 603-619.
171. "Occultations of the year 1924 collected and reduced by the Bond Club," *AJ*, v. 42, 1933, p. 145-148.
172. *Planetary Theory* (with C. A. Shook), Cambridge, Eng., 1933, xi+(1)+302 p.
173. "Revision of the residuals from occultations of the years 1923-6 with additions" (with D. Brouwer), *AJ*, v. 43, 1933, p. 49-55.
174. "Compilation and discussion of 1199 occultations observed in 1932" (with D. Brouwer), *AJ*, v. 43, 1934, p. 137-152.
175. "Compilation and discussion of 1194 occultations observed in 1933" (with D. Brouwer), *AJ*, v. 44, 1935, p. 129-146.
176. "Gravitation in the solar system," [lect. at the Smithsonian 25 Jan. 1933], *Smithsonian Inst., Annual Report for 1933*, Wash., 1935, p. 181-188.
177. "Change from 5" to 3" in the reduction of the occultations observed in 1936" (with D. Brouwer), *AJ*, v. 44, 1936, p. 176.
178. "On the calculation of the principal parts of the motions of the lunar perigee and node," *AJ*, v. 45, 1936, p. 84-88.
179. "Solutions of the equations of variations," *RAS MN*, v. 96, 1936, p. 579-587.
180. "The stellar problem of three bodies: I. Application of satellite theory; II. The equations of motion with a simplified solution; III. The motions of the apse and node with applications to the moon; IV. Perturbations in the system E Ursae Majoris," *RAS MN*, v. 97, 1936, p. 56-61, 62-66, 116-127; 1937, p. 388-395.

181. Reviews of books by Burbury in *Phys. Rev.*, 1901; by J. C. Adams, Lamb, Schubert, Gundelfinger, Darwin, Levy, Rajna, Tisserand and Andoyer, Peirce, Kepler, Kirchoff, Meriman, Poincaré, Rice, Villie, Berry, Suter, Clerke, Green, E. B. Wilson, H. G. Bader, Tamborel, Jordan, Larmor, Jeans, Born, of *Annuaire du Bureau des Longitudes* (1897–1906, 1908–1909), of *Astronomical Papers prepared for the use of the American Ephemeris and Nautical Almanac*, 5, 6, 7, of *Belgian Annuaire Astronomique*, 1905, in *AMS Bull.*, 1896–1928; of books by Webster, Hill, Larmor, Darwin, Noyes in *Science*, 1905–22; by Hale, Ornstein in *AJS*, 1908–1928; by Plummer in *Astrophys. J.*, 1919; and by Jeans in *Yale Rev.*, 1930.

14. LEONARD EUGENE DICKSON

CURRICULUM VITAE.—B. Independence, Ia. 22 Jan. 1874. Attended U. Texas while serving as chemist on the Geol. Survey of the state and graduated as valedictorian (Sc. B. 93, A.M. 94); continued post graduate study in math. at U. Chicago where he was one of the first two mathematicians to get the doctorate (Ph.D. 96), and at U. Paris and Leipzig (96–97). Instr. math. U. California (97–99; assist. prof. 99); assoc. prof. U. Texas 99–00; assist. prof. U. Chicago (00–07); assoc. prof. 07–10; prof. 10–). Visiting prof. U. California 14, 18, 22.

HONORS.—VP AMS 10. Joint ed. *AMS Trans.* Oct. 10–Dec. 16. Mem. NAS 13; resigned 37. Colloq. lect. AMS 13. Assoc. Fellow AACAS 15. P AMS 17–18. AMS nominee mem. Div. Phys. Sci. NRC 19–22. Corresp. mem. sect. geom. Acad. des Sci., Institut de France 20 (see *AMM*, v. 27, 1920, p. 384). Hon. P. Intern. Math. Union 20. Mem. Div. For. Relations NRC as chm. Amer. Sect. Intern. Math. Union 20–24. VP, and one of the four general lects., Intern. Congress Mathems. Strasbourg 20; topic, "Some relations between the theory of numbers and other branches of mathematics" (Bibl. no. 209). Mem. Amer. Phil. So. 20; resigned, 25. Chm. Comm. on Algebraic Numbers, Div. Phys. Sci. NRC 20– . Hon. mem. Czechoslovakian Union of Math. and Phys. 23. First award of \$1000 prize, offered by a member of the AAAS for the most notable contribution to the advancement of science, reported at its Cincinnati meeting, 24; the award was made for the book *Algebras and their Arithmetics* (Bibl., no. 229) together with two papers presented by Dickson at Cincinnati, namely, "The theory of numbers and generalized quaternions" (no. 235) and "Quadratic fields in which factorization is always unique" (no. 234). VP Intern. Congress Mathems. Toronto 24. Awarded AMS Frank Nelson Cole Prize of \$200 for his book, *Algebren und ihre Zahlentheorie* (no. 253) 28. Mem. comm. eds. *CMP Rend.* 28–35. One of four mathems. (chosen because they were regarded as the leading research men in America, England, France and Italy), lects. at Harvard Tercentenary Celebration 36. Hon. Sc.D. Harvard Terc. Celeb. 36.

BIOGRAPHICAL NOTES.—Prof. Dickson's father was a merchant and banker of Texas, and a descendant of William Dickson, a native of Londonderry, Ireland, who came to America in the early part of the eighteenth century and settled at Londonderry, N. H. Prof. Dickson is one of the greatest research mathematicians that America has produced, and his research output has been enormous. In addition to more than 280 papers he has published eighteen books, two of which have been translated into German; one has appeared only in German. Fifteen of these books present material of high importance and include his monumental *History of the Theory of Numbers* in three volumes (no. 204; reviewed in *AMS Bull.*, v. 26, 30, and *AMM*, v. 26, 28, 30). In the preface to the second v. Dickson takes us into his confidence. "Conventional histories take for granted that each fact has been discovered by a natural series of deductions from earlier facts and devote considerable space in the attempt to

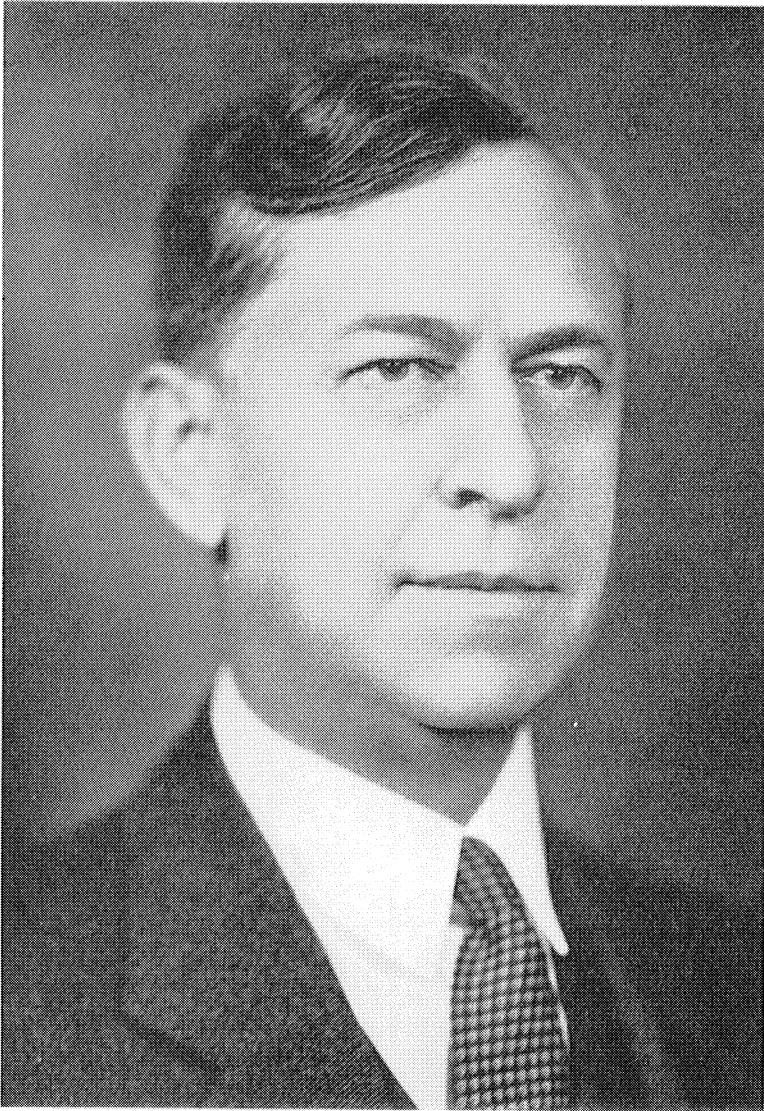
trace the sequence. But men experienced in research know that at least the germs of many important results are discovered by a sudden and mysterious intuition, perhaps the result of subconscious mental effort, even though such intuitions have to be subjected later to the sorting process of the critical faculties. What is generally wanted is a full and correct statement of the facts, not an historian's personal explanation of those facts. The more completely the historian remains in the background or the less conscious the reader is of the historian's personality, the better the history. . . . With such a view of the ideal self-effacement of the historian, what induced the author to interrupt his own investigations for the greater part of the past nine years to write this history? Because it fitted in with his convictions that every person should aim to perform at some time in his life some serious, useful work for which it is highly improbable that there will be any reward whatever other than his satisfaction therefrom." Here as in all of his writing Dickson's extraordinary gift of clear, compact, exact expression and compression is everywhere in evidence.

In Dickson's *Algebren und ihre Zahlentheorie*, which won the prize noted above, a new theory was devised to determine what should be the subject-matter of arithmetics and algebras, after which it was found possible to construct a highly developed science of arithmetics. The result is a rich array of fundamental results which mark great steps forward in the classical theory of algebraic numbers and in the generalization of Hurwitz's integral quaternions. Dickson was able to unify and greatly enlarge the whole subject of the theories of algebras (see *Science*, n.s., v. 59, 1934, p. 77). E. T. Bell wrote of the English form of this work that it "bids fair to be epoch-making." See Hasse's detailed review in *DMV Jahrb.* v. 37, 1928.

Dickson discovered the fundamental cyclic algebras, essential in the theory of "Division algebras" (nos. 121, 122 and chap. 5 in no. 229). It has been called a "Dickson algebra" by Wedderburn (*AMS Trans.*, v. 22, p. 129). He was the founder of the theory of modular invariants (compare no. 183). He exploded a fallacy which had persisted in connection with certain Diophantine equations from the time of Gauss to the present day (nos. 212, 213, 241). His solution of Waring's problem (no. 290) is outstanding and the results in such papers as no. 104 and 116 are of special interest.

Even back in 1903, when Dickson had been an assistant professor at the U. Chicago for only three years, mathematicians of the U. S. ranked him as ninth (*Amer. Men Sci.*, 5th ed., p. 1269); the first eight then were, Moore, Hill, Osgood, Bôcher, Bolza (Newcomb), Morley, Brown, and White. He was an assoc. ed. of the *AMS Trans.* 1911-16; managing ed. of the *AMM*, 1902-06, and assoc. ed. 1906-08.

Prof. Dickson's ideas and publications have been developed by many



Leonard E. Dickson.

1932

others and in particular by the following 64 persons who prepared their theses for the doctorate under his direction at the U. of Chicago, 1901–37: T. M. Putnam, W. H. Bussey, H. E. Jordan, A. Ranum, R. L. Börger, A. H. Wilson, W. C. Krathwohl, Mildred L. Sanderson, F. B. Wiley, Olive C. Hazlett, A. Henderson, J. E. McAtee, G. H. Cresse, W. L. G. Williams, Mayme I. Logsdon, C. C. MacDuffee, H. S. Everett, J. S. Turner, Mrs. Constance R. Ballantine, M. M. Feldstein, G. E. F. Sherwood, B. F. Yanney, Marguerite D. Darkow, C. Gouwens, Mildred Hunt, C. G. Latimer, F. S. Nowlan, Echo D. Pepper, A. E. Cooper, R. J. Garver, J. S. Georges, R. G. Archibald, Lois W. Griffiths, J. Williamson, A. A. Albert, B. W. Jones, D. C. Morrow, E. L. Thompson, K. C. Yang, O. E. Brown, R. H. Marquis, G. Pall, S. Silberfarb, A. Oppenheim, R. S. Underwood, Mina S. Rees, Emily M. Chandler, A. E. Ross, F. W. Sparks, Ruth G. Mason, R. D. James, R. Hull, R. E. Huston, Frances E. Baker, R. C. Shook, G. C. Webber, Marie Litzinger, K. S. Ghent, Mable G. Humphreys, J. C. Brixey, Mae R. Anderson, Dora McFarland, S. B. Townes, H. Chatland.

Bridge, tennis, and billiards have long been Professor Dickson's chief recreations.

SOURCES.—T. C. Dickson, *Some of the Descendants of William Dickson and Elizabeth Campbell of Cherry Valley, New York*, Brattleboro, Vt., 1938; L. E. Dickson, no. 363, p. 147–148. The genealogy of Dickson's mother is to be found in T. C. Dickson, *Some of the Descendants of Lt. Thomas Tracy of Norwich, Conn.*, Philadelphia, Pa., 1937. *Nat. Cycl. Amer. Biog.*, v. 18, 1922. *Publications of the Members of the University of Chicago 1902–1916*, Chicago, 1917. *Who's Who in Amer.*, v. 19. *Amer. Men Sci.*, 5th ed.

BIBLIOGRAPHY

1. "On the number of inscriptible regular polygons," *NYMS Bull.*, v. 3, 1894, p. 123–125.
2. "Lowest integers representing sides of a right triangle," *AMM*, v. 1, 1894, p. 6–11.
3. "The simplest model for illustrating the conic sections," *AMM*, v. 1, 1894, p. 261.
4. "The inscription of regular polygons," *AMM*, v. 1, 1894, p. 299–301, 342–345, 376–377, 423–425; v. 2, 1895, p. 7–9, 38–40.
5. "Some fallacies of an angle trisector," *AMM*, v. 2, 1895, p. 71–72.
6. "A quadratic Cremona transformation defined by a conic," *AMM*, v. 2, 1895, p. 218–221.
7. "Gergonne's pile problem," *AMS Bull.*, v. 1, 1895, p. 184–186.
8. "On the inscription of regular polygons," *AM*, v. 9, 1895, p. 73–84.
9. "Cyclic numbers," *QJM*, v. 27, 1895, p. 366–377.
10. "A quadratic Cremona transformation defined by a conic," *CMP Rend.*, v. 9, 1895, p. 256–259.
11. "Analytic functions suitable to represent substitutions," *AJM*, v. 18, 1896, p. 210–218.
12. "The analytic representation of substitutions on a power of a prime number of letters with a discussion of the linear groups," *AM*, v. 11, 1897, p. 65–120, 161–183. Doctoral diss.
13. "Systems of continuous and discontinuous simple groups," *AMS Bull.*, v. 3, 1897, p. 265–273.
14. "Higher irreducible congruences," *AMS Bull.*, v. 3, 1897, p. 381–389.
15. "A triply infinite system of simple groups," *QJM*, v. 29, 1897, p. 169–178.
16. "Orthogonal group in a Galois field," *AMS Bull.*, v. 4, 1898, p. 196–200.

17. "Systems of simple groups derived from the orthogonal group," *AMS Bull.*, v. 4, 1898, p. 382-389.
18. "The structure of the hypoabelian groups," *AMS Bull.*, v. 4, 1898, p. 495-510.
19. "Concerning a linear homogeneous group in $C_{m,q}$ variables isomorphic to the general linear homogeneous group in m variables," *AMS Bull.*, v. 5, 1898, p. 120-135.
20. "A new solution of the cubic equation," *AMM*, v. 5, 1898, p. 38-39.
21. "The quadratic Cremona transformation," *Calif. Acad. Sci., Proc.*, s. 3, Math.-Phys. v. 1 1898, p. 13-23.
22. "The structure of certain linear groups with quadratic invariants," *LMS Proc.*, v. 30, 1898, p. 70-98.
23. "The first hypoabelian group generalized," *QJM*, v. 30, 1898, p. 1-16.
24. "Systems of simple groups derived from the orthogonal group," *Calif. Acad. Sci., Proc.*, s. 3, Math.-Phys., v. 1, 1898, p. 29-46; 1899, p. 47-57.
25. "The largest linear homogeneous group with an invariant Pfaffian," *AMS Bull.*, v. 5, 1899, p. 338-342.
26. "The known finite simple groups," *AMS Bull.*, v. 5, 1899, p. 470-475.
27. "Report on the recent progress in the theory of linear groups," *AMS Bull.*, v. 6, 1899, p. 13-27.
28. "Determination of the structure of all linear homogeneous groups in a Galois field which are defined by a quadratic invariant," *AJM*, v. 21, 1899, p. 193-256.
29. "A generalization of Fermat's theorem," *AM*, s. 2, v. 1, 1899, p. 31-36.
30. "The group of linear homogeneous substitutions on mq variables which is defined by the invariant $\phi \equiv \sum_{i=1}^m \xi_i \xi_2 \cdots \xi_{iq}$," *LMS Proc.*, v. 30, 1899, p. 200-208.
31. "Concerning the four known simple linear groups of order 25920, with an introduction to the hyperabelian linear groups," *LMS Proc.*, v. 31, 1899, p. 30-68.
32. "The abstract groups isomorphic with the symmetric group on k letters," *LMS Proc.*, v. 31, 1899, p. 351-353.
33. "Simplicity of the Abelian group on two pairs of indices in the Galois field of order $2^n, n > 1$," *QJM*, v. 30, 1899, p. 383-384.
34. "A class of linear groups including the Abelian group," *QJM*, v. 31, 1899, p. 60-66.
35. "The structure of the linear homogeneous groups defined by the invariant $\lambda_1 \xi_1^r + \lambda_2 \xi_2^r + \cdots + \lambda_m \xi_m^r$," *MA*, v. 52, 1899, p. 561-581.
36. "Sur une généralisation du théorème de Fermat," *CR Paris*, v. 128, 1899, p. 1083-1085.
37. "Sur plusieurs groupes linéaires isomorphes au groupe simple d'ordre 25920," *CR Paris*, v. 128, 1899, p. 873-875.
38. "Definition of the Abelian, the two hypoabelian, and related linear groups, as quotient-groups of the groups of isomorphisms of certain elementary groups," *AMS Trans.*, v. 1, 1900, p. 30-38.
39. "A new definition of the general Abelian linear group," *AMS Trans.*, v. 1, 1900, p. 91-96.
40. "Determination of an abstract simple group of order $2^7 \cdot 3^6 \cdot 5 \cdot 7$ holodrically isomorphic with a certain orthogonal group and with a certain hyperabelian group," *AMS Trans.*, v. 1, 1900, p. 353-370, 509.
41. "Proof of the existence of the Galois field of order p^r , for every integer r and prime number p ," *AMS Bull.*, v. 6, 1900, p. 203-204.
42. "Isomorphism between certain systems of simple linear groups," *AMS Bull.*, v. 6, 1900, p. 323-328.
43. "Certain subgroups of the Betti-Mathieu group," *AJM*, v. 22, 1900, p. 49-54.
44. "Canonical form of a linear homogeneous substitution in a Galois field," *AJM*, v. 22, 1900, p. 121-137.
45. "Concerning the cyclic subgroups of the simple group G of all linear fractional substitutions of determinant unity in two non-homogeneous variables with coefficients in an arbitrary Galois field," *AJM*, v. 22, 1900, p. 231-252.

46. "An abstract simple group of order 25920," *LMS Proc.*, v. 32, 1900, p. 3–10.
47. "Linear substitutions commutative with a given substitution," *LMS Proc.*, v. 32, 1900, p. 165–170.
48. "Proof of the non-isomorphism of the simple Abelian group on $2m$ indices and the simple orthogonal group on $2m+1$ indices, for $m>2$," *QJM*, v. 32, 1900, p. 42–63.
49. *Linear Groups with an Exposition of the Galois Field Theory*, Leipzig, 1901, x+312 p.
50. "Canonical forms of quaternary Abelian substitutions in an arbitrary Galois field," *AMS Trans.*, v. 2, 1901, p. 103–138.
51. "Theory of linear groups in an arbitrary field," *AMS Trans.*, v. 2, 1901, p. 363–394.
52. "Concerning real and complex continuous groups," *AMS Bull.*, v. 7, 1901, p. 340–350.
53. "The configurations of the 27 lines on a cubic surface and the 28 bitangents to a quartic curve," *AMS Bull.*, v. 8, 1901, p. 63–70.
54. "Distribution of the ternary linear homogeneous substitutions in a Galois field into complete sets of conjugate substitutions," *AJM*, v. 23, 1901, p. 37–40.
55. "Representation of linear groups as transitive substitution groups," *AJM*, v. 23, 1901, p. 337–377.
56. "On systems of isothermal curves," *AMM*, v. 8, 1901, p. 187–192.
57. "Concerning the Abelian and related linear groups," *LMS Proc.*, v. 33, 1901, p. 313–325.
58. "Linear groups in an infinite field," *LMS Proc.*, v. 34, 1901, p. 185–205.
59. "A class of groups in an arbitrary realm connected with the configuration of the 27 lines on a cubic surface," *QJM*, v. 33, 1901, p. 145–173.
60. "Théorie des groupes linéaires dans un domaine arbitraire de rationalité," *CR Paris*, v. 132, 1901, p. 1547–1548.
61. "The alternating group on eight letters and the quaternary linear congruence group modulo two," *MA*, v. 54, 1901, p. 564–569.
62. "The known systems of simple groups and their inter-isomorphisms," *Intern. Congress Mathems.*, Paris, 1902, p. 225–229.
63. "The groups of Steiner in problems of contact," *AMS Trans.*, v. 3, 1902, p. 38–45.
64. "On the group defined for any given field by the multiplication table of any given finite group," *AMS Trans.*, v. 3, 1902, p. 285–301.
65. "The groups of Steiner in problems of contact," (second paper), *AMS Trans.*, v. 3, 1902, p. 377–382.
66. "A class of simply transitive linear groups," *AMS Bull.*, v. 8, 1902, p. 394–401.
67. "Cyclic subgroups of the simple ternary linear fractional group in a Galois field," *AJM*, v. 24, 1902, p. 1–12.
68. "Canonical form of a linear homogeneous transformation in an arbitrary realm of rationality," *AJM*, v. 24, 1902, p. 101–108.
69. "Geometrical derivation of certain trigonometric formulae," *AMM*, v. 9, 1902, p. 36–37.
70. "Factors of a certain determinant of order six," *AMM*, v. 9, 1902, p. 66–68.
71. "The order of a certain senary linear group," *AMM*, v. 9, 1902, p. 149–152.
72. "A matrix defined by the quaternion group," *AMM*, v. 9, 1902, p. 243–248.
73. "An elementary exposition of Frobenius's theory of group-characters and group-determinants," *AM*, s. 2, v. 4, 1902, p. 25–49.
74. "On the groups defined for an arbitrary field by the multiplication tables of certain finite groups," *LMS Proc.*, v. 35, 1902, p. 68–80.
75. "The abstract group simply isomorphic with the group of linear fractional transformations in a Galois field," *LMS Proc.*, v. 35, 1902, p. 292–305.
76. "Generational relations of an abstract simple group of order 4080," *LMS Proc.*, v. 35, 1902, p. 306–319.
77. "Theorems on the residues of multinomial coefficients with respect to a prime modulus," *QJM*, v. 33, 1902, p. 378–384.
78. "The hyperorthogonal groups," *MA*, v. 55, 1902, p. 521–572.
79. "Ternary orthogonal group in a general field," *U. Chicago Decennial Pub.*, v. 9, 1902, p. 27–34.

80. "Groups defined for a general field by the rotation groups," *U. Chicago Decennial Pub.*, v. 9, 1902, p. 35–51.
- 80A. *College Algebra*, New York, 1902, vi+214 p. *Answers*, New York, 1904, 14 p.
81. *Introduction to the Theory of Algebraic Equations*, New York, 1903, v+104 p.
82. "Definitions of a field by independent postulates," *AMS Trans.*, v. 4, 1903, p. 13–20.
83. "Definitions of a linear associative algebra by independent postulates," *AMS Trans.*, v. 4, 1903, p. 21–26.
84. "On the subgroups of order a power of p in the quaternary Abelian group in the Galois field of order p^n ," *AMS Trans.*, v. 4, 1903, p. 371–386.
85. "On the reducibility of linear groups," *AMS Trans.*, v. 4, 1903, p. 434–436.
86. "Three sets of generational relations defining the abstract simple group of order 504," *AMS Bull.*, v. 9, 1903, p. 194–204.
87. "Generational relations defining the abstract simple group of order 660," *AMS Bull.*, v. 9, 1903, p. 204–206.
88. "The abstract group G simply isomorphic with the alternating group on six letters," *AMS Bull.*, v. 9, 1903, p. 303–306.
89. "Fields whose elements are linear differential expressions," *AMS Bull.*, v. 10, 1903, p. 30–31.
90. "Three algebraic notes," *AMM*, v. 10, 1903, p. 219–226.
91. "A generalization of symmetric and skew-symmetric determinants," *AMM*, v. 10, 1903, p. 253–256.
92. "Generational relations for the abstract group simply isomorphic with the linear fractional group in the $GF\ 2^n$," *LMS Proc.*, v. 35, 1903, p. 443–454.
93. "Addition to the paper on the four known simple groups of order 25920," *LMS Proc.*, s. 2, v. 1, 1903, p. 283–284.
94. "The subgroups of order a power of 2 of the simple quinary orthogonal group in the Galois field of order $p^n=8l+3$," *AMS Trans.*, v. 5, 1904, p. 1–38.
95. "Determination of all the subgroups of the known simple group of order 25920," *AMS Trans.*, v. 5, 1904, p. 126–166.
96. "Two systems of subgroups of the quaternary Abelian group in a general Galois field," *AMS Bull.*, v. 10, 1904, p. 178–184.
97. "On the subgroups of order a power of p in the linear homogeneous and fractional groups in the $GF\ p^n$," *AMS Bull.*, v. 10, 1904, p. 385–397.
98. "Memoir on Abelian transformations," *AJM*, v. 26, 1904, p. 243–318.
99. "A property of the group $G_2^{2^n}$ all of whose operators except identity are of period 2," *AMM*, v. 11, 1904, p. 203–206.
100. "Determination of all groups of binary linear substitutions with integral coefficients taken modulo 3 and of determinant unity," *AM*, s. 2, v. 5, 1904, p. 140–144.
101. "Application of groups to a complex problem in arrangements," *AM*, s. 2, v. 6, 1904, p. 31–44.
102. "A new extension of Dirichlet's theorem on prime numbers," *MM*, v. 33, 1904, p. 155–161.
103. "On the minimum degree of resolvents for the p -section of the periods of hyperelliptic functions of four periods," *DMV Jahr.*, v. 13, 1904, p. 559–560.
104. "The minimum degree τ of resolvents for the p -section of the periods of hyperelliptic functions of four periods," *AMS Trans.*, v. 6, 1905, p. 48–57.
105. "Definitions of a group and a field by independent postulates," *AMS Trans.*, v. 6, 1905, p. 198–204.
106. "On semi-groups and the general isomorphism between infinite groups," *AMS Trans.*, v. 6, 1905, p. 205–208.
107. "On hypercomplex number systems," *AMS Trans.*, v. 6, 1905, p. 344–348.
108. "The group of a tactical configuration," *AMS Bull.*, v. 11, 1905, p. 177–179.
109. "On the class of the substitutions of various linear groups," *AMS Bull.*, v. 11, 1905, p. 426–432.

110. "A general theorem on algebraic numbers," *AMS Bull.*, v. 11, 1905, p. 482-486.
111. "Determination of the ternary modular groups," *AJM*, v. 27, 1905, p. 189-202.
112. "Subgroups of order a power of p in the general and special m -ary linear homogeneous groups in the $GF p^n$," *AJM*, v. 27, 1905, p. 280-302.
113. "On the cyclotomic function," *AMM*, v. 12, 1905, p. 86-89.
114. "Graphical methods in trigonometry," *AMM*, v. 12, 1905, p. 129-133.
115. "Expressions for the elements of a determinant in terms of the minors of a given order. Generalization of a theorem due to Studnicka," *AMM*, v. 12, 1905, p. 217-221.
116. "On the real elements of certain classes of geometrical configurations," *AM*, s. 2, v. 6, 1905, p. 141-150.
117. "Determination of all the subgroups of the three highest powers of p in the group G of all m -ary linear homogeneous transformations modulo p ," *QJM*, v. 36, 1905, p. 373-384.
118. "A new system of simple groups," *MA*, v. 60, 1905, p. 137-150.
119. "On finite algebras," *GN*, 1905, p. 358-393.
120. "On quadratic, Hermitian and bilinear forms," *AMS Trans.*, v. 7, 1906, p. 275-292.
121. "Linear algebras in which division is always uniquely possible," *AMS Trans.*, v. 7, 1906, p. 370-390.
122. "On commutative linear algebras in which division is always uniquely possible," *AMS Trans.*, v. 7, 1906, p. 514-522.
123. "Criteria for the irreducibility of functions in a finite field," *AMS Bull.*, v. 13, 1906, p. 1-8.
124. "On the theory of equations in a modular field," *AMS Bull.*, v. 13, 1906, p. 8-10.
125. "On the quaternary linear homogeneous groups modulo p of order a multiple of p ," *AJM*, v. 28, 1906, p. 1-16.
126. "On linear algebras," *AMM*, v. 13, 1906, p. 201-205.
127. "The abstract form of the special linear homogeneous group in an arbitrary field," *QJM*, v. 38, 1907, p. 141-145.
128. "The abstract form of the Abelian linear groups," *QJM*, v. 38, 1907, p. 145-157.
129. "Invariants of binary forms under modular transformations," *AMS Trans.*, v. 8, 1907, p. 205-232.
130. "Modular theory of group-matrices," *AMS Trans.*, v. 8, 1907, p. 389-398.
131. "Algebraic numbers and forms," *AMS Bull.*, v. 13, 1907, p. 348-362.
132. "The symmetric group on eight letters and the senary first hypoabelian group," *AMS Bull.*, v. 13, 1907, p. 386-389.
133. "Modular theory of group characters," *AMS Bull.*, v. 13, 1907, p. 477-488.
134. "On quadratic forms in a general field," *AMS Bull.*, v. 14, 1907, p. 108-115.
135. "Note on the volume of a tetrahedron in terms of the coordinates of the vertices," *AMM*, v. 14, 1907, p. 117-118.
136. "Invariants of the general quadratic form modulo 2," *LMS Proc.*, s. 2, v. 5, 1907, p. 301-324.
137. "Representations of the general symmetric group as linear groups in finite and infinite fields," *AMS Trans.*, v. 9, 1908, p. 121-148.
138. "On triple algebras and ternary cubic forms," *AMS Bull.*, v. 14, 1908, p. 160-169.
139. "On higher congruences and modular invariants," *AMS Bull.*, v. 14, 1908, p. 313-318.
140. "Criteria for the irreducibility of a reciprocal equation," *AMS Bull.*, v. 14, 1908, p. 426-430.
141. "On the canonical forms and automorphs of ternary cubic forms," *AJM*, v. 30, 1908, p. 117-128.
142. "Invariantive reduction of quadratic forms in the $GF 2^n$," *AJM*, v. 30, 1908, p. 263-281.
143. "The Galois group of a reciprocal quartic equation," *AMM*, v. 15, 1908, p. 71-78.
144. "On the factorization of large numbers," *AMM*, v. 15, 1908, p. 217-222.
145. Second paper with title: "A class of groups in an arbitrary realm connected with the configuration of the 27 lines on a cubic surface," *QJM*, v. 39, 1908, p. 205-209.
146. "On families of quadratic forms in a general field," *QJM*, v. 39, 1908, p. 316-333.

147. "On the last theorem of Fermat" (second paper), *QJM*, v. 40, 1908, p. 27-45.
148. "On the congruence $x^n+y^n+z^n\equiv 0 \pmod{p}$," *Crelle's J.*, v. 135, 1908, p. 134-141.
149. "On the last theorem of Fermat," *MM*, v. 38, 1908, p. 14-32.
150. "Definite forms in a finite field," *AMS Trans.*, v. 10, 1909, p. 109-122.
151. "General theory of modular invariants," *AMS Trans.*, v. 10, 1909, p. 123-158.
152. "Equivalence of pairs of bilinear or quadratic forms under rational transformation," *AMS Trans.*, v. 10, 1909, p. 347-360.
153. "On the representation of numbers by modular forms," *AMS Bull.*, v. 15, 1909, p. 338-347.
154. "Rational reduction of a pair of binary quadratic forms; their modular invariants," *AJM*, v. 31, 1909, p. 103-146.
155. "A theory of invariants," *AJM*, v. 31, 1909, p. 337-354.
156. "On the representation of numbers as the sum of two squares," (with M. Kaba) *AMM*, v. 16, 1909, p. 85-87.
157. "Rational edged cuboids with equal volumes and equal surfaces," *AMM*, v. 16, 1909 p. 107-114.
158. "Modular invariants of a general system of linear forms," *LMS Proc.*, s. 2, v. 7, 1909, p. 430-444.
159. "On commutative linear groups," *QJM*, v. 40, 1909, p. 167-196.
160. "Combinants," *QJM*, v. 40, 1909, p. 349-366.
161. "Lower limit for the number of sets of solutions of $x^e+y^e+z^e\equiv 0 \pmod{p}$," *Creele's J.*, v. 135, 1909, p. 181-188.
162. "On certain Diophantine equations," *MM*, v. 39, 1909-10, p. 86-87.
163. "On the factorization of integral functions with p -adic coefficients," *AMS Bull.*, v. 17, 1910, p. 19-23.
164. "On the negative discriminants for which there is a single class of positive primitive binary quadratic forms," *AMS Bull.*, v. 17, 1911, p. 534-537.
165. "Constructions with ruler and compasses; regular polygons," J. W. A. Young, *Monographs on Topics of Modern Math.* . . . , New York, 1911, p. 351-386.
166. "An invariantive investigation of irreducible binary modular forms," *AMS Trans.*, v. 12, 1911, p. 1-18.
167. "A fundamental system of invariants of the general modular linear group with a solution of the form problem," *AMS Trans.*, v. 12, 1911, p. 75-98.
168. "Binary modular groups and their invariants," *AJM*, v. 33, 1911, p. 175-192.
169. "Notes on the theory of numbers," *AMM*, v. 18, 1911, p. 109-111.
170. "Note on cubic equations and congruences," *AM*, s. 2, v. 12, 1911, p. 149-152.
171. "Note on modular invariants," *QJM*, v. 42, 1911, p. 158-161.
172. "On non-vanishing forms," *QJM*, v. 42, 1911, p. 162-171.
173. "Linear algebras," *AMS Trans.*, v. 13, 1912, p. 59-73.
174. "Proof of the finiteness of modular covariants," *AMS Trans.*, v. 14, 1913, p. 299-310.
175. "On binary modular groups and their invariants," *AMS Bull.*, v. 20, 1913, p. 132-134.
176. "Finiteness of the odd perfect and primitive abundant numbers with n distinct prime factors," *AJM*, v. 35, 1913, p. 413-422.
177. "Even abundant numbers," *AJM*, v. 35, 1913, p. 423-426.
178. "Amicable number triples," *AMM*, v. 20, 1913, p. 84-92.
179. "On the rank of a symmetrical matrix," *AM*, s. 2, v. 15, 1913, p. 27-28.
180. "Theorems and tables on the sum of the divisors of a number," *QJM*, v. 44, 1913, p. 264-296.
181. *Algebraic Invariants*, New York, 1914, x+100 p.
182. *Linear Algebras*, Cambridge, 1914, viii+73 p.
183. *On Invariants and the Theory of Numbers* (*AMS Colloq. Pub.*), 1914, vi+110 p.

184. "Linear associative algebras and Abelian equations," *AMS Trans.*, v. 15, 1914, p. 31-46.
185. "Invariants in the theory of numbers," *AMS Trans.*, v. 15, 1914, p. 497-503.
186. "On the trisection of an angle and the construction of regular polygons of 7 and 9 sides," *AMM*, v. 21, 1914, p. 259-262.
187. "The invariants, seminvariants and linear covariants of the binary quartic form modulo 2," *AM*, s. 2, v. 15, 1914, p. 114-117.
188. "The points of inflexion of a plane cubic curve," *AM*, s. 2, v. 16, 1914, p. 50-66.
189. "Modular invariants of the system of a binary cubic, quadratic, and linear form," *QJM*, v. 45, 1914, p. 373-384.
190. *Elementary Theory of Equations*, New York, 1914, v+184 p.
191. "Projective classification of cubic surfaces, modulo 2," *AM*, s. 2, v. 16, 1915, p. 139-157.
192. "Quartic curves modulo 2," *AMS Trans.*, v. 16, 1915, p. 111-120.
193. "Invariants, seminvariants, and covariants of the ternary and quaternary quadratic form modulo 2," *AMS Bull.*, v. 21, 1915, p. 174-179.
194. "On the relation between linear algebras and continuous groups," *AMS Bull.*, v. 22, 1915, p. 53-61.
195. "Invariantive theory of plane cubic curves modulo 2," *AJM*, v. 37, 1915, p. 107-116.
196. "Geometrical and invariantive theory of quartic curves modulo 2," *AJM*, v. 37, 1915, p. 337-354.
197. "Invariantive classification of pairs of conics modulo 2," *AJM*, v. 37, 1915, p. 355-358.
198. "Classification of quartic curves modulo 2," *MM*, v. 44, 1915, p. 189-192.
199. "Recent progress in the theories of modular and formal invariants and in modular geometry," *NAS Proc.*, v. 1, 1915, p. 1-4.
200. "The straight lines on modular cubic surfaces," *NAS Proc.*, v. 1, 1915, p. 248-253.
201. *Theory and Applications of Finite Groups* (with Miller and Blichfeldt), New York, 1916, xvii+390 p. Reprinted with corrections, New York, 1938.
202. "An extension of the theory of numbers by means of correspondences between fields," *AMS Bull.*, v. 23, 1916, p. 109-111.
203. "Fermat's last theorem and the origin and nature of algebraic numbers," *AM*, s. 2, v. 18, 1917, p. 161-187.
204. *History of the Theory of Numbers* (Carnegie Institution): v. 1, *Divisibility and Primality*, 1919, xii+486 p.; v. 2, *Diophantine Analysis*, 1920, xxv+803 p.; v. 3, *Quadratic and Higher Forms*; 1923, v+313 p. Facsimile reprint, reduced size of page, New York, G. E. Stechert and Co., 3 v., 1934.
205. "On quaternions and their generalization and the history of the eight square theorem," *AM*, s. 2, v. 20, 1919, p. 155-171.
206. "Mathematics in war perspective," *AMS Bull.*, v. 25, 1919, p. 289-311. AMS ret. P add. 27 Dec. 1918.
207. "Applications of the geometry of numbers to algebraic numbers," *AMS Bull.*, v. 25, 1919, p. 453-455.
208. "Les polynomes égaux à des déterminants," *CR Paris*, v. 171, 1920, p. 1360-1362.
209. "Some relations between the theory of numbers and other branches of mathematics," *Intern. Congress Mathems.*, Strasbourg, 1921, p. 41-56.
210. "Homogeneous polynomials with a multiplication theorem," *Intern. Congress Mathems.*, Strasbourg, 1921, p. 215-230.
211. "Determination of all general homogeneous polynomials expressible as determinants with linear elements," *AMS Trans.*, v. 22, 1921, p. 167-179.
212. "Fallacies and misconceptions in Diophantine analysis," *AMS Bull.*, v. 27, 1921, p. 312-319.
213. "A new method in Diophantine analysis," *AMS Bull.*, v. 27, 1921, p. 353-365.

214. "Algebraic theory of the expressibility of cubic forms as determinants, with application to Diophantine analysis," *AJM*, v. 43, 1921, p. 102-125.
215. "Rational triangles and quadrilaterals," *AMM*, v. 28, 1921, p. 244-250.
216. "Reducible cubic forms expressible rationally as determinants," *AM*, s. 2, v. 23, 1921, p. 70-74.
217. "A fundamental system of covariants of the ternary cubic form," *AM*, s. 2, v. 23, 1921, p. 78-82.
218. "Arithmetic of quaternions," *LMS Proc.*, v. 20, 1921, p. 225-232.
219. "La composition des polynomes," *CR Paris*, v. 172, 1921, p. 636-640.
220. "Quaternions and their generalizations," *NAS Proc.*, v. 7, 1921, p. 109-114.
221. "Perfect and amicable numbers," *Scientific Mo.*, v. 12, 1921, p. 349-354.
222. "Why it is impossible to trisect an angle or to construct a regular polygon of seven or nine sides by ruler and compasses," *MT*, v. 14, 1921, p. 217-223.
223. "Progrès recents dans la théorie de nombres," *Sphinx (Edipe)*, v. 16, 1921, 32 p. suppl. (according to index of the periodical).
224. *Plane Trigonometry with Practical Applications*, Chicago, 1922, xi+176+35 p.
225. *First Course in the Theory of Equations*, New York, 1922, vi+168 p.
226. "Impossibility of restoring unique factorization in a hypercomplex arithmetic," *AMS Bull.*, v. 28, 1922, p. 438-442.
227. "The theory of numbers: its principal branches," *Scientia*, 1922, p. 421-430.
228. *Report of Committee on Algebraic Numbers* (NRC, with Vandiver, etc.), 1923, 96 p.
229. *Algebras and Their Arithmetics*, Chicago, U. Chicago Press, 1923, xiii+241 p. Reprinted, New York, Stechert, 1938. See also no. 253.
230. "Integral solutions of $x^2 - my^2 = zw$," *AMS Bull.*, v. 29, 1923, p. 464-467.
231. "The rational linear algebras of maximum and minimum ranks," *LMS Proc.*, v. 22, 1923, p. 145-162.
232. "A new simple theory of hypercomplex integers," *Journ. d. Mathém.*, s. 9, v. 2, 1923, p. 281-326.
233. "Algebras and their arithmetics," *AMS Bull.*, v. 30, 1924, p. 247-257.
234. "Quadratic fields in which factorization is always unique," *AMS Bull.*, v. 30, 1924, p. 328-334.
235. "On the theory of numbers and generalized quaternions," *AJM*, v. 46, 1924, p. 1-16.
236. "Differential equations from the group standpoint," *AM*, s. 2, v. 25, 1924, p. 287-378.
237. "Resolvent sextics of quintic equations," *AMS Bull.*, v. 31, 1925, p. 515-523.
238. "Algèbres nouvelles de division," *CR Paris*, v. 181, 1925, p. 836-838.
239. *Modern Algebraic Theories*, Chicago, 1926, ix+276 p.
German trans.: *Höhere Algebra*, Leipzig, 1929, vii+242 p.
240. "New division algebras," *AMS Trans.*, v. 28, 1926, p. 207-234.
241. "All integral solutions of $ax^2 + bxy + cy^2 = w_1 w_2 \cdots w_n$," *AMS Bull.*, v. 32, 1926, p. 644-648.
242. "Quadratic forms which represent all integers," *NAS Proc.*, v. 12, 1926, p. 756-757.
243. "Singular case of pairs of bilinear, quadratic, or Hermitian forms," *AMS Trans.*, v. 29, 1927, p. 239-253.
244. "Integers represented by a positive ternary quadratic form," *AMS Bull.*, v. 33, 1927, p. 63-70.
245. "A generalization of Waring's theorem on nine cubes," *AMS Bull.*, v. 33, 1927, p. 299-300.
246. "Extensions of Waring's theorem on fourth powers," *AMS Bull.*, v. 33, 1927, p. 319-327.
247. "All positive integers are sums of values of a quadratic function of x ," *AMS Bull.*, v. 33, 1927, p. 713-720.
248. "Quaternary quadratic forms representing all integers," *AJM*, v. 49, 1927, p. 39-56.

249. "Generalizations of Waring's theorem on fourth, sixth, and eighth powers," *AJM*, v. 49, 1927, p. 241-250.
250. "Extensions of Waring's theorem on nine cubes," *AMM*, v. 34, 1927, p. 177-183.
251. "Ternary quadratic forms and congruences," *AM*, s. 2, v. 28, 1927, p. 333-341.
252. "Recent light on classic problems in the theory of numbers," *APS Proc.*, v. 66, 1927, p. 281-286.
253. *Algebren und ihre Zahlentheorie. Mit einem Kapitel [p. 270-303] über Idealtheorie* von Andreas Speiser, Zürich, 1927, viii+308+1 p. "Berichtigungen." This work is a trans. of a new English manuscript by Dickson and differs in many important ways from no. 229 above.
254. "Simpler proofs of Waring's theorem on cubes, with various generalizations," *AMS Trans.*, v. 30, 1928, p. 1-18.
255. "Generalizations of the theorem of Fermat and Cauchy on polygonal numbers," *AMS Bull.*, v. 34, 1928, p. 63-72.
256. "Extended polygonal numbers," *AMS Bull.*, v. 34, 1928, p. 205-217.
257. "New division algebras," *AMS Bull.*, v. 34, 1928, p. 555-560.
258. "Additive number theory for all quadratic functions," *AJM*, v. 50, 1928, p. 1-48.
259. "Quadratic functions or forms, sums of whose values give all positive integers," *Journ. d. Mathém.*, s. 9, v. 7, 1928, p. 319-336.
260. "Further development of the theory of arithmetics of algebras," *Intern. Congress Mathems.*, Toronto, 1928, p. 173-184.
261. "Outline of the theory to date of the arithmetics of algebras," *Intern. Congress Mathems.*, Toronto, 1928, p. 95-102.
262. "A new theory of linear transformations and pairs of bilinear forms," *Intern. Congress Mathems.*, Toronto, 1928, p. 361-363.
263. *Introduction to the Theory of Numbers*, Chicago, 1929, viii+183 p.
- German trans. by Bodwiz: *Einführung in die Zahlentheorie*, Leipzig, 1931, viii+175 p.
264. "Universal quadratic forms," *AMS Trans.*, v. 31, 1929, p. 164-189.
265. "The forms $ax^2+by^2+cz^2$ which represent all integers," *AMS Bull.*, v. 35, 1929, p. 55-59.
266. *Studies in the Theory of Numbers*, Chicago, 1930, x+230 p.
267. "Construction of division algebras," *AMS Trans.*, v. 32, 1930, p. 319-334.
268. "Proof of a Waring theorem on fifth powers," *AMS Bull.*, v. 37, 1931, p. 549-553.
269. *Minimum Decompositions into Fifth Powers* (BAAS, *Math. Tables, III*), 1933, vi+400 p.
270. "Recent progress on Waring's theorem and its generalizations," *AMS Bull.*, v. 39, 1933, p. 701-727.
271. "Minimum decomposition into n -th powers," *AJM*, v. 55, 1933, p. 593-602.
272. "Waring's problem for cubic functions," *AMS Trans.*, v. 36, 1934, p. 1-12.
273. "A new method for Waring theorems with polynomial summands," *AMS Trans.*, v. 36, 1934, p. 731-748.
274. "Waring's problem for ninth powers," *AMS Bull.*, v. 40, 1934, p. 487-493.
275. "The converse of Waring's problem," *AMS Bull.*, v. 40, 1934, p. 711-714.
276. "Two-fold generalizations of Cauchy's lemma," *AJM*, v. 56, 1934, p. 513-528.
277. "Polygonal numbers and related Waring problems," *QJMO*, v. 5, 1934, p. 283-290.
278. "Universal Waring theorem for eleventh powers," *LMS Journ.*, v. 9, 1934, p. 201-206.
279. *Researches on Waring's Problem*, Carnegie Institution, Wash., 1935, v+257 p.
280. "Cyclotomy and trinomial congruences," *AMS Trans.*, v. 37, 1935, p. 363-380.
281. "Cyclotomy when e is composite," *AMS Trans.*, v. 38, 1935, p. 187-200.
282. "Congruences involving only e -th powers," *Acta Arith.* v. 1, 1935, p. 161-167.
283. "Linear algebras with associativity not assumed," *DMJ*, v. 1, 1935, p. 113-125.
284. "Cyclotomy, higher congruences, and Waring's problem," *AJM*, v. 57, 1935, p. 391-424.
285. "A new method for Waring theorems with polynomial summands, II," *AMS Trans.*, v. 39, 1936, p. 205-208.

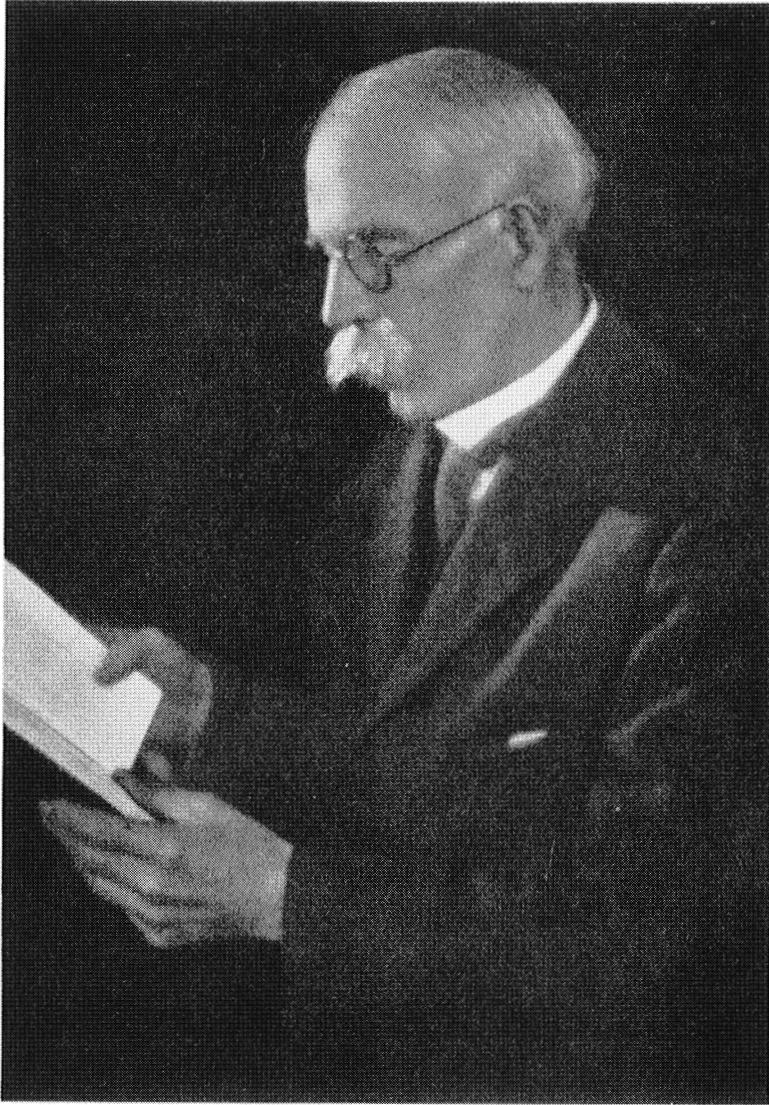
286. "A generalization of Waring's problem," *AMS Bull.*, v. 42, 1936, p. 525-529.
 287. "The Waring problem and its generalizations," *AMS Bull.*, v. 42, 1936, p. 833-842.
 288. "Waring theorems of new type," *AJM*, v. 58, 1936, p. 241-248.
 289. "Proof of the ideal Waring theorem for exponents 7-180," *AJM*, v. 58, 1936, p. 521-529.
 290. "Solution of Waring's problem," *AJM*, v. 58, 1936, p. 530-535.
 291. "On Waring's problem and its generalization," *AM*, s. 2, v. 37, 1936, p. 293-316.
 292. "Universal Waring theorems with cubic summands," *Acta Arith.*, v. 2, 1936, p. 184-196.
 293. "The ideal Waring theorem for twelfth powers," *DMJ*, v. 2, 1936, p. 192-204.
 294. "Universal Waring theorems," *MMP*, v. 43, 1936, p. 391-400.
 295. "Biographical memoir of Eliakim Hastings Moore, 1862-1932" (with G. A. Bliss), *NAS Biog. Mem.*, v. 17, 1936, p. 83-102.
 296. "Herbert Ellsworth Slaught" (with G. A. Bliss), *Science*, v. 86, 1937, p. 72-73.
 297. "New Waring theorems for polygonal numbers," *QJMO*, v. 8, 1937, p. 62-65.
 298. "Universal forms $\sum a_i x_i^n$ and Waring's problem," *Acta Arith.*, v. 2, 1937, p. 177-196.
 299. Reviews of books by Page, Cahen, Dedekind, Bachmann, Zindler, Bauer, Burkhardt, de Séguier, Cajori, Tannery, König, Galois, Minkowski, Sylvester, Hensel, Bell, in *AMS Bull.*, 1899-1928.

15. FRANK MORLEY

CURRICULUM VITAE.—B. Woodbridge, Suffolk, Eng. 9 Sept. 1860; d. Baltimore, Md. 17 Oct. 1937. At King's C., Cambridge (79-84; A.B. 84, A.M. 87). Math. master Bath C. (84-87). Instr. Haverford C., Pa. (87-88; prof. 88-00, leave of absence during 97-98, spent in England at Cambridge U. (Sc.D. 98); prof. JHU (00-28; prof. emeritus 28-37).

HONORS.—Ed. *AMS Bull.*, 95-98, Oct. 99-02. Mem. Amer. Phil. So. 97. Cooperating ed. *AJM*, July 99-00, Apr. 30-36; ed. 01-21; joint ed. 22-Jan. 30. VP AMS 02. Mem. Advisory Comm. on Math. to Carnegie Institution (with E. H. Moore chm.; and O. Stone) 02. Starred *Amer. Men Sci.* 06. Research assist., or Assoc., Carnegie Institution 09-36; except for a few years. Fellow AAAS 17. P AMS 19-20. Portrait painted by T. C. Corner of Baltimore, presented to JHU and placed in the Library 26; reproduction in *JH Alumni Mag.*, v. 14, 1926, opp. p. 513, and in *AJM*, v. 60, frontispiece, 1938.

BIOGRAPHICAL NOTES.—Prof. Morley was a son of Quaker parents Joseph R. and Elizabeth (Muskett) Morley of Suffolk, Eng. Having won an open scholarship and prize he went into residence at King's C., Cambridge, in 1879, but his university career was sorely hampered by illness. He did not graduate until a year later than the normal date, eighth in the list when G. B. Mathews was senior wrangler and A. N. Whitehead fourth. "Ill health beyond all doubt had prevented him from doing himself justice, but the disappointment was keen. In middle life he was loth to speak of his student days, yet the friendships then formed with Lowes Dickinson and others were lasting." (Richmond). After settling in the U. S., hardships of his earlier years were behind him, his health was no longer a cause for anxiety, and since he had an assured position he married an English lady of Sussex. The twelve years at the Quaker college in Haverford were years of great happiness during which his powers and reputation steadily increased. More than a score of papers, and two books date from this period. His closest mathematical associations were with two Cambridge professors at the neighbouring college of Bryn Mawr, Charlotte Scott of Girton C., one of the foremost of the younger geometers, and James



Frank Morley

1916

Harkness¹ of Trinity C., who collaborated with him in his first book, *A Treatise on the Theory of Functions* (no. 15), reissued six years later in a shorter and much improved form as an *Introduction to the Theory of Analytic Functions* (no. 27); even today this work is a classic.

Of these treatises there were admirable reviews by Maschke (*NYMS Bull.*, v. 3), and Bolza (*AMS Bull.*, v. 6). Maschke wrote of the first that it "rendered the theory of functions accessible to everyone who wishes to acquire a thorough knowledge of the subject" and that "the great merits of this valuable work will secure it a high rank in modern mathematical literature." Of the *Introduction* Bolza pointed out that the title conveys an inadequate idea of its scope and object; it may be shortly described as a very complete treatise on Weierstrass's general theory of functions with applications to elliptic and algebraic functions, preceded by an introduction devoted to the number concept and the geometric interpretation of complex quantities, and followed by a short account of some of the leading ideas of Riemann and Cauchy. Bolza closes his review as follows: "Thus the authors have succeeded in producing not only a work of high scientific and pedagogical value but at the same time of a singular beauty and elegance. But there are numerous beauties of detail as well, for which, however, the reader must be referred to the book itself. A certain freshness and originality pervade the whole, even in places where the authors follow along beaten tracks, and give at every turn evidence of the complete mastery of the subject with which the book is written."

For comments on some of his papers we follow Prof. Coble. He tells us that Prof. White thought most highly of the one on geometry whose element is the 3-point of a plane (no. 40) but that his own favorite was the brief article on the Lüroth quartic curve (no. 50), a penetrating geometric analysis of kaleidoscopic character which eventually yields an algebraic result quite unattainable by conventional methods. His chief contribution to algebra was in the discussion of the eliminant of a net of curves (nos. 58, 62). The delightful retiring presidential address on "Pleasant questions and wonderful effects" (no. 52) reflected the invigorating spirit of a great man and a great teacher. He went to the JHU when graduate work in mathematics so brilliantly initiated by Sylvester had commenced to decline, and soon made it an inspiring intellectual center, which drew many students. He lectured several times a week to all students in the department, stimulating the entire group by his unusual gift in the application of advanced ideas to elementary topics by striking translation of the abstract into the concrete, the whole pervaded with refreshing humor.

¹ In his reminiscences Morley wrote of Harkness as follows: "A man of wide accurate and available information, remarkable in any case and astonishing in an Englishman of that time. Knew not only the pure mathematics as it then stood but much history and much worthwhile pure literature. And he brought out quotations apt to the occasion, usually with a chuckle. The élite of the men of Bryn Mawr ran to his rooms in cottage no. 2, at the hour of afternoon tea, Tom Morgan leading. Henry Crew and I at Haverford College a mile away joined up."

Many of Prof. Morley's ideas were also developed during 1900–31 by the following 49 students who carried on their work for the doctor's degree, at Haverford C. and JHU under his direction: F. H. Loud (at Haverford), I. E. Rabinovitch (name later changed to Marshall), A. B. Coble, H. A. Converse, C. E. Brooks, W. B. Carver, J. G. Hun, C. C. Grove, H. B. Phillips, R. P. Stephens, J. F. Messick, C. S. Atchison, A. E. Landry, E. C. F. Phillips, J. R. Conner, D. D. Leib, H. I. Thomsen, J. E. Hodgson, J. E. Rowe, T. B. Ashcraft, M. Clara L. Bacon, J. I. Tracey, R. M. Winger, H. Bateman, Florence P. Lewis, L. E. Wear, J. W. Gain, H. C. Gossard, Mabel M. Young, C. H. Rawlins, Jr., A. W. Hobbs, Teresa Cohen, Flora D. Sutton, G. H. Collignon, F. J. Gerst, Anna M. Whelan, J. B. Linker, L. T. Moore, B. C. Patterson, Martha H. Barton, P. S. Wagner, L. M. Blumenthal, A. S. Winsor, J. W. Peters, A. W. Richeson, Mildred W. Dean, W. K. Morrill, C. A. Spicer, H. A. Robinson. Coble tells us that with Morley "it was a cardinal point to have on hand a sufficient variety of thesis problems to accommodate particular tastes and capacities. Many promising ideas which occurred to him were laid aside for student use. He followed the development of each one of his students with great solicitude and felt fully rewarded when some evidence of independent thinking appeared."

Many of Prof. Morley's discoveries are also contained in more than three scores of problems proposed for solution in the *Ed. Times* (Bibl. no. 1) from the time that he was an undergraduate on for nearly fifty years. Most of the problems are geometrical; three of them are as follows: 8340: Show that on a chess-board the number of squares visible is 204, and the number of rectangles (including squares) visible is 1296; and that, on a similar board with n squares in each side, the number of squares is the sum of the first n square numbers, and the number of rectangles (including squares) is the sum of the first n cube numbers.

10034: Prove that, of the four focal circles of a circular cubic or bicircular quartic, any two are orthogonal, and the radii are connected by the relation $\sum(\mu - 2) = 0$.

10562: Let there be three parallel rectilinear vortices in an infinite mass of fluid. Let a cross section meet the vortices at ABC . Prove that (1) the motion of any vortex A is at right angles to AK , where K is the symmedian point; and (2) the particles at foci of the maximum ellipse inscribed in ABC are instantaneously at rest.

By about 1900 the following result due to Prof. Morley was well known to Cambridge mathematicians and others: "If the angles of any triangle be trisected, the triangle, formed by the meets of pairs of trisectors, each pair being adjacent to the same side, is equilateral." The first published reference to it as "Morley's theorem,"¹ a term now in general use,

¹ See also *P. Mat.*, s. 4, v. 1, 1921, p. 240–290. *L'Enseignement Mathém.*, v. 22, 1922, p. 344. *Math. Gazette*, v. 11, 1922, p. 85, 164, 171, 310; v. 12, 1925, p. 391; v. 17, 1933, p. 126–268, and v. 22, 1938, p. 50–57, an art. entitled "Morley's triangle." *LMS Proc.*, s. 2, v. 31, 1930, p. 364. *DB*, v. 72, 1937, p. 360.

seems to have been in a paper by F. G. Taylor and W. L. Marr (*EMS Proc.*, v. 32, 1914, p. 119). This was followed by papers of Taylor, "The relation of Morley's theorem to the Hessian axis and circumcentre" (p. 132-135); and Marr, "Morley's trisection theorem: an extension and its relation to the circles of Apollonius" (p. 136-150). Morley's first personal published reference to the theorem was ten years later (no. 56), when he told the manner of its discovery. He found that if a variable cardioid touch the sides of a triangle the locus of its center, that is, the center of the circle on which the equal circles roll, is a set of 9 lines which are three by three parallel, the directions being those of the sides of an equilateral triangle. The meets of these lines correspond to double tangents; they are also the meets of certain pairs of trisectors of the angles, internal and external, of the first triangle. See also *Inversive Geometry* (no. 72, p. 242-244; rev. by Snyder in *AMS Bull.*, v. 40), a work which represents the development and refinement of many of his own articles and those of his students during a number of years. A quotation from the preface is illuminating: "We believe that the tradition that simple geometrical and mechanical questions are to be handled only as Euclid or Descartes may have handled them is very hampering; that the ideas of Riemann, Poincaré, Klein and others have pleasant reverberations in the investigation of elementary questions by students of proper maturity and leisure."

For many years, even after his retirement from the university, Professor Morley participated in research programs of the Carnegie Institution assisted by various associates including A. B. Coble, H. Bateman and J. R. Conner. When in 1903 mathematicians of America rated in order their 80 leading men of research, Morley was put seventh. In the recently published (1934) index of *Encyk. d. Math. Wiss.*, v. 3, there are 30 references to work of Morley; see in particular "Die Potentialkurven und die Morleyschen Enveloppen," part 2, p. 609-610, with references to his papers on metric geometry of the plane n -line and on projective coordinates (nos. 32, 39).

He enjoyed music and was for a number of years a member of the Baltimore Choral So. As a boy and young man he had shown exceptional promise as a chess player; "throughout life he could grasp the possibilities of a position at chess or of a hand at cards with astonishing ease and certainty. He had something of the same power in discussing a geometrical configuration, for he proved, not once but many times, that he could penetrate more deeply into its inner significance than the rest of us." (Richmond). He was on the Cambridge U. chess team 1880-84 and had the distinction of having once beaten Dr. Lasker, when Lasker was the champion of the world.

"He was a striking figure in any group. Deliberate in manner and speech, there was a suggestion of shyness about him. He was generally very well informed and interested in a strikingly wide range of subjects.

He was of an artistic temperament. While many of his papers and lectures seemed involved to the uninitiated, they all possessed a characteristic artistic charm." (Cohen). In the mass of his manuscripts left behind are many charming and characteristic items. An examination set his students in 1904 was prefaced with the remark: "In this examination, if an exact answer does not suggest itself, an inspired guess will be of value." In a seminary paper, when a new dormitory was being built, was the remark that what the University needed was not a dormitory but a cogitatory. His contributions to family newspapers of his children and grandchildren would probably interest a wide circle. "Those who were privileged to know him well will never forget the kindly aspects of his daily life nor the devotion with which he pursued the high cultural and scientific ideals which he had set. His personal achievements and his stimulating influence on the mathematics of his time assure him a permanent place in the history of the science." (Coble).

All three of Prof. Morley's sons were Rhodes scholars and have attained to distinction in various fields. Christopher, contributing ed. of *Saturday Rev. of Lit.*, is the author of scores of popular books; Felix is the ed. of the *Washington Post*; Frank V., after getting his Ph.D. in mathematics at Oxford, became director of the publishing firm Faber and Faber, Ltd., London. Since they were all born in this country they are citizens of the U. S.; but their father always remained a British subject.

SOURCES.—H. W. Richmond, (1) *Nature*, v. 40, 1937, p. 880; (2) *LMS Journ.*, v. 13, 1938. A. B. Coble, *AMS Bull.*, v. 44, 1938. A. Cohen, *Science*, n.s., v. 86, 1937, p. 461. *Who's Who in Amer.*, v. 19. *The Times*, London, 19 Oct. 1937. *Nat. Cycl. Amer. Biog.*, v. 15, 1916. *Amer. Men Sci.*, 5th ed., 1933. Carnegie Inst. *Year Book*, 1909–36.

BIBLIOGRAPHY

1. *ETR: problems proposed*—6082, v. 32; 6112, v. 36; 6138, v. 37; 7216, v. 40; 8340, v. 44; 8376, v. 46; 9020, v. 47; 8413, 8620, 8654, 8896, 9067, 9107, v. 48; 9367, v. 49, 51, and 69; 9279, v. 50; 10034, v. 51; 9336, 10190, 10263, v. 53; 10495, 10562, 10592, v. 54; 10624, 10701, 10834, 10873, 10956, v. 55; 10873, 11163, v. 56; 10766, 10794, 11440, v. 57; 11689, 11719, v. 59; 11994, v. 60; 11001, 12032, 12189, 12227, v. 61; 9224, 12377, 12413, v. 63; 12748, 12848, v. 64; 9224, 13006, 13054, v. 65; 11652, v. 66; 13192, v. 67; 14227, v. 73; 14543, v. 74, 1880–1901; s. 2, problems 10728, v. 1; 12904, v. 2 and 4; 15060, v. 3; 14735, v. 6 and 7; 10386, 11098, v. 10; 11045, v. 11; 9186, v. 12; 8654, 16524, v. 16; 11514, v. 16, 18, and 19; 10230, v. 17; 10531, 12344, v. 19; 10928, 13079, v. 21, 1902–1912; s. 3, problems 12575, v. 1; 11222, v. 5, 1916–1918; *solutions*—7216, v. 40; 8620, 8654, v. 48; 10710, v. 54; 10701, v. 55; 11328, v. 57; 9224, v. 65, 1884–1896; s. 2, problem, 14917, v. 2, 1902.
2. "A nine-line conic," *MM*, v. 15, 1886, p. 190–192.
3. "Some properties of confocal conics and a derived cubic," *MM*, v. 16, 1887, p. 181–185.
4. "On plane cubics which inflect on crossing their asymptotes," *MM*, v. 17, 1887, p. 51–57.
5. "A rule for escaping a danger," *Nature*, v. 35, 1887, p. 345. Interesting mathematical letter dated "Bath College."
6. "On critic centres," *AJM*, v. 10, 1888, p. 141–148.
7. "Note on geometric inferences from algebraic symmetry," *AJM*, v. 10, 1888, p. 173–174.
8. "On the geometry of a nodal circular cubic," *Haverford C. Studies*, no. 1, 1889, p. 88–99; *AJM*, v. 11, 1889, p. 307–316.

9. "On some properties of the triangle," *Haverford C. Studies*, no. 3, 1890, p. 74-80.
10. "On the caustic of the epicycloid," *Haverford C. Studies*, no. 4, 1890, p. 9-16.
11. "On the kinematics of a triangle of constant shape but varying size," *QJM*, v. 24, 1890, p. 359-369.
12. "Note on conformal representation by means of the p -function," *Haverford C. Studies*, no. 10, 1891, p. 50-56.
13. "On the epicycloid," *AJM*, v. 13, 1891, p. 179-184.
14. "On the covariant geometry of the triangle," *QJM*, v. 25, 1891, p. 186-197.
15. *A Treatise on the Theory of Functions* (with J. Harkness), New York and London, 1893, ix+507 p.
16. "Three notes on permutations," *NYMS Bull.*, v. 3, 1894, p. 142-148.
17. "On adjustable cycloidal and trochoidal curves," *AJM*, v. 16, 1894, p. 188-204.
18. "Apolar triangles on a conic," *AMS Bull.*, v. 1, 1895, p. 116-124.
19. "Note on the theory of three similar figures," *AMS Bull.*, v. 1, 1895, p. 235-237.
20. "On a generalization of Weierstrass's equation with three terms," *AMS Bull.*, v. 2, 1895, p. 21-22.
21. "Note on the congruence $2^{2n} \equiv (-)^n (2n)! / (n!)^2$, where $2n+1$ is a prime," *AM* v. 9, 1895, p. 168-170.
22. "Note on the common tangents of two similar cycloidal curves," *AMS Bull.*, v. 2, 1896, p. 111-116.
23. "A generating function for the number of permutations with an assigned number of sequences," *AMS Bull.*, v. 4, 1897, p. 23-28.
24. "On the Poncelet polygons of a limaçon," *LMS Proc.*, v. 29, 1897, p. 83-97.
25. "A construction by the ruler of a point covariant with five given points," *MA*, v. 49, 1897, p. 596-600.
26. "On a regular rectangular configuration of ten lines," *LMS Proc.*, v. 29, 1898, p. 670-673.
27. *Introduction to the Theory of Analytic Functions* (with J. Harkness), New York and London, 1898, xv+336 p.
28. "The 'no-rolling' curves of Amsler's planimeter," *AM*, s. 2, v. 1, 1899, p. 21-30.
29. "Some polar constructions," *MA*, v. 51, 1899, p. 410-416.
30. "On a regular configuration of ten line pairs conjugate as to a quadric," *AMS Bull.*, v. 5, 1899, p. 252-253.
31. "Note on the sphero-conic," *Math. Gazette*, v. 1, 1899, p. 299-300.
32. "On the metric geometry of the plane n -line," *AMS Trans.*, v. 1, 1900, p. 97-115.
33. "The undergraduate mathematical curriculum." Report of discussion at summer meeting AMS, June 1900, *AMS Bull.*, v. 7, 1900, p. 21-22.
34. "The value of $\int_0^{\pi/2} (\log 2 \cos \phi)^m \phi^n d\phi$," *AMS Bull.*, v. 7, 1901, p. 390-392.
35. "On a point in Sylvester's theory of canonical forms" (abstract), *AMS Bull.*, v. 7, 1901, p. 206.
36. "On the series $1 + \left(\frac{p}{1}\right)^3 + \left\{\frac{p(p+1)}{1.2}\right\}^3 + \dots$," *LMS Proc.*, v. 34, 1902, p. 397-402
37. Report (with E. H. Moore and O. Stone) of Advisory Comm. on Math., Carnegie Inst., *Yearbook*, v. 1, 1902, p. 232-235; followed by a letter from F. N. Cole to Morley, p. 235-238.
38. "Orthocentric properties of the plane n -line," *AMS Trans.*, v. 4, 1903, p. 1-12.
39. "Projective coordinates," *AMS Trans.*, v. 4, 1903, p. 288-296.
40. "On the geometry whose element is the 3-point of a plane," *AMS Trans.*, v. 5, 1904, p. 467-476.
41. "On a plane quintic curve," *LMS Proc.*, s. 2, v. 2, 1904, p. 114-121.
42. "A fragment of elementary mathematics," *BAAS Report*, 1904, p. 439-440.
43. "A solution, not by elliptic functions, is wanted of the following: Given five lines $abcde$ in a plane, it is known that the pairs of points, $ab, ce; bc, da; cd, eb; de, ac; ea, bd$ are in a collineation. Prove that the fixed triangle of this collineation is self-polar as to both the conic on ab, bc ,

- cd*, *de*, *ea*, and the conic on *ac*, *ce*, *eb*, *bd*, *da*," *Math. Gazette*, v. 3, 1905, p. 262. Solutions were given by H. Bateman (p. 379) and A. C. Dixon (v. 4, p. 15).
44. "On two cubic curves in triangular relation," *LMS Proc.*, s. 2, v. 4, 1906, p. 384-392.
 45. "On reflexive geometry," *AMS Trans.*, v. 8, 1907, p. 14-24.
 46. "Plane sections of a Weddle surface" (with J. R. Conner), *AJM*, v. 31, 1909, p. 263-270, and errata slip.
 47. "The contact conics of the plane quintic curve," *JHU Circulars*, v. 31, 1912, p. 69-73.
 48. "On the extension of a theorem of W. Stahl," *Intern. Congress Mathems.*, Cambridge, v. 2, 1913, p. 11-17.
 49. "An extension of Feuerbach's theorem," *NAS Proc.*, v. 2, 1916, p. 171-173.
 50. "On the Lüroth quartic curve," *AJM*, v. 41, 1919, p. 279-282.
 51. "Note on the preceding paper," [i.e., "Notes on the cyclic quadrilateral" by F. V. Morley] *AM*, s. 2, v. 22, 1920, p. 43.
 52. "Pleasant questions and wonderful effects," *AMS Bull.*, v. 27, 1921, p. 309-312. AMS ret. P add. 28 Dec. 1920.
 53. "Note on Einstein's equation of an orbit," *AJM*, v. 43, 1921, p. 29-32.
 54. [Greetings and good wishes from *JHU* on the occasion of the inauguration of Pres. Atwood at Clark U.], *Clark U. Lib., Pub.*, v. 6, no. 4, 1921, p. 19-21.
 55. Problems proposed in *AMM*: no. 3093, v. 31, 1924; no. 3199 [3187], v. 33, 1926; no. 3444, v. 37, 1930 with solution by proposer v. 38, 1931; nos. 3560, 3575, v. 39, 1932; no. 3718, v. 42, 1935; no. 3792, v. 43, 1936.
 56. "On the intersections of the trisectors of the angles of a triangle," *Math. Assoc. Japan Secondary Ed., Journ.*, v. 6, 1924, p. 260-262.
 57. "The curve of ambience," *AJM*, v. 46, 1924, p. 193-200.
 58. "The eliminant of a net of curves," *AJM*, v. 47, 1925, p. 91-97.
 59. "On an equation of planar motion," *AJM*, v. 47, 1925, p. 98-100.
 60. "Notes on Neuberg's cubic curve," *AMM*, v. 32, 1925, p. 407-411.
 61. "On differential inversive geometry," *AJM*, v. 48, 1926, p. 144-146.
 62. "New results in elimination" (with A. B. Coble), *AJM*, v. 49, 1927, p. 463-488.
 63. "Extensions of Clifford's chain-theorem," *AJM*, v. 51, 1929, p. 465-472.
 64. "On algebraic inversive invariants" (with B. C. Patterson), *AJM*, v. 52, 1930, p. 413-424.
 65. "Note on range-finding" (with H. A. Robinson), *NAS Proc.*, v. 16, 1930, p. 74-77.
 66. "Tritangent circles of the rational bicubic" (with W. K. Morrill), *AJM*, v. 54, 1932, p. 185-189.
 67. "The celestial sphere," *AJM*, v. 54, 1932, p. 276-278.
 68. "Second note on the celestial sphere," *AJM*, v. 54, 1932, p. 489-492. See also *AMM*, v. 39, 1932, p. 507-508.
 69. "On the common points of two planar cubics and of two planar cyclides" (with W. K. Morrill), *AJM*, v. 54, 1932, p. 493-495.
 70. "The rectangular five-point" (with R. C. Yates), *AJM*, v. 54, 1932, p. 496-498.
 71. "The theory of six numbers" (abstract), *AMM*, v. 39, 1932, p. 249-250.
 72. *Inversive Geometry* (with F. V. Morley), London, Oct. 1933, and Boston, Nov. 1933, ix + 273 p.
 73. "Regions and paths" (abstract), *AMM*, v. 41, 1934, p. 66.
 74. "When and where," *The Criterion*, ed. by T. S. Eliot, London, v. 15, 1936, p. 200-209. Strictly mathematical relativity article overlooked by abstracting journals.
 75. "Note on astatic elements" (with J. R. Musselman), *AJM*, v. 58, 1936, p. 637-638.
 76. "On $2n$ points with a real cross-ratio" (with J. R. Musselman), *AJM*, v. 59, 1937, p. 787-792.
 77. "Planar positions," *Intern. Congress Mathems.*, Oslo, v. 2, 1937, p. 144-146.
 78. "The Hexlet," *Nature*, v. 139, 1937, p. 72-73. Compare F. Soddy, (a) "The kiss precise,"

(b) "The hexlet" (poem), (c) "The bowl of integers and the hexlet"; (a) v. 137, p. 1021, (b) v. 138, p. 958, (c) v. 139, p. 77-79. Morley's letter was inspired by (b).

79. Reviews of books by Lachlan in *NYMS Bull.*, 1893; Gundelfinger, Schwatt, Huebner, Hadamard, Schoenflies, Duporcq, d'Ocagne in *AMS Bull.*, 1895-1900.

16. GILBERT AMES BLISS

CURRICULUM VITAE.—B. Chicago, Ill. 9 May 1876. Educ. U. Chicago (93-00; B.S. 97; M.S. 98; Ph.D. 00); instr. math. U. Minnesota (00-02); student U. Göttingen 02-03; assoc. U. Chicago (03-04); assist. prof. U. Missouri (04-05); preceptor Princeton U. (05-08); assoc. prof. U. Chicago (08-13; prof. 13- ; chm. dept. since 27). Martin A. Ryerson distinguished service prof. U. Chicago since 33. Lect. U. Wisconsin summer 07, Harvard U. first sem. 11-12.

HONORS.—Colloq. Lect. AMS 09. Starred *Amer. Men Sci.* 10. VP AMS 11. Mem. NAS 16. Scientific expert, Range Firing Sect., Aberdeen Proving Ground, Oct.-Dec. 18. P AMS 21-22. Mem. NRC Fellowship Board 24-36. AMS trustee 24. First award of Chauvenet (quinquennial) Prize of \$100 by MAA 25; for a mathematical article of expository excellence, "Algebraic functions and their divisors," see Bibl. no. 43. Mem. Amer. Phil. So. 26. Mem. AMS Comm. on Colloquia 26-28. Chm. editorial comm. Science Series, U. Chicago 29- . VP AAAS and chm. Sect A 30; ret. add. see Bibl. no. 57. Fellow AACAS 35. Hon. Sc.D. U. Wisconsin 35.

BIOGRAPHICAL NOTES.—Prof. Bliss is a son of George Harrison Bliss, an electrical expert who superintended the installation of one of the first incandescent lighting plants in a theater in Chicago. He is a descendant of Thomas Bliss who came from Belstone, Eng. to Boston, Mass. in 1636 and settled in Rehoboth, Mass. On his mother's side he is a grandson of Orrin P. Gilbert of Colchester, Conn., afterwards, instructor in modern languages in Worcester Academy.

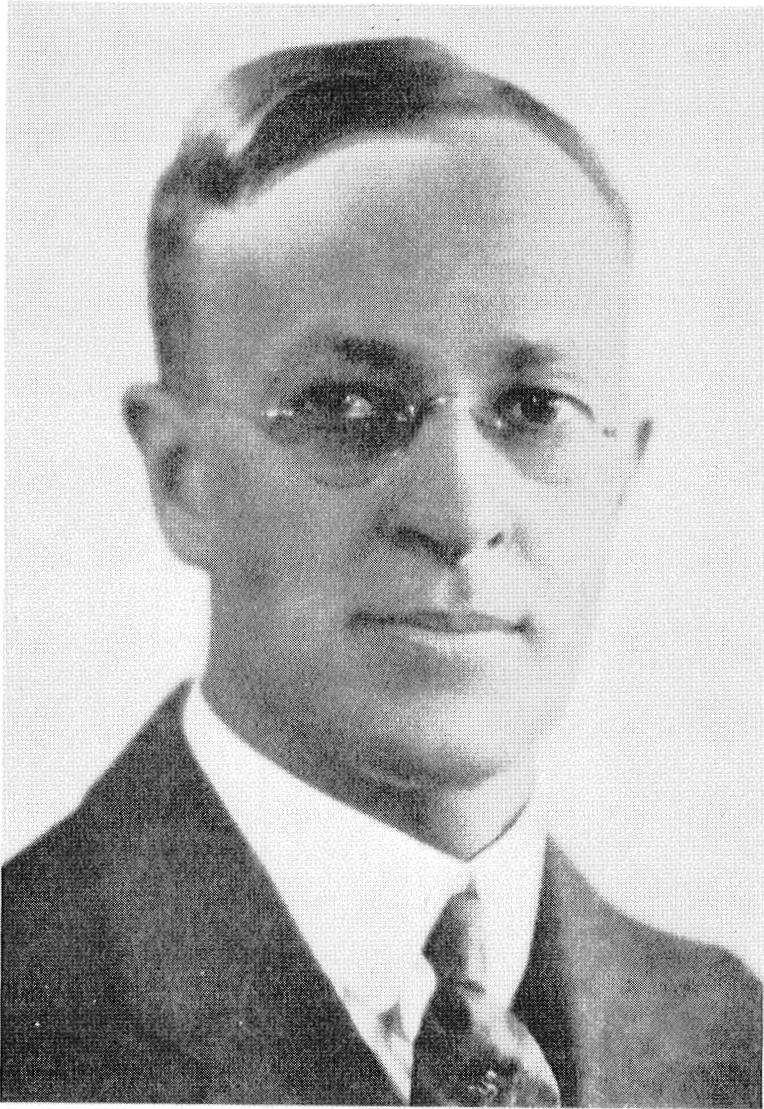
In the graduate school at U. Chicago Bliss's work was at first mostly in mathematical astronomy under F. R. Moulton, an inspiring teacher who encouraged him in writing his first published paper (Bibl. no. 1). His principal interest was in mathematics, however, and in 1898 he became a candidate for the doctor's degree in that field. Through the acquisition of a copy of the famous course of lectures in the calculus of variations which Weierstrass gave in 1879, and through Bolza's fascinating lectures, this subject became Bliss's dominant interest. During the year at Göttingen, Klein, Hilbert and Minkowski were the leaders, and among the younger men were Zermelo, E. Schmidt, Abraham, Féjer, Carathéodory, Kellogg, and Max Mason. After only a year spent as assist. prof. math. under Prof. Hedrick at U. Missouri (where W. A. Hurwitz was an extraordinarily able and precocious student in one of his classes), he accepted a call to Princeton U. in connection with the initiation of President Wilson's preceptorial scheme, when Dean Fine commenced to lay the basis for the development of a great department. Eisenhart, Veblen, J. W. Young, and R. L. Moore were the associates with whom discussions were constantly stimulating. Maschke died in 1908, and Bliss was appointed to his place at the U. Chicago.

While the Bibliography below testifies to Prof. Bliss's activity in re-

search and his special gift for lucid and interesting exposition, he has ever been generous in giving up time to much less congenial editorial tasks, as follows: assoc. ed. *AM* 06–08, assoc. ed. *AMS Trans.* 09–16, mem. editorial comm. *Carus Monographs*, 24–. But further, apart from directing the AMS at a critical period, and the affairs of his department for more than a decade he has long had many students working for their doctorate under his direction. The complete list of such students (46) is an interesting one, namely: E. J. Miles, Marion B. White, L. L. Dines, C. A. Fischer, W. V. Lovitt, Gillie A. Larew, A. S. Merrill, D. S. Smith, K. W. Lamson, F. E. LeSturgeon, W. P. Ott, I. A. Barnett, E. H. Clarke, J. D. Eshleman, L. M. Graves, Jewel W. Hughes, J. H. Taylor, H. A. Simmons, I. R. Pounder, Marion E. Stark, F. H. Bamforth, T. F. Cope, D. R. Davis, E. L. Mackie, A. O. Hickson, Rosa L. Jackson, Marie M. Johnson, L. La Paz, M. G. Boyce, W. L. Duren, Jr., Aline Huke, E. J. McShane (under Bliss and Graves), F. L. Wren, M. Coral, R. G. Sanger, M. R. Hestenes, K.-S. Hu (under Bliss and Graves), A. W. Raab (under Bliss and Graves), Julia W. Bower, B. Crosby II, R. H. Bardell, Evelyn P. Wiggin (under Bliss and Reid), C. H. Denbow (under Bliss, Graves and Reid), A. S. Householder, N. A. Moscovitch, F. A. Valentine (under Bliss and Graves).

After the U. S. joined in the World War, navigation was taught at U. Chicago in the summer of 1918, and Bliss had a section with about 100 students. At this time Oswald Veblen was a major in charge of the Range Firing Sect. of the Aberdeen Proving Ground, and induced Bliss to go there as scientific expert. His particular problem was to deal with “differential corrections” of trajectories for the effects of wind, variations from normal in the density of the air and weights of the projectile and powder charge, and in the case of long ranges, for the rotation of the earth. Application of the theories of calculus of variations was highly effective and in many cases reduced by three-fourths the time previously necessary for range corrections.

Of special significance in Bliss’s research are the generalization of algebraic elimination theory (no. 21), the theory of the singularities of real transformations of the plane in the *Colloquium Lectures* (no. 22, of which there was a 2d ed.), and the theory of “differential corrections” (nos. 36, 37, 39, 40), applicable elsewhere than in ballistics, which may be the basis of future results of significance. Studies of the simplification of algebraic curves by birational transformations (nos. 41, 42, 43, 60) led to another volume in the *Colloq. Pub.* series. But by far the most extensive part of Bliss’s research has been in the calculus of variations and culminated in the lectures on *The Problem of Bolza* (no. 68). Two earlier papers “Jacobi’s condition for problems of the calculus of variations in parametric form” (no. 31), and “The transformation of Clebsch” (no. 49) are especially notable since they are the bases for quite remarkable improvements in the theory of the second variation in the calculus of variations, and have had



G. A. Bliss

1924

much influence on the literature. As a result of them the elaborate transformation theories of Clebsch, von Escherich, and others, and of Weierstrass for parametric problems, can be replaced by relatively very simple arguments.

As an undergraduate Prof. Bliss was in the Glee Club and its president for a year. In order to earn money necessary for his college expenses he became a member of a student professional mandolin quartet. He has always been interested in sport and beginning with bicycle racing in student days he has successively taken up tennis, racquets, and golf. In 1910 Waseda U. of Tokyo invited U. Chicago to send its baseball team to Japan for a series of games with the teams of Waseda U. and Keio U. (near Tokyo). The Chicago team was the first one so invited and Prof. Bliss was asked to go with the team as faculty representative. He arranged not only for seven months' leave of absence, but also joined with the captain of the team on a trip around the world when the games were over. After the team left Hong Kong for the U. S., Bliss visited Canton, Singapore, Burma, India, and Egypt.

As an administrator, as a teacher, and as a man, Prof. Bliss's influence on American mathematicians has been most notable. We refer in chapter III to his services while he was P of the Society.

SOURCES.—*Amer. Men Sci.*, 5th ed. *Who's Who in Amer.*, v. 19. "Poggendorff" v. 5-6. *Nat. Cycl. Amer. Biog.*, New York, v. A., 1930. *Catalogue of the Delta Kappa Epsilon Fraternity*, New York, 1910. J. H. Bliss, *Genealogy of the Bliss Family in America*, Boston, 1881, p. 601, etc. C. A. Hoppin, *The Bliss Book*, Hartford, Conn., privately printed, 1913; deals particularly with the English family. Personal information.

BIBLIOGRAPHY

1. "The motion of a heavenly body in a resisting medium," *Pop. Astr.*, v. 6, 1898, p. 20-29.
2. "The geodesic lines on the anchor ring," *AM*, s. 2, v. 4, 1902, p. 1-21. Doctoral diss.
3. "The second variation of a definite integral when one end-point is variable," *AMS Trans.*, v. 3, 1902, p. 132-141.
4. "Jacobi's criterion when both endpoints are variable," *MA*, v. 58, 1904, p. 70-80.
5. "Sufficient condition for a minimum with respect to one-sided variations," *AMS Trans.*, v. 5, 1904, p. 477-492.
6. "An existence theorem for a differential equation of the second order, with an application to the calculus of variations," *AMS Trans.*, v. 5, 1904, p. 113-125.
7. "The exterior and interior of a plane curve," *AMS Bull.*, v. 10, 1904, p. 398-404.
8. "The solutions of differential equations of the first order as functions of their initial values," *AM*, s. 2, v. 6, 1905, p. 49-68.
9. "A proof of the fundamental theorem of analysis situs," *AMS Bull.*, v. 12, 1906, p. 336-341.
10. "A generalization of the notion of angle," *AMS Trans.*, v. 7, 1906, p. 184-196.
11. "A problem of the calculus of variations in which the integrand is discontinuous" (with Max Mason), *AMS Trans.*, v. 7, 1906, p. 325-336.
12. "The construction of a field of extremals about a given point," *AMS Bull.*, v. 13, 1907, p. 321-324.
13. "A new form of the simplest problem of the calculus of variations," *AMS Trans.*, v. 8, 1907, p. 405-414, 536.

14. "On the inverse problem of the calculus of variations," *AM*, s. 2, v. 9, 1908, p. 127-140.
15. "A method of deriving Euler's equation in the calculus of variations," *AMM*, v. 15, 1908, p. 47-54.
16. "The properties of curves in space which minimize a definite integral" (with Max Mason), *AMS Trans.*, v. 9, 1908, p. 440-466.
17. "A new proof of Weierstrass' theorem concerning the factorization of a power series," *AMS Bull.*, v. 16, 1910, p. 356-359.
18. "Fields of extremals in space" (with Max Mason), *AMS Trans.*, v. 11, 1910, p. 325-340.
19. "The function concept and the fundamental notions of the calculus," J. W. A. Young, *Monographs on Topics of Modern Mathematics*, New York, 1911, p. 261-304.
20. "A new proof of the existence theorem for implicit functions," *AMS Bull.*, v. 18, 1912, p. 175-179.
21. "A generalization of Weierstrass' preparation theorem for a power series in several variables," *AMS Trans.*, v. 13, 1912, p. 133-145.
22. *Fundamental Existence Theorems* (*AMS Colloq. Pub.*, v. 6), 1913, li+107 p.; reprinted 1934. *AMS colloq. lects. at Princeton*, Sept. 1909.
23. "A note on symmetric matrices," *AM*, s. 2, v. 16, 1914, p. 43-44.
24. "A substitute for Duhamel's theorem," *AM*, s. 2, v. 16, 1914, p. 45-49.
25. "A method of subdividing the interior of a simply closed rectifiable curve with an application to Cauchy's theorem," *Sci. Labs. Denison U., Bull.*, v. 17, 1914, p. 375-389.
26. "The minimum of a definite integral for unilateral variations in space" (with A. L. Underhill), *AMS Trans.*, v. 15, 1914, p. 291-310.
27. "The Weierstrass E -function for problems of the calculus of variations in space," *AMS Trans.*, v. 15, 1914, p. 369-378.
28. "Generalizations of geodesic curvature and a theorem of Gauss concerning geodesic triangles," *AJM*, v. 37, 1915, p. 1-18.
29. "A note on functions of lines," *NAS Proc.*, v. 1, 1915, p. 173-177.
30. "A note on the problem of Lagrange in the calculus of variations," *AMS Bull.*, v. 22, 1916, p. 220-225.
31. "Jacobi's condition for problems of the calculus of variations in parametric form," *AMS Trans.*, v. 17, 1916, p. 195-206.
32. "Integrals of Lebesgue," *AMS Bull.*, v. 24, 1917, p. 1-47.
33. "A necessary and sufficient condition for the existence of a Stieltjes integral," *NAS Proc.*, v. 3, 1917, p. 633-637.
34. "Solutions of differential equations as functions of the constants of integration," *AMS Bull.*, v. 25, 1918, p. 15-26.
35. "The problem of Mayer with variable end points," *AMS Trans.*, v. 19, 1918, p. 305-314.
36. "A method of computing differential corrections for a trajectory," *Journ. U. S. Artillery*, v. 51, 1919, p. 445-449; a corrected copy of earlier reprint in v. 50, 1919, p. 455-460.
37. "The use of adjoint systems in the problem of differential corrections for a trajectory," *Journ. U. S. Artillery*, v. 51, 1919, p. 296-311. In the files of the Aberdeen Proving Ground there is a blueprint by Bliss, "Differential corrections for anti-aircraft guns," 1919.
38. "Some recent developments in the calculus of variations," *AMS Bull.*, v. 26, 1920, p. 343-361.
39. "Differential equations containing arbitrary functions," *AMS Trans.*, v. 21, 1920, p. 79-92.
40. "Functions of lines in ballistics," *AMS Trans.*, v. 21, 1920, p. 93-106.
41. "Birational transformations simplifying singularities of algebraic curves," *AMS Trans.*, v. 24, 1922, p. 274-285.
42. "The reduction of singularities of plane curves by birational transformation," *AMS Bull.*, v. 29, 1923, p. 161-183. *AMS ret. P add.* 28 Dec. 1922.
43. "Algebraic functions and their divisors," *AM*, s. 2, v. 26, 1924, p. 95-124.

44. *The Problem of Lagrange in the Calculus of Variations* (mimeographed lect. notes), U. Chicago, 1925, 3+75 p. Reprinted with corrections and additions in *AJM*, v. 52, 1930, p. 673-744.
45. "*Calculus of Variations (Carus Math. Monograph)*, Chicago, 1925, xiii+189 p.; 2d impression 1927.
German trans. by F. Schwank: *Variationsrechnung*, Leipzig, 1932, viii+127 p.
46. "A boundary value problem in the calculus of variations," *AMS Bull.*, v. 32, 1926, p. 317-331.
47. "A boundary value problem for a system of ordinary linear differential equations of the first order," *AMS Trans.*, v. 28, 1926, p. 561-584.
48. "Contributions that have been made by pure science to the advancement of engineering and industry. Mathematics," *Scientific Mo.*, v. 24, 1927, p. 308-319.
49. "The transformation of Clebsch in the calculus of variations," *Intern. Congress Mathems.*, Toronto, v. 1, 1928, p. 589-603.
50. (a) *Existence Theorems for Implicit Functions*; (b) *Existence Theorems for Differential Equations* (mimeographed lect. notes), U. Chicago, 1929 (?), 9+14 p.; (b) is also Chap. IX of *The Theory of Functions of Real Variables* by L. M. Graves (mimeographed lect. notes), U. Chicago, 1931.
51. "An integral inequality," *LMS Journ.*, v. 5, 1930, p. 40-46.
52. *Contributions to the Calculus of Variations, 1930* (ed. with L. M. Graves), U. Chicago, 1931, vii+349 p.
53. "On separation, comparison and oscillation theorems for self-adjoint systems of linear second order differential equations" (with I. J. Schoenberg), *AJM*, v. 53, 1931, p. 781-800.
54. *Topics of the Calculus of Variations* (mimeographed lect. notes, ed. by G. A. Bliss), U. Chicago, 1932, 67 p.
55. "Ernest Julius Wilczynski," *Science*, v. 76, 1932, p. 316-317.
56. "The problem of Bolza in the calculus of variations," *AM*, s. 2, v. 33, 1932, p. 261-274.
57. "The calculus of variations and the quantum theory," *AMS Bull.*, v. 38, 1932, p. 201-224. Add. VP AAAS and chm. Sect. A, 29 Dec. 1931.
58. "On the derivation of necessary conditions for the problem of Bolza" (with I. J. Schoenberg), *AMS Bull.*, v. 38, 1932, p. 858-864.
59. *The Calculus of Variations, Multiple Integrals* (mimeographed lect. notes), U. Chicago, 1933, iii+108 p.
60. *Algebraic Functions* (AMS Colloq. Pub. v. 16), 1933, ix+218 p.
61. *Contributions to the Calculus of Variations, 1931-32* (ed. with L. M. Graves), U. Chicago, 1933, vii+523 p.
62. "Eliakim Hastings Moore," Chicago, *Univ. Record*, v. 19, 1933, p. 130-134.
63. "Eliakim Hastings Moore," *AMS Bull.*, v. 39, 1933, p. 831-838.
64. "Mathematical interpretations of geometrical and physical phenomena," *AMM*, v. 40, 1933, p. 472-480. Reprinted with minor changes in M. I. Logsdon, *A Mathematician Explains*, Chicago, 1935, Chap. 8, p. 146-158; 2d ed. 1936.
65. "Sufficient conditions for a problem of Mayer in the calculus of variations" (with M. R. Hestenes), *AMS Trans.*, v. 35, 1933, p. 305-326; also *Contributions to the Calculus of Variations 1931-32*, p. (297)-(337).
66. *The Calculus of Variations in Three-Space* (mimeographed lect. notes), U. Chicago, 1934, iii+123 p.
67. "The scientific work of Eliakim Hastings Moore," *AMS Bull.*, v. 40, 1934, p. 501-514.
68. *The Problem of Bolza in the Calculus of Variations* (mimeographed lect. notes), U. Chicago, 1935, vii+140 p.
69. Part IV of symposium from 1935 Alumni Reunion Conference on "What is this thing called academic freedom?" *U. Chicago Mag.*, 1935, p. 336-338.
70. "Biographical memoir of Eliakim Hastings Moore, 1862-1932" (with L. E. Dickson), *NAS Biog. Mem.*, v. 17, 1936, p. 83-102+ portrait.

71. "The evolution of problems of the calculus of variations," *AMM*, v. 43, 1936, p. 598-609.
72. "Herbert Ellsworth Slaught" (with L. E. Dickson), *Science*, v. 86, 1937, p. 72-73.
73. "Herbert Ellsworth Slaught," *U. Chicago Mag.*, 1937, p. 22-24. Also in Kansas Assoc. Teach. Math., *Bull.*, v. 12, 1937, p. 9-12; with portraits of Slaught and Bliss.
74. "Herbert Ellsworth Slaught—in Memoriam," *AMS Bull.*, v. 43, 1937, p. 595-597.
75. "Herbert Ellsworth Slaught—teacher and friend," *AMM*, v. 45, 1938, p. 5-10. Presented at meeting MAA Sept. 1937.
76. "Normality and abnormality in the calculus of variations," *AMS Trans.*, v. 43, 1938, p. 365.
77. Reviews of books by Pierpont, Bôcher, Eisenhart, Volterra, Osgood, Blaschke, Vivanti, and Forsyth in *AMS Bull.*, 1906-28; by Vivanti in *Boll. d. Matem.*, 1926; and by Hardy, Littlewood and Polya in *Science*, 1935.

17. OSWALD VEBLEN

CURRICULUM VITAE.—B. Decorah, Ia. 24 June 1880. Prepared at public schools Iowa City, Ia., as student U. Iowa (94-98; A.B. 98; lab. assist. phys. 98-99); at Harvard U. (99-00; A.B. 00); at U. Chicago (00-03; Ph.D. 03; assoc. 03-05). Preceptor Princeton U. (05-10; prof. 10-26; Henry Burchard Fine prof. 26-32). Prof. in School of Math., Inst. for Adv. Study (32-). Capt. and major, U. S. Ordnance Dept., Aberdeen, Md., 17-19. Deputy for the Savilian prof. math. (exchange with G. H. Hardy), U. Oxford first sem. 28-29. Walker Ames prof. U. Washington first term of summer 37.

HONORS.—Starred *Amer. Men Sci.* 10. Joint ed. *AM* Sept. 11-July 25; cooperating ed. Oct. 26-Sept. 31. Mem. Amer. Phil. So. 12. VP AMS 15. Colloq. Lect. AMS 16; "Analysis situs" (Bibl. no. 30). VP MAA 17; trustee 16, 20-22, 26-31. Mem. NAS 19. AMS nominee mem. NRC Div. Phys. Sci. Jan. 20-July 23; also mem. exec. comm. of Div. 20-23, and vice-chm. 22-23. VP AAAS and chm. Sect. A 21; add. "Geometry and physics" (no. 35). Fellow Amer. Phys. So. 21. Fellow AAcAS 23. P AMS 23-24; ret. P add. "Remarks on the foundations of geometry" (no. 40). Trustee AMS 24, 27-30. Mem. NRC Fellowship Board for phys., chem., and math. 25-36. Mem. board of trustees of Nat. Research Endowment of NAS 26; see *Science*, n.s., v. 63, p. 158. Chm. AMS comm. on Colloquia and *Colloq. Pubs.* 26-28, Dec. 33-36. Mem. council NAS 26-29; 37- . Mem. AAAS comm. on grants 26. Mem. Council LMS 28. Hon. Sc.D. U. Oxford 29. Hon. Ph.D. U. Oslo 29; on the occasion of the Abel centenary celebration. Corresp. mem. Göttingen So. Sci. 29. William Lowell Putnam Lect. Harvard U., "Five-dimensional relativity," 30. Lect. U. Göttingen 32. Delegate U. S. Govt., Intern. Congress Mathems., Zürich 32. Delegate AAAS to BAAS 32. Hon. Ph.D. U. Hamburg 32. Assoc. ed. *Com. Mathem.* 34-. Invited speaker Intern. Congress Mathems., Oslo 36; "Spinors and projective geometry" (no. 67). Delegate U. S. Govt., and AAAS to Intern. Congress Mathems. Oslo 36. Joint ed. *Zentralblatt f. Math.* 36-.

BIOGRAPHICAL NOTES.—Prof. Veblen is a grandson of Thomas Anderson and Kari T. (Bunde) Veblen, who in 1847 emigrated from Valdris, Norway, and settled in Ozaukee County, Wis. In 1865 they moved to a prairie farm in Rice County, Minn. where their family of twelve children was reared under the harsh conditions of early settlement in the Northwest. One of this family was Thorstein Bunde Veblen (1857-1929) the distinguished economist and social theorist (see *DAB*, v. 19, 1936; *Cycl. Amer. Biog.*, v. 21, 1931). His brother Andrew Anderson (1848-1932) who became prof. of physics at U. Iowa (see *Amer. Men Sci.*, 4th ed.) and m. Kirsti Hougen, was Prof. Veblen's father. With such an inheritance it is not strange that Prof. Veblen's favorite recreation is working out of doors.



Oswald Veblen

1924

He received the major part of his mathematical training at the U. Chicago from that inspiring trio Bolza, Maschke, and Moore. Under their direction he laid the basis for the important work he was later to achieve in the fields of foundations of geometry, projective geometry, analysis situs, differential invariants, and spinors. His often quoted dissertation (no. 5), under E. H. Moore, on a system of axioms of Euclidean geometry, followed the trend of development of Pasch (1882) and Peano (1889, 1894) rather than that of Hilbert (1899) and Pieri (1899). In this system "point" and "order" are the only undefined elements, and the number of axioms is reduced to twelve, which were proved to be independent (the first set of axioms for geometry of which this is true). His next paper, on analysis situs, appeared just before leaving for Princeton, which under his leadership during the next thirty years was to become one of the great centers of the world for topological studies. His lectures in this field at Princeton U., and such notable publications as nos. 25 and 26 naturally paved the way for his Colloquium Lectures on Analysis Situs in 1916 (no. 30; see reviews by S. Lefschetz, *DB*, v. 57, and *AMS Bull.*, v. 30). This book was for several years the source from which mathematicians in all parts of the world learned Topology and it is still a useful adjunct to the more modern and extensive work on Topology by Lefschetz, also in the AMS Colloquium series.

Veblen's diss. (no. 5) led naturally to questions treated in papers on projective geometry (nos. 11, 12, 13, 18) and to the very notable and scholarly treatise on the subject (no. 19), in two v., the first in collaboration with J. W. Young (see reviews by J. L. Coolidge *AMS Bull.*, v. 18, and R. L. Moore, *idem.* v. 26). This book has had a considerable influence on students of abstract algebra as well as of abstract geometry. As to the point of view in the joint v. the authors write: "Even the limited space devoted in this v. to the foundations may seem a drawback from the pedagogical point of view of some mathematicians. To this we can only reply that, in our opinion, an adequate knowledge of geometry cannot be obtained without attention to the foundations. We believe, moreover, that the abstract treatment is peculiarly desirable in projective geometry, because it is through the latter that the other geometric disciplines are most readily coördinated. Since it is more natural to derive the geometrical disciplines associated with the names of Euclid, Descartes, Lobatchewsky, etc., from projective geometry than it is to derive projective geometry from one of them, it is natural to take the foundations of projective geometry as the foundations of all geometry." The first v. made extensive use of spaces with a finite number of parts as illustrative of the generality of the theory. Linear order and continuity, and hence the discussion of the metric geometries characterized by certain subgroups of the general projective group, are topics of the second v. In this there are two principles for the classification of any theorem of geometry: (i) the axiomatic basis,

or bases, from which it can be derived, or in other words, the class of spaces in which it can be valid: and (ii) the group to which it belongs in a given space.

Veblen's interest in the foundations of mathematics led to his collaboration with N. J. Lennes, then an instr. in a Chicago high school, in the preparation of another book, *Introduction to Infinitesimal Analysis, Functions of One Real Variable* (no. 15). Only fifteen years before, the first treatise in the English language on the theory of functions of a complex variable had been published. During that period the sister theory came into prominence in American university lecturing. In admirable fashion his work brought home to many American students of 1907 what was necessary for rigorous logical discussion of fundamental theorems of infinitesimal calculus. Such things as the systematic use of the Heine-Borel theorem, methodical use of the upper and lower bounds of a function for simplifying proofs, and the treatment of integration, were then novelties here. That the work is in demand, even at the present time, is indicated by its recent reprint.

Some of Veblen's important contributions after the world war were summed up in two of the *Cambridge Tracts* (nos. 43, 55) and in a monograph of the *Ergebnisse* series (no. 56). The first, *Invariants of Quadratic Differential Forms* (no. 43; reviewed by M. H. A. Newman in *Math. Gazette*, v. 14) took account of many new discoveries made after the advent of relativity, and sets forth those parts of the subject of primary value for applications to electromagnetic theory, dynamics, and quantum theory. The second tract on *The Foundations of Differential Geometry* (no. 55), written in collaboration with a former student, is a companion to the first and contains a critical study of the foundations of all mathematical systems which have been called geometries. A rigid definition of geometry is not attempted on the ground that any objective definition of geometry would include the whole of mathematics. "Any mathematical science is a body of theorems deduced from a set of axioms. A geometry is a mathematical science. The question arises why the name geometry is given to some mathematical sciences and not to others. It is likely that there is no definite answer to this question, but that a branch of mathematics is called a geometry because the name seems good, on emotional and traditional grounds, to a sufficient number of competent people." The third tract, *Projektive Relativitätstheorie* (no. 56; reviewed by D. J. Struik *AMS Bull.*, v. 40) is a result of a series of lectures at U. Göttingen and dealt with what was then a new aspect of the theory of relativity. It allows a unified theory of the gravitational and the electromagnetic field, and, with his later papers (nos. 57, 58), of the modern wave mechanics. It may be regarded as a generalization of classical non-euclidean geometry. The projective relativity theory is one of a series of investigations in which attempts, begun by Weyl in 1918, were made to define a space-time structure depending not only on gravitational but also on electromagnetic po-

tentials. Projective relativity seems to offer a simple and attractive solution. It has subsequently been recast and extended by various other mathematicians and physicists, as for example by Schouten and Van Dantzig in *Zeitsch. f. Physik*, and *AM* (v. 34). The recently published index (1934) to *Encyk. d. Math. Wiss.*, v. 3, gives more than a score of references to Veblen's publications.

With the founding of the Institute for Advanced Study in 1930, and the starting in 1932 of its School of Mathematics, a new stimulant of extraordinary potency was provided in Princeton for the development of mathematical research in the U. S. It was Veblen who was chiefly responsible for choosing the brilliant group of professors (Alexander, Einstein, Morse, von Neumann, Weyl) who constitute the nucleus of this School. At present he annually conducts seminars on topics such as: Modern differential geometry; Differential geometry and quantum theory; Geometry of complex domains (see no. 66); and in 1937-38, Quantum mechanics of composite systems, the last three with J. von Neumann.

Veblen made a great contribution to mathematical research in this country in yet another direction. It was largely through his influence that mathematicians since 1924 have been the recipients of National Research Council Fellowships. In chapter III an attempt is made to indicate the extraordinary indebtedness of the Society to him, at a critical time, for constructive service which he alone was qualified to render.

At U. Chicago and Princeton U. the doctoral dissertations of the following fifteen individuals were done under Veblen's direction, 1905-36: R. L. Moore (at Chicago), G. MacF. Conwell, U. G. Mitchell, H. H. Mitchell, A. A. Bennett, H. R. Brahana, P. Franklin, T. Y. Thomas, A. Church, M. S. Knebelman, J. H. C. Whitehead, A. L. Foster, B. Hoffmann, J. L. Vanderslice, J. W. Givens.

During the World War Major Veblen's remarkable powers of organization were capitalized by the Govt. which put him in charge of range firing and ballistic work at Aberdeen, Md. His work was largely experimental (see no. 28) and administrative. In addition to the routine computations, a considerable number of mathematical investigations were carried out in 1918 by the following mathematicians in this organization: H. F. Blichfeldt, G. A. Bliss, T. H. Gronwall, C. R. Dines, P. Franklin, W. C. Graustein, C. N. Haskins, H. H. Mitchell, and W. H. Roever.

It can be the privilege of but few to have done as much as Prof. Veblen to promote mathematical research in the United States.

Mrs. Veblen's brother O. W. Richardson, formerly a professor at Princeton U., is the distinguished research prof. of the RS and director of research in physics at King's C., London.

SOURCES.—*Who's Who*, 1938, London. *Who's Who in Amer.*, v. 19. *Amer. Men Sci.*, 5th ed. Doctoral diss. "Life" (Bibl. no. 5). Portrait, frontispiece U. Hamburg, Math. sem. *Abhandlungen*, v. 12, no. 1, 1937. "Poggendorff," v. 5. Inst. for Adv. Study, *Bulls.* 2-7, 1933-38.

BIBLIOGRAPHY

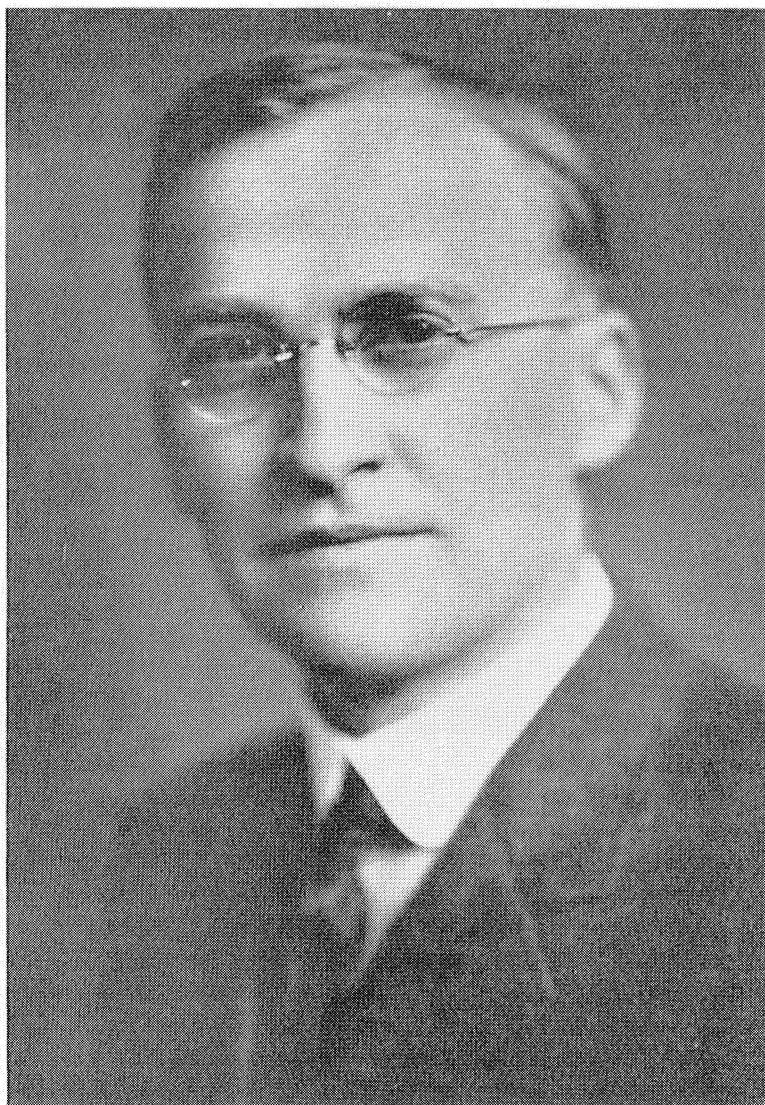
1. "Hilbert's foundations of geometry," *Monist*, v. 13, 1903, p. 303-309.
2. "The Heine-Borel theorem," *AMS Bull.*, v. 10, 1904, p. 436-439.
3. "Polar coordinate proofs of trigonometric formulas," *AMM*, v. 11, 1904, p. 6-12.
4. "The transcendence of π and e ," *AMM*, v. 11, 1904, p. 219-223.
5. "A system of axioms for geometry," *AMS Trans.*, v. 5, 1904, p. 343-384. Doctoral diss. as separate with special title page and "Life."
6. "Theory of plane curves in non-metrical analysis situs," *AMS Trans.*, v. 6, 1905, p. 83-98. Compare Bibl. no. 8 of R. L. Moore.
7. "Definition in terms of order alone in the linear continuum and in well-ordered sets," *AMS Trans.*, v. 6, 1905, p. 165-171.
8. "Euclid's parallel postulate," *Open Court*, v. 19, 1905, p. 752-755.
9. "The foundations of geometry," *Pop. Sci. Mo.*, 1906, p. 21-28.
10. "The square root and the relations of order," *AMS Trans.*, v. 7, 1906, p. 197-199.
11. "Finite projective geometries" (with W. H. Bussey), *AMS Trans.*, v. 7, 1906, p. 241-259.
12. "Collineations in a finite projective geometry," *AMS Trans.*, v. 8, 1907, p. 366-368.
13. "Non-desarguesian and non-pascalian geometries" (with J. H. M. Wedderburn), *AMS Trans.*, v. 8, 1907, p. 379-388.
14. "On magic squares," *MM*, v. 37, 1907, p. 116-118.
15. *Introduction to Infinitesimal Analysis, Functions of One Real Variable* (with N.J. Lennes), London and New York, Wiley, 1907, vii+227 p.; reprinted New York, Stechert, 1935.
16. "Continuous increasing functions of finite and transfinite ordinals," *AMS Trans.*, v. 9, 1908, p. 280-292.
17. "On the well-ordered subsets of the continuum," *CMP Rend.*, v. 25, 1908, p. 235-236, 397.
18. "A set of assumptions for projective geometry" (with J. W. Young), *AJM*, v. 30, 1908, p. 347-380.
19. *Projective Geometry*, 2 v. (v. 1 with J. W. Young), Boston, 1910-18, x+342+xii+511 p.
20. "Letter to the editor of the *Jahresbericht*," *DMV Jahr.*, v. 19, 1910, p. 263.
21. "The foundations of geometry," J. W. A. Young, *Monographs on Topics of Modern Mathematics*, New York, 1911, Chap. I, p. 1-51.
22. "On the definition of multiplication of irrational numbers," *AJM*, v. 34, 1912, p. 211-214.
23. "Jules Henri Poincaré," *APS Proc.*, v. 51, 1912, p. iii-ix.
24. "An application of modular equations in analysis situs," *AM*, s. 2, v. 14, 1912, p. 86-94.
25. "Decomposition of an n -space by a polyhedron," *AMS Trans.*, v. 14, 1913, p. 65-72, 506.
26. "Manifolds of n dimensions" (with J. W. Alexander), *AM*, s. 2, v. 14, 1913, p. 163-178.
27. "On the deformation of an n -cell," *NAS Proc.*, v. 3, 1917, p. 654-656.
28. "Rotating bands" (with P. L. Alger), *Journ. U. S. Artillery*, v. 51, 1919, p. 355-390.
29. "On matrices whose elements are integers" (with P. Franklin), *AM*, s. 2, v. 23, 1921, p. 1-15. Also, with minor changes, in O. Veblen, *Analysis Situs*, 2d ed., 1931 (no. 30), p. 170-189.
30. *Analysis Situs* (*AMS Colloq. Pub.*, v. 5, part 2), 1922, vii+150 p.; 2 ed., 1931, x+194 p.
31. "The Riemann geometry and its generalization" (with L. P. Eisenhart), *NAS Proc.*, v. 8, 1922, p. 19-23.
32. "Normal coordinates for the geometry of paths," *NAS Proc.*, v. 8, 1922, p. 192-197.
33. "Projective and affine geometry of paths," *NAS Proc.*, v. 8, 1922, p. 347-350.
34. "Equiaffine geometry of paths," *NAS Proc.*, v. 9, 1923, p. 3-4.
35. "Geometry and physics," *Science*, v. 57, 1923, p. 129-139. Add. VP AAAS, and chm. sect. A, 28 Dec. 1922.
36. "The intersection numbers," *AMS Trans.*, v. 25, 1923, p. 540-550. Also, with minor changes, in O. Veblen, *Analysis Situs*, 2d. ed., 1931 (no. 30), p. 159-169.

37. "The geometry of paths" (with T. Y. Thomas), *AMS Trans.*, v. 25, 1923, p. 551-608.
38. "Extensions of relative tensors" (with T. Y. Thomas), *AMS Trans.*, v. 26, 1924, p. 373-377.
39. "Invariance of the Poincaré numbers of a discrete group," *AMS Bull.*, v. 30, 1924, p. 405-406.
40. "Remarks on the foundations of geometry," *AMS Bull.*, v. 31, 1925, p. 121-141. AMS ret. P add. 31 Dec. 1924.
41. "Projective normal coordinates for the geometry of paths" (with J. M. Thomas), *NAS Proc.*, v. 11, 1925, p. 204-207.
42. "Projective invariants of affine geometry of paths" (with J. M. Thomas), *AM*, s. 2, v. 27, 1926, p. 279-296.
43. *Invariants of Quadratic Differential Forms* (Cambridge Tracts in Math. and Math. Phys., no. 24), Cambridge, 1927, vii+102 p.
44. "Projective tensors and connections," *NAS Proc.*, v. 14, 1928, p. 154-166.
45. "Conformal tensors and connections," *NAS Proc.*, v. 14, 1928, p. 735-745.
46. "Differential invariants and geometry," *Intern. Congress Mathems.*, Bologna, v. 1, 1929, p. 181-189.
47. "Generalized projective geometry," *LMS Journ.*, v. 4, 1929, p. 140-160.
48. "Differential forms"; "Projection in mathematics"; "Projective geometry"; *Encycl. Brit.*, 14th ed. London and New York, 1929, v. 7, p. 365-366; v. 18, p. 572-576.
49. "Henry Burchard Fine—in memoriam," *AMS Bull.*, v. 35, 1929, p. 726-730.
50. "A generalization of the quadratic differential form," *QJMO*, v. 1, 1930, p. 60-76.
51. "Projective relativity" (with B. Hoffmann), *Phys. Rev.*, v. 36, 1930, p. 810-822.
52. "The department of Mathematics," *Princeton Alumni Weekly*, v. 31, 1931, p. 633.
53. "The significance of Fine Hall," *Princeton Alumni Weekly*, v. 32, 1931, p. 112-113. Incorporated in an article entitled, "A memorial to a school-teacher."
54. "A set of axioms for differential geometry" (with J. H. C. Whitehead), *NAS Proc.*, v. 17, 1931, p. 551-561.
55. *The Foundations of Differential Geometry* (with J. H. C. Whitehead), (Cambridge Tracts in Math. and Math. Phys., no. 29), Cambridge, 1932, ix+96 p.
56. *Projektive Relativitätstheorie* (Ergebnisse der Mathematik und ihrer Grenzgebiete, v. 2, no. 1), Berlin, 1933, v+73 p.
57. "Geometry of two-component spinors," *NAS Proc.*, v. 19, 1933, p. 462-474.
58. "Geometry of four-component spinors," *NAS Proc.*, v. 19, 1933, p. 503-517.
59. "Spinors in projective relativity," *NAS Proc.*, v. 19, 1933, p. 979-989.
60. "Projective differentiation of spinors" (with A. H. Taub), *NAS Proc.*, v. 20, 1934, p. 85-92.
61. "The Dirac equation in projective relativity" (with A. H. Taub and J. von Neumann), *NAS Proc.*, v. 20, 1934, p. 383-388.
62. "Certain aspects of modern geometry—A course of three lectures. . . I. The modern approach to elementary geometry; II. Analysis situs; III. Modern differential geometry," *RI Pamphlets*, v. 31, 1934, p. 207-255.
63. "Spinors," *Wash. Acad. Sci., Journ.*, v. 24, 1934, p. 281-290; *Science*, n.s., v. 80, 1934, p. 415-419.
64. "Formalism for conformal geometry," *NAS Proc.*, v. 21, 1935, p. 168-173.
65. "A conformal wave equation," *NAS Proc.*, v. 21, 1935, p. 484-487.
66. *Geometry of Complex Domains* (with J. W. Givens), (mimeographed lect.), Princeton, 1936, iii+227 p.
67. "Spinors and projective geometry," *Intern. Congress Mathems.*, Oslo, v. 1, 1937, p. 111-127.
68. Reviews of books by Bortolotti, Russell, Vahlen, Lechlas, Stolz and Gmeiner, Huntington, and Birkhoff in *AMS Bull.*, 1905-24.

18. GEORGE DAVID BIRKHOFF

CURRICULUM VITAE.—B. Overisel, Mich. 21 Mar. 1884. He was a student at the Lewis Inst., Chicago (96–02), U. Chicago (02–03; 05–07; Ph.D. 07), Harvard U. (03–05, A.B. 05; A.M. 06). Inst. U. Wisconsin (07–09); preceptor Princeton U. (09–11); prof. (11–12); assist. prof. Harvard U. (12–19; prof. 19– ; acting dean faculty arts and sci. 35–36; dean Sept. 36–). Visiting prof. U. Chicago summer 17; U. California summers 22 and 24; Columbia U. summer 29.

HONORS.—Starred *Amer. Men Sci.* 10. Fellow AAAS 13. Mem. NAS 18; at the age of 34.1 years Birkhoff and Newcomb were the youngest of the 45 mathematicians and mathematical physicists who had been elected members of the Acad. up to 1937, when J. v. Neumann, aged 33.4, was elected. Awarded Quirini Stampalia Prize, of 3000 lire, by the Royal Venice Inst. Sci. Letters and Arts for realizing an important advance in the theory of periodic solutions of differential equations 18; the specific memoirs crowned listed in Bibl. nos. 23 and 27 below. VP AAAS and chm. sect. A 18. VP AMS 19. For. mem. Royal Danish So. Sci. 20. Colloq. Lect. AMS 20; see Bibl. no. 45. Mem. Amer. Phil. So. 21. Ed. AMS *Trans.* 21–24. For. Mem. So. Sci., Göttingen 22. Chm. comm. on revolving fund, NRC 22–36. Hon. Sc.D. Brown U. 23; citation: “youngest professor of mathematics at our oldest university, already recognized throughout America and Europe as a leading discoverer and interpreter in the most fundamental of the sciences” (Faunce). Lect. Lowell Inst. 23 (Bibl. no. 40). First award AMS Bôcher Prize \$200, “for a notable research memoir in analysis,” “Dynamical systems with two degrees of freedom” (Bibl. no. 27) 23. Lect. at Yale U., 2d sem. 23. Harvard exchange prof. with Pomona C., Colorado C., Grinnell C., 1st sem. 24–25. P AMS 25–26. Mem. exec. comm. NRC 25–28. Mem. NRC Fellowship Board 25–36. Lect. U. St. Andrews math. colloq. 26. Cabot research fellow, Harvard U. 26–30. Fourth award of the prize of \$1000 offered by a member of the AAAS for the most notable contribution to the advancement of science reported at the Philadelphia meeting, 26; the award was made for his ret. add. as P AMS, “A mathematical critique of some physical theories” (no. 49). Hon. mem. EMS 27. Hon. Sc.D. U. Wisconsin 27. General lect. Intern. Congress Mathems., Bologna 28 (no. 58). Lect. U. Berlin 28; “Einige Probleme der Dynamik” (no. 56). Mem. comm. eds. *CMP Rend.* 28–35. Corresp. mem., sect. geom., Acad. des Sci., Institut de France 29. For. assoc. Royal Acad. Lincei 29. Corresp. mem. Royal Acad. Sci. of the Institute, Bologna 30. Lect. under the foundation Michonis at Collège de France, Paris, 30; lectures: “Le dernier théorème de géométrie de Poincaré, ses généralisations, et ses applications à la dynamique.” Lectures at L’Institut Henri Poincaré 31; “Sur l’existence de régions d’instabilité en dynamique” (no. 72). Hon. doctorate U. Poitiers 33, on the 500th anniversary of the founding of the U. Hon. Sc.D. Harvard U. 33; citation: “first in our land among masters of mathematics, that great tool of science, greater still in the realm of pure imagination” (Lowell). Awarded a prize of 10,000 lire by the Pontifical Acad. Sci. of the New Lincei for a memoir on systems of solutions of differential equations 33; the memoir is “Nouvelles recherches sur les systèmes dynamiques” (no. 93). Lect. at Phys. Math. So. of Japan, Tokyo, at Tsing-Hua U., Peiping, at Nat. U. of Peiping, at Higher Normal School, Pisa, 34. Hon. doctor U. Paris 36; in the notable and beautiful tribute to Birkhoff by M. Maurain, dean of the faculty of sci., it is mentioned incidentally that he played a prominent rôle in bringing about the establishment of the Institut Henri Poincaré. General lect. Intern. Congress Mathems., Oslo 36; see no. 97. Named one of 70 “pontifical academicians,” who may be of any nationality or religion, in a newly organized Pontifical Acad. Sci. 36; the math. academicians named were U. Amaldi, Birkhoff, Carathéodory, de La Vallée Poussin, Levi-Civita, Picard, Volterra, E. T. Whittaker. Hon. doctor U. Athens on centenary celebration of its founding 37. P AAAS 37; the previous presidents who may be regarded as mathems. were: B. Peirce, W. Chauvenet, J. Lovering, S. Newcomb, H. A. Newton, and E. H. Moore. Officer in the French Legion of Honor, 37. Mem. exec. comm. AAAS 38– . Hon. mem. Amsterdam Math. So. 38; Vinogradov, H. Bohr, Blaschke and Godeaux were elected at the same time. Delegate to dedication of Benjamin Franklin Memorial, of the Franklin Institute 38; add. “Electricity as a fluid”; on this occasion hon. Sc.D. U. Pennsylvania. Lect. at Gregory Tercentenary celebration by the EMS July 38; 4 lects. Hon. LL.D. U. St. Andrews 38.



George D. Birkhoff

1925

BIOGRAPHICAL NOTES.—Prof. Birkhoff is a son of David Birkhoff a physician in Michigan, whose father George Birkhoff came from Middleharnis, Holland, in 1870, and settled in Chicago, Ill. His mother was also of Dutch extraction. During his two years at Harvard, one in college and one in the graduate school, Bôcher and Osgood were in their prime; but during the next two years he worked under Moore, Bolza, and Maschke, in the most inspiring mathematical center in the United States at that time. His dissertation was done quite independently, however.

Newcomb, Hill, and Birkhoff are the three Presidents whose achievements have been most extensively acclaimed internationally. But of these three the latter two have been especially outstanding in mathematical research. Hill was a remarkable instance of a man who was reserved and somewhat of a recluse, who had comparatively few contacts with fellow scientists, and who rarely went to meetings or congresses, but who, nevertheless, wrote extraordinarily original memoirs in the serenity of his home on a farm. His experiences in a classroom were excessively brief and he was not gifted in exposition. Birkhoff, on the other hand, is by nature intensely social; through many trips to Europe, and circumnavigation of the globe, he has been extensively in contact with scholars throughout the world; he is a constant attendant and participant at meetings and congresses, and has been frequently in demand as a writer and speaker on popular themes. In recent administrative gatherings the originality and breadth of his views have been noteworthy. For more than a generation he has been lecturing in university classrooms of the middle west and east. Like Hill he has had a hobby long occupying his attention. He has told us that the formal structure of western music, the riddle of melody, began to interest him in undergraduate days; somewhat intense consideration of the mathematical elements here involved led him to apply his theory also to aesthetic objects such as polygons, tilings, vases, and even poetry. And thus he was led to publish his volume *Aesthetic Measure* (no. 79; see also nos. 58, 66, 69, 76).

From the Bibliography it will be observed that Birkhoff's main research has been in the fields of differential and difference equations, calculus of variations, relativity, dynamical systems and stability, the problem of three bodies, and Poincaré's geometric theorem. This last theorem of Poincaré was announced in his posthumous paper "Sur un théorème de géométrie" (CMP, *Rend.*, v. 33, 1912, p. 375-407). It is of great importance, in particular for the restricted problem of three bodies; but having, after long-continued efforts, succeeded in treating only a great variety of special cases, he gave out the theorem for the consideration of other mathematicians. In a simple form the theorem may be stated as follows: "Suppose that a continuous, one-to-one transformation T takes the ring R , formed by two concentric circles C_a and C_b of radii a and b respectively ($a > b > 0$), into itself in such a way as to advance the points of

C_a in the positive sense and the points of C_b in the negative sense, and at the same time to preserve areas. Then there are at least two invariant points." Birkhoff's proof, published in less than a year (see Bibl. nos. 15, 30, 53, and the generalization in no. 41), was possible because of the mathematical tools which he had been employing in earlier work.

A similar experience involving his two earlier papers (nos. 33, 54) and prepublication knowledge of a paper of J. von Neumann (*NAS Proc.*, v. 18, p. 70-82) who proved the existence of the ergodic theorem in the mean, of great importance in physical applications, led Birkhoff, by a stroke of genius to prove what Hopf (in *Ergodentheorie*, Berlin, 1937) calls the individual ergodic theorem, which is of much greater interest to the mathematician (Bibl. nos. 68, 73). The ergodic theorem may be stated as follows: "If $Z_{\alpha,\beta}(P;M)$ denotes the relative sojourn of the moving point $P_t(P_0=P)$ in M in the time interval $\alpha \leq t \leq \beta$ (i.e. it is the length of this sojourn divided by $\beta - \alpha$), then $Z_{\alpha,\beta}(P;M) \rightarrow Z(P;M)$ as $\beta - \alpha \rightarrow +\infty$, for all P of Ω except for a set of measure zero."

But Birkhoff's great contributions to stability in dynamics were not only in the two directions just indicated, but also in discussions of other important papers and in the notable volume of his *Colloq. Lects.* before the AMS (see nos. 23, 27, 33, 41, 45, 46, 51, 54, 71, 87). His doctoral dissertation (no. 6) and paper 39 contain the first complete solution of the problem of asymptotic developments of solutions of differential equations and applications to systematic treatments of boundary value problems. Papers 11 and 61 presented important contributions to the existence theory of solutions of linear difference equations, and an entirely new method for a complete investigation of fundamental sets of solutions of difference equations; a new way was opened up for a complete solution of analogous problems for differential and more general equations. Papers 16, 17, 21 contain a complete solution of the famous Riemann problem concerning differential equations, and an extension to various more general situations. These notes suffice to indicate that Birkhoff has been attacking great problems and has already produced many inspired solutions.

The following 38 students have prepared their theses for the doctorate in association with Professor Birkhoff at Princeton, Yale, and Harvard U., and Radcliffe C., 1911-37: R. D. Carmichael (at Princeton), K. P. Williams (at Princeton), J. Slepian, R. B. Robbins, L. T. Wilson, P. M. Batchelder, R. W. Brink, N. Miller, H. C. M. Morse, C. N. Reynolds, Jr. (under Bôcher and Birkhoff), H. J. Ettlenger, J. L. Walsh, C. R. Adams, R. E. Langer, Eleanor Pairman (Mrs. B. H. Brown), C. A. Garabedian, B. Z. Linfield, F. H. Murray, J. L. Holley, D. V. Widder, H. Betz (at Yale), H. W. Brinkmann, L. E. Ward, B. O. Koopman, M. H. Stone, I. M. Sheffer, C. J. Coe, J. J. L. Hinrichsen, C. N. Liu, C. B. Morrey, Jr., T. L. Smith, H. Whitney, Mrs. Frances (Thorndike) Cope (at Radcliffe C.), D. C. Lewis, G. B. Price, F. H. Steen, A. S. Galbraith, O. E. Lancaster.

His son Garrett is a young mathematician of very exceptional promise.

SOURCES.—*Annuario della Pontificia Accademia delle Scienze*, v. 1, 1936–1937, Città del Vaticano, 1937, portrait. *Who's Who in Amer.*, v. 19. *Amer. Men Sci.*, 5th ed. H. S. White, *Scientific Mo.*, v. 44, 1937, portrait. *Annales de l'Université de Paris*, Nov.–Dec. 1936. E. J. Moulton, *AMM*, v. 44, 1937, portrait. *Harvard C. Class of 1905, Reports of 1911, 1925, 1930*. Personal information.

BIBLIOGRAPHY

1. "On the integral divisors of $a^n - b^n$ " (with H. S. Vandiver), *AM*, s. 2, v. 5, 1904, p. 173–180.
2. "A theorem concerning uniform convergence," *AM*, s. 2, v. 6, 1905, p. 90–92.
3. "General mean value and remainder theorems with applications to mechanical differentiation and quadrature," *AMS Trans.*, v. 7, 1906, p. 107–136.
4. "Note on certain quadratic number systems for which factorization is unique," *AMM*, v. 13, 1906, p. 156–159.
5. "On the asymptotic character of the solutions of certain linear differential equations containing a parameter," *AMS Trans.*, v. 9, 1908, p. 219–231.
6. "Boundary value and expansion problems of ordinary linear differential equations," *AMS Trans.*, v. 9, 1908, p. 373–395. Nos. 5 and 6 a doctoral diss.
7. "Existence and oscillation theorem for a certain boundary value problem," *AMS Trans.*, v. 10, 1909, p. 259–270.
8. "Singular points of ordinary linear differential equations," *AMS Trans.*, v. 10, 1909, p. 436–470.
9. "A simplified treatment of the regular singular point," *AMS Trans.*, v. 11, 1910, p. 199–202.
10. "On the solutions of ordinary linear homogeneous differential equations of the third order," *AM*, s. 2, v. 12, 1911, p. 103–127.
11. "General theory of linear difference equations," *AMS Trans.*, v. 12, 1911, p. 243–284.
12. "Note on the expansion of the Green's function," *MA*, v. 72, 1912, p. 292–294.
13. "A determinant formula for the number of ways of coloring a map," *AM*, s. 2, v. 14, 1912, p. 42–46.
14. "Quelques théorèmes sur le mouvement des systèmes dynamiques," *SMF Bull.*, v. 40, 1912, p. 305–323.
15. "Proof of Poincaré's geometric theorem," *AMS Trans.*, v. 14, 1913, p. 14–22.
French trans. by Janet: "Démonstration du dernier théorème de géométrie de Poincaré," *SMF Bull.*, v. 42, 1914, p. 1–12.
16. "A theorem on matrices of analytic functions," *MA*, v. 74, 1913, p. 122–133; Berichtigung, p. 461.
17. "Equivalent singular points of ordinary linear differential equations," *MA*, v. 74, 1913, p. 134–139.
18. "The reducibility of maps," *AJM*, v. 35, 1913, p. 115–128.
19. "Note on the expansion problems of ordinary linear differential equations," *CMP Rend.*, v. 36, 1913, p. 115–126.
20. "Note on the gamma function," *AMS Bull.*, v. 20, 1913, p. 1–10.
21. "The generalized Riemann problem for linear differential equations and the allied problems for linear difference and q -difference equations," *AACAS Proc.*, v. 49, 1913, p. 521–568.
22. "On a simple type of irregular singular point," *AMS Trans.*, v. 14, 1913, p. 462–476.
23. "The restricted problem of three bodies," *CMP Rend.*, v. 39, 1915, p. 265–334.
24. "An elementary double inequality for the roots of an algebraic equation having greatest absolute value," *AMS Bull.*, v. 21, 1915, p. 494–495.
25. "Theorem concerning the singular points of ordinary linear differential equations," *NAS Proc.*, v. 1, 1915, p. 578–581.
26. "Infinite products of analytic matrices," *AMS Trans.*, v. 17, 1916, p. 386–404.

27. "Dynamical systems with two degrees of freedom," *AMS Trans.*, v. 18, 1917, p. 199–300; brief summary in *NAS Proc.*, v. 3, 1917, p. 314–316.
28. "Sur une généralisation de la série de Taylor," *CR Paris*, v. 164, 1917, p. 942–945.
29. "A theorem on series of orthogonal functions with an application to Sturm-Liouville series," *NAS Proc.*, v. 3, 1917, p. 656–659.
30. "Sur la démonstration directe du dernier théorème de Henri Poincaré par M. Dantzig," *DB*, s. 2, v. 42, 1918, p. 41–43. [Showing that Mr. Dantzig had published an interesting but fallacious attempt at a proof; Prof. E. B. Wilson had earlier independently considered and rejected the same "proof."]
31. "The scientific work of Maxime Bôcher," *AMS Bull.*, v. 25, 1919, p. 197–215.
32. "Recent advances in dynamics," *Science*, v. 51, 1920, p. 51–55. Add. VP AAAS and chm. Sect. A 30 Dec. 1919.
33. "Surface transformations and their dynamical applications," *Acta M.*, v. 43, 1920, p. 1–119.
34. "An elementary treatment of Fourier series," *AMM*, v. 28, 1921, p. 200–203.
35. "Invariant points in function space" (with O. D. Kellogg), *AMS Trans.*, v. 23, 1922, p. 96–115.
36. "Circular plates of variable thickness," *Phil. Mag.*, v. 43, 1922, p. 953–962.
37. "Celestial mechanics" (with E. W. Brown, A. O. Leuschner, H. N. Russell), *NRC Bull.*, v. 4, 1922, p. 1–22. Report of Comm. on Celestial Mechanics.
38. *Relativity and Modern Physics* (with cooperation of R. E. Langer), Cambridge, 1923, 11+283 p.; 2d ed., 1927.
39. "The boundary problems and developments associated with a system of ordinary linear differential equations of first order" (with R. E. Langer), *AAcAS Proc.*, v. 58, 1923, p. 49–128.
40. *The Origin, Nature, and Influence of Relativity* (Lowell Inst. Lects.), New York, 1925, 10+185 p. A revision of arts. in *Scientific Mo.*, v. 18, 1924, p. 225–238, 408–421, 517–528, 616–624; v. 19, 1924, p. 18–29, 180–187.
41. "An extension of Poincaré's last geometric theorem," *Acta M.*, v. 47, 1925, p. 297–311.
42. "Stabilità e periodicità nella dinamica," *P. Mat.*, s. 4 v. 6, 1926, p. 262–271.
43. "Sur la signification des équations canoniques de la dynamique," *CR Paris*, v. 183, 1926, p. 516–519; errata, p. 1144.
44. "Über gewisse Zentralbewegungen dynamischer Systeme," *GN*, 1926, p. 81–92.
45. *Dynamical Systems* (*AMS Colloq. Pub.*, v. 9), New York, 1927, 8+295 p.
46. "Stability and the equations of dynamics," *AJM*, v. 49, 1927, p. 1–38.
47. "A theory of matter and electricity," *NAS Proc.*, v. 13, 1927, p. 160–165.
48. "The hydrogen atom and the Balmer formula," *NAS Proc.*, v. 13, 1927, p. 165–169.
49. "A mathematical critique of some physical theories," *AMS Bull.*, v. 33, 1927, p. 165–181. AMS ret. P add. 30 Dec. 1926.
50. "A gratifying computation. Princeton, reckoned among country's three chief mathematical centers, faces opportunity of assuming lead in this field," *Princeton Alumni Weekly*, v. 27, 1927, p. 882.
51. "On the periodic motions of dynamical systems," *Acta M.*, v. 50, 1927, p. 359–379.
52. "Physics and mathematics" (with T. Lyman), *The Choice of a Field of Concentration* [at *Harvard Univ.*], *Harvard Crimson*, 1927, p. 24–25; 2d ed. 1929, p. 38–39.
53. "A remark on the dynamical rôle of Poincaré's last geometric theorem," *Szeged Acta*, v. 4, 1928, p. 6–11. [Lecture at U. Szeged 8 June 1928.]
54. "Structure analysis of surface transformations" (with P. A. Smith), *Journ. d. Mathém.*, s. 9, v. 7, 1928, p. 345–379.
55. "Newton's philosophy of gravitation with special reference to modern relativity ideas," *Sir Isaac Newton 1727–1927. A Bicentenary Evaluation of his Work*, Baltimore, 1928, p. 51–64.
56. "Einige Probleme der Dynamik," *DMV Jahr.*, v. 38, 1929, p. 1–16.
57. "Science and spiritual perspective." *Century Mag.*, v. 118, 1929, p. 156–165.
58. "Quelques éléments mathématiques de l'art." *Intern. Congress Mathems.*, Bologna, v. 1, 1929, p. 315–333.

59. "Démonstration d'un théorème élémentaire sur les fonctions entières," *CR Paris*, v. 189, 1929, p. 473-475.
60. "Divergente Reihen und singuläre Punkte gewöhnlicher Differentialgleichungen," *PA Sitz.*, 1929, p. 171-183.
61. "Formal theory of irregular linear difference equations," *Acta M.*, v. 54, 1930, p. 205-246.
62. "Divergent series and singular points of ordinary differential equations" (with F. R. Bamforth), *AMS Trans.*, v. 32, 1930, p. 114-146.
63. "On the number of ways of colouring a map," *EMS Proc.*, s. 2, v. 2, 1930, p. 83-91.
64. "A new approach to elementary geometry" (with Ralph Beatley), *Nat. Council Teachers Math., Yearbook*, 1930, p. 86-95.
65. "Une généralisation à n dimensions du dernier théorème de géométrie de Poincaré," *CR Paris*, v. 192, 1931, p. 196-198.
66. "A mathematical approach to aesthetics," *Scientia*, 1931, p. 133-146.
67. "Proof of a recurrence theorem for strongly transitive systems," *NAS Proc.*, v. 17, 1931, p. 650-655.
68. "Proof of the ergodic theorem," *NAS Proc.*, v. 17, 1931, p. 656-660.
69. "Polygonal forms," *Nat. Council Teachers Math., Yearbook*, 1931, p. 165-195.
70. "A new criterion of stability," *Intern. Congress Mathems.*, Bologna, v. 5, 1931, p. 5-13.
71. "Sur quelques courbes fermées remarquables," *SMF Bull.*, v. 60, 1932, p. 1-26.
72. "Sur l'existence de régions d'instabilité en dynamique," *IHP Ann.*, v. 2, 1932, p. 369-386.
73. "Recent contributions to the ergodic theory" (with B. O. Koopman), *NAS Proc.*, v. 18, 1932, p. 279-282.
74. "A set of postulates for plane geometry, based on scale and protractor," *AM*, s. 2, v. 33, 1932, p. 329-345; p. 788.
75. "Probability and physical systems," *AMS Bull.*, v. 38, 1932, p. 361-379.
76. "A mathematical theory of aesthetics and its application to poetry and music—A course of lectures. . . I. Relation of the theory to earlier aesthetic theories; II. The musical quality in poetry; III. The diatonic chords; IV. Harmony; V. Melody," *RI Pamphlets*, v. 19, 1932, p. 189-342.
77. "Minute on the life and services of Professor Oliver Dimon Kellogg" (with J. L. Coolidge and G. W. Pierce), *Harvard U. Gazette*, v. 28, 1932, p. 38-39.
78. "Analytic theory of singular difference equations" (with Trjitzinsky), *Acta M.*, v. 60, 1933, p. 1-89.
79. *Aesthetic Measure*, Cambridge, Mass., 1933, 13+225 p.
80. *Geometry* (with Ralph Beatley), [Boston, 1933], 5+159 p.
81. "Some remarks concerning Schrödinger's wave equation," *NAS Proc.*, v. 19, 1933, p. 339-344; correction, p. 475.
82. "The mathematical work of Oliver Dimon Kellogg," *AMS Bull.*, v. 39, 1933, p. 171-177.
83. "On the periodic motion near a given periodic motion of a dynamical system" (with D. C. Lewis, Jr.), *Annali M.*, s. 4, v. 12, 1933, p. 117-133.
84. "Quantum mechanics and asymptotic series," *AMS Bull.*, v. 39, 1933, p. 681-700.
85. "Mathematics: quantity and order," *Science Today. The Scientific Outlook on World Problems explained by leading Exponents of Modern Scientific Thought planned and arranged by the late Sir J. Arthur Thomson . . . ed. by J. G. Crowther*, London, 1934, p. 293-317. Amer. ed. *Science for a New World. The Scientific Outlook . . .*, New York, 1934.
86. "Eliakim Hastings Moore (1862-1932)," *AAcAS Proc.*, v. 69, 1934, p. 527-528.
87. "Sur le problème restreint des trois corps," *SNSP Annali*, s. 2, v. 4, 1935, p. 267-306; v. 5, 1936, p. 9-50.
88. "Generalized minimax principle in the calculus of variations" (with M. R. Hestenes), *NAS Proc.*, v. 21, 1935, p. 96-99.
89. "Natural isoperimetric conditions in the calculus of variations" (with M. R. Hestenes), *NAS Proc.*, v. 21, 1935, p. 99-102.
90. "Natural isoperimetric conditions in the calculus of variations" (with M. R. Hestenes), *DMJ*, v. 1, 1935, p. 198-286.

91. "Stability in causal systems" (with D. C. Lewis, Jr.), *Philosophy of Sci.*, v. 2, 1935, p. 304-333.
92. "Generalized minimax principle in the calculus of variations" (with M. R. Hestenes), *DMJ*, v. 1, 1935, p. 413-432.
93. "Nouvelles recherches sur les systèmes dynamiques," *NAL Mem.*, s. 3, v. 1, 1935, p. 85-216.
94. "Note sur la stabilité en dynamique," *Journ. d. Mathém.*, s. 9, v. 15, 1936, p. 339-344.
95. Reports as Acting Dean and Dean of the Faculty of Arts and Sci. of Harvard U., *Official Register of Harvard U.*, v. 33, 1936, no. 4, p. 33-45; v. 34, 1937, no. 11, p. 29-41; v. 35, 1938, no. 4, p. 37-48.
96. "The American Association for the Advancement of Science" [Message as President on a circular descriptive of the organization], Wash., 1937, 1 p.
97. "The foundations of quantum mechanics," *Intern. Congress Mathems.*, Oslo, v. 1, 1937, p. 207-225. One of the long invited addresses at the Congress.
98. Reviews of books by Poincaré; E. H. Moore, Wilczynski, and Mason; Blumenthal; Whittaker; books on relativity by Blumenthal, ed., H. Weyl, Einstein trans. by Lawson, R. D. Carmichael, Angerbach, Whitehead, and Brouwer; and Landau in *AMS Bull.*, 1911-1929; by E. B. Edwards in *Tech. Studies in Field of Fine Arts*, 1932; by Robb and Courant in *Science*, 1936, and 1937.

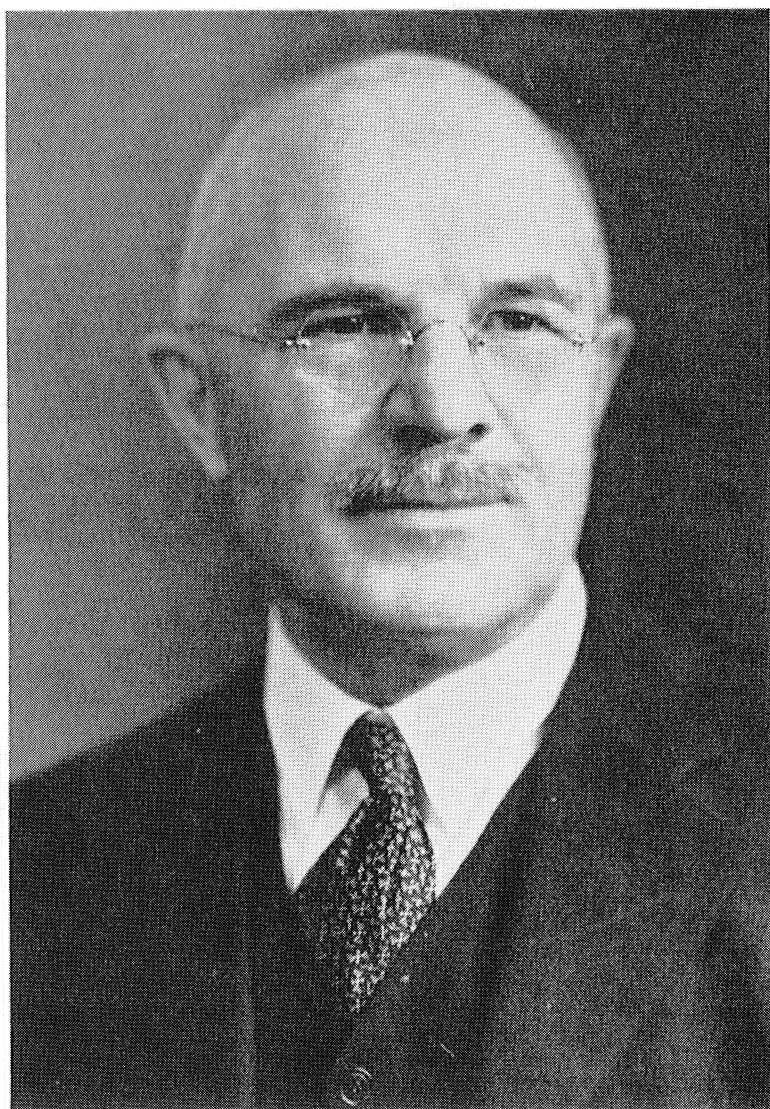
19. VIRGIL SNYDER

CURRICULUM VITAE.—B. Dixon, Ia. 9 Nov. 1869. Educ. Iowa State C. (86-89; Sc.B. 89); Cornell U. (90-92), Brooks fellow from Cornell U. at U. Göttingen (92-94; Ph.D. Dec. 94). Instr. math. Cornell U. (95-03; assist. prof. 03-10; prof. 10-38; prof. emeritus 38-). Semi-centennial prof. U. California, summer 18.

HONORS.—Starred *Amer. Men Sci.* 06. Ed. *AMS Bull.* 08-20. VP AMS 16. Fellow AACAS 19. Fellow in Italy on Heckscher Foundation 21-22, 28-29. Hon. D. U. Padua on the celebration of the 700th anniversary of its founding 22. Del. NRC and Intern. Math. Union, Intern. Congress Mathems. Toronto 24; Bologna 28; Zürich 32. Chm. NRC Comm. on Rational Transformations 24-34. AMS nominee mem. Div. Phys. Sci. NRC 26-29. P AMS 27-28; ret. P add. "The problem of the cubic variety in S_4 " (Bibl. no. 70). Del. U. S. Govt. to Intern. Congress Mathems. Bologna 28; Oslo 36.

BIOGRAPHICAL NOTES.—Prof. Snyder is a son of Ephraim Snyder, a farmer and pioneer in the state of Iowa. He is descended from Johannes Schneider from Swabia, Germany, who first settled in Bethel, Pa., in 1777. His mother, Elisa Jane Randall, a native of New England and a school teacher, was of English-French descent.

During more than forty years at Cornell U., Prof. Snyder has devoted himself whole-heartedly, and with high idealism, to improving the teaching of mathematics, to promoting the welfare of his students and guiding them into research, and to carrying on his own original work in the fields of geometry of the line and sphere, configurations of ruled surfaces, and birational transformations. For the College Entrance Exam. Board he was chm. of the comm. of examiners in 1912, chief examiner in geometry 1912-14, and chief reader, 1912-17, 1919-23, 1925-32. He and J. H. Tanner were joint eds. of plane and solid geometries (no. 38); he was joint author with J. McMahan and with J. I. Hutchinson of three different works on the calculus (nos. 6, 16, 45); and with C. H. Sisam of an analytic



Virgil Snyder

1935

geometry of space (no. 52). Turning to activities in the field of research, Prof. Snyder was an assist. ed. *AMS Bull.*, Feb. 1904–Dec. 1907, and a member of the comm. of pub. 1908–20. His paper no. 17 inspired Prof. R. P. Baker of Iowa to make a model of the quintic scroll, and the first purchaser of a copy was Mittag-Leffler who keenly appreciated the elegance of the results. Nos. 18, 19, 20 were written in ignorance of A. Wiman's Lund diss. *Klassifikation af Regelytorna af sjette Graden*, 1892 which inspired nos. 24, 26, where were listed the only two cases (as later proved by Wiman *Acta M.*, v. 57, 1931) overlooked by Wiman. In his paper on twisted curves whose tangents belong to a linear complex (no. 28) there is a theorem, contradicting one published by C. P. Steinmetz (1892), featured by Zindler in *Encyk. d. Math. Wiss.*, v. 3.2, p. 1024–5. There are more than fifty references to Snyder's work in this v. In no. 31, Snyder gives a proof of the interesting result that if two non-singular plane quartic curves are in (1, 1) correspondence they are projectively equivalent—a result duly set forth in the *Encyklopädie*; in no. 32 this is generalized to apply to all curves of order n , and of certain genus. But years later, proofs for part of the cases were given by Severi, Segre, Kapferer, and Wirtinger. The paper on the construction of plane curves of given order and genus, having distinct double points (no. 33) is most frequently cited by others. But the one written with Sharpe on certain types of involutorial space transformations (no. 60) is probably the most important. Prof. Snyder's most useful tool for the research worker, a very notable aid to the student in the field of rational transformations and related topics, is the large report (396+84 p.) on *Selected Topics in Algebraic Geometry* (nos. 69, 77) which he, as chm., and his five associates, A. B. Coble, A. Emch, S. Lefschetz, F. R. Sharpe, and C. H. Sisam, prepared for the NRC; it makes a report on 3585 books and papers (see reviews by T. R. Hollcroft in *AMS Bull.*, v. 38 and v. 42; by Van der Waerden in *Zentralblatt f. Math.*, v. 10). A. H. Black and L. A. Dye cooperated in preparing the supplementary part of the report.

Many developments of Prof. Snyder's work were carried out by the following 39 students who prepared their doctoral dissertations under his direction at Cornell U. 1902–37: P. Field, C. L. E. Moore, O. P. Akers, E. C. Colpitts, C. H. Sisam, Anna L. Van Benschoten, J. V. McKelvey, Mrs. Helen B. Owens, P. P. Boyd, F. M. Morgan, A. Helen Tappen, L. C. Cox, J. V. DePorte, T. R. Hollcroft, Anna M. Howe, J. O. Osborn, Marian M. Torrey, Fay Farnum, Hazel E. Schoonmaker, H. A. Davis, Ethel I. Moody, Mrs. Evelyn C. Rusk, H. N. Hubbs, W. R. Hutcherson, C. C. Torrance, A. H. Black, J. M. Clarkson, E. J. Purcell, Augustus Sisk, Mrs. Helen S. Adams, Roberta F. Johnson, J. A. Hyden, C. R. Wylie, Jr., Gertrude K. Blanch, L. H. Chambers, Harriet F. Montague, L. H. Bowen, R. A. Harrison, J. E. Ikenberry.

Prof. Snyder is a lover of travel, also intensely interested in politics.

His favorite recreation is mountain climbing and going on long hikes with Mrs. Snyder as companion.

SOURCES.—*Who's Who in Amer.*, v. 19. *Amer. Men Sci.*, 5th ed. "Lebenslauf" in doctoral diss. (Bibl. no. 1). Personal information.

BIBLIOGRAPHY

1. *Ueber die linearen Complexe der Lie'schen Kugelgeometrie*, Göttingen, 1895, iv+48 p. Doctoral diss.
2. "Lines common to four linear complexes," *AMS Bull.*, v. 3, 1897, p. 247–250.
3. "Criteria for nodes in Dupin's cyclides, with a corresponding classification," *AM*, v. 11 1897, p. 137–147.
4. "Condition that the line common to $n-1$ planes in an n -space may pierce a given quadric surface in the same space," *AMS Bull.*, v. 4, 1897, p. 68–73.
5. "Geometry of some differential expressions in hexaspherical coordinates," *AMS Bull.*, v. 4, 1898, p. 144–154.
- 5A. "On the Steiner points of Pascal's hexagon," *AMS Bull.*, v. 4, p. 441–442.
6. *Treatise on Differential Calculus* (with J. McMahon), New York, etc., 1898, xiv+337 p.
7. "Asymptotic lines on ruled surfaces having two rectilinear directrices," *AMS Bull.*, v. 5, 1899, p. 343–353.
8. "Lines of curvature on annular surfaces having two spherical directrices," *AJM*, v. 22, 1900, p. 96–100.
9. *Geometric Construction of the Elliptic Integral of the Second Kind*, Halle, 1900, 12 p.
10. "On cyclical quartic surfaces in space of n dimensions," *AMS Bull.*, v. 6, 1900, p. 194–198.
11. "On the geometry of the circle," *AMS Bull.*, v. 6, 1900, p. 319–322, 464.
12. "On some invariant scrolls in collineations which leave a group of five points invariant," *AJM*, v. 22, 1900, p. 253–258.
13. "On a special form of annular surfaces," *AJM*, v. 23, 1901, p. 166–172.
14. "On a system of plane curves having factorable parallels," *AMS Bull.*, v. 7, 1901, p. 299–302.
15. "On the forms of quintic scrolls," *AMS Bull.*, v. 8, 1902, p. 293–296.
16. *Differential and Integral Calculus* (with J. I. Hutchinson), New York, etc., 1902, xvi+320 p.
17. "On the quintic scroll having three double conics," *AMS Bull.*, v. 9, 1903, p. 236–242.
18. "On the forms of unicursal sextic scrolls," *AJM*, v. 25, 1903, p. 59–84.
19. "On the forms of sextic scrolls of genus one," *AJM*, v. 25, 1903, p. 85–96.
20. "On the forms of sextic scrolls of genus greater than one," *AJM*, v. 25, 1903, p. 261–268.
21. "On developable and tubular surfaces having spherical lines of curvature," *AMS Bull.*, v. 11, 1904, p. 1–6.
22. "On the forms of sextic scrolls having a rectilinear directrix," *AJM*, v. 27, 1905, p. 77–102.
23. "On the quintic scroll having a tacnodal or oscnodal conic," *AMS Bull.*, v. 11, 1905, p. 182–186.
24. "On the forms of sextic scrolls having no rectilinear directrix," *AJM*, v. 27, 1905, p. 173–188.
25. "Surfaces generated by conics cutting a twisted quartic curve and an axis in the plane of the conic," *AMS Bull.*, v. 12, 1906, p. 383–387.
26. "On certain unicursal twisted curves," *AJM*, v. 28, 1906, p. 237–242.
27. "The New Haven colloquium," *AMS Bull.*, v. 13, 1906, p. 71–74.
28. "Twisted curves whose tangents belong to a linear complex," *AJM*, v. 29, 1907, p. 279–288.
29. "On a special algebraic curve having a net of minimum adjoint curves," *AMS Bull.*, v. 14, 1907, p. 70–74.

30. "Plane quintic curves which possess a group of linear transformations," *AJM*, v. 30, 1908, p. 1-9.
31. "Normal curves of genus 6, and their groups of birational transformations," *AJM*, v. 30, 1908, p. 325-336.
32. "On the range of birational transformation of curves of genus greater than the canonical form," *AJM*, v. 30, 1908, p. 337-346.
33. "Construction of plane curves of given order and genus, having distinct double points," *AMS Bull.*, v. 15, 1908, p. 1-4.
34. "Surfaces derived from the cubic variety having nine double points in four-dimensional space." *AMS Trans.*, v. 10, 1909, p. 71-78.
35. "Surfaces and congruences derived from the cubic variety having a double line in four-dimensional space," *AJM*, v. 31, 1909, p. 147-166.
36. "The Princeton colloquium," *AMS Bull.*, v. 16, 1909, p. 105-106.
37. "Infinite discontinuous groups of birational transformations which leave certain surfaces invariant," *AMS Trans.*, v. 11, 1910, p. 15-24.
38. Ed. (with J. H. Tanner) of geometries by Hart and Feldman, (a) *Plane Geometry*, 1910, viii+305 p.; (b) *Plane and Solid Geometry*, 1911, viii+488 p.; (c) *Solid Geometry*, 1912, xvi+188 p.; New York.
39. "Surfaces invariant under infinite discontinuous birational groups defined by line congruences," *AJM*, v. 32, 1910, p. 177-185.
40. "Conjugate line congruences contained in a bundle of quadric surfaces," *AMS Trans.*, v. 11, 1910, p. 371-387.
41. "The Königsberg meeting of the Deutsche Mathematiker-Vereinigung," *AMS Bull.*, v. 17, 1911, p. 172-176.
42. "An application of a (1, 2) quaternary correspondence to the Kummer and Weddle surfaces," *AMS Trans.*, v. 12, 1911, p. 354-366.
43. "Entrance to college by college entrance board examinations," *ICT Math., Amer. Report*, Comm. no. VII, 1911, p. 28-39.
44. "The involutorial birational transformation of the plane, of order 17," *AJM*, v. 33, 1911, p. 327-336.
45. *Elementary Textbook on the Calculus* (with J. I. Hutchinson), New York, etc., 1912, 384 p.
46. "The Karlsruhe meeting of the German Mathematical Society," *AMS Bull.*, v. 18, 1912, p. 169-174.
47. "Periodic quadratic transformations in the plane," *AM*, s. 2, v. 13, 1912, p. 140-148.
48. "The fifth international congress of mathematicians, Cambridge, 1912," *AMS Bull.*, v. 19, 1912, p. 107-130; 1913, p. 175-191.
49. "The Münster meeting of the Deutsche Mathematiker-Vereinigung," *AMS Bull.*, v. 19, 1913, p. 191-197.
50. "Algebraic surfaces invariant under an infinite discontinuous group of birational transformations" (2d paper), *AMS Trans.*, v. 14, 1913, p. 105-108.
51. "The Vienna meeting of the Deutsche Mathematiker-Vereinigung," *AMS Bull.*, v. 20, 1913, p. 120-131.
52. *Analytic Geometry of Space* (with C. H. Sisam), New York, 1914, xi+289 p.
53. "Birational transformations of certain quartic surfaces" (with F. R. Sharpe), *AMS Trans.*, v. 15, 1914, p. 266-276.
54. "Birational transformations of the cubic variety in four-dimensional space," *CMP Rend.*, v. 38, 1914, p. 344-352.
55. "Certain quartic surfaces belonging to infinite discontinuous cremonian groups" (with F. R. Sharpe), *AMS Trans.*, v. 16, 1915, p. 62-70.
56. "The Cambridge colloquium," *AMS Bull.*, v. 23, 1916, p. 81-88, 164.
57. "Mathematics at an Italian technical school," *AMS Bull.*, v. 23, 1916, p. 149-151.
58. "Types of (2, 2) point correspondences between two planes" (with F. R. Sharpe), *AMS Trans.*, v. 18, 1917, p. 402-414.

59. "Space involutions defined by a web of quadrics" (with F. R. Sharpe), *AMS Trans.*, v. 19, 1918, p. 275-290.
60. "Certain types of involutorial space transformations" (with F. R. Sharpe), *AMS Trans.*, v. 20, 1919, p. 185-202; v. 21, 1920, p. 52-78.
61. "The construction of algebraic correspondences between two algebraic curves" (with F. R. Sharpe), *AMS Trans.*, v. 22, 1921, p. 31-40.
62. "Un'involuzione d'ordine due dell' S_3 appartenente alla varietà cubica generale," *Giorn. M.*, v. 61, 1923, p. 125-128.
63. "The (1, 2) correspondence associated with the cubic space involution of order two" (with F. R. Sharpe), *AMS Trans.*, v. 25, 1923, p. 1-12.
64. "On the types of monoidal involutions," *AM*, s. 2, v. 25, 1924, p. 279-284.
65. "Problems in involutorial transformations of space," *AMS Bull.*, v. 30, 1924, p. 101-124.
66. "Further types of involutorial transformation which leave each cubic surface of a web invariant," *AJM*, v. 46, 1924, p. 131-141.
67. "Non-monoidal involutions which leave each monoid of a web invariant," *AM*, s. 2, v. 26, 1925, p. 165-172.
68. "On a problem in closure," *AMS Bull.*, v. 33, 1927, p. 39-43.
69. "Multiple correspondences between two planes"; "Involutions on rational curves"; "Correspondences on non-rational curves"; "(1, 2) correspondences between S'_r and S_r , $r > 2$ "; "Multiple correspondence in space and hyperspace," *Selected Topics in Algebraic Geometry* (NRC Bull. no. 63), 1928, p. 122-196, 227-251, 257-274.
70. "The problem of the cubic variety in S_4 ," *AMS Bull.*, v. 35, 1929, p. 607-642. AMS ret. P add. 29 Aug. 1929.
- 70A. "Line Geometry," *Encycl. Brit.*, 14th ed., v. 14, 1929, p. 157-159.
71. "The simplest involutorial transformation contained multiply in a line complex," *AMS Bull.*, v. 36, 1930, p. 89-93.
72. "On an involutorial transformation found by Montesano," *AM*, s. 2, v. 31, 1930, p. 335-343.
73. "Involutorial space transformations contained multiply in a linear line complex," *Intern. Congress Mathems.*, Bologna, v. 4, 1931, p. 13-21.
74. "Generating involutions of infinite discontinuous Cremona groups of S_4 which leave a general cubic variety invariant" (with M. Lehr), *AJM*, v. 53, 1931, p. 186-194.
75. "Two involutorial transformations, of orders 11 and 9, associated with null reciprocities" (with H. E. Schoonmaker), *AJM*, v. 54, 1932, p. 299-304.
76. "On a series of involutorial Cremona transformations of space defined by a pencil of ruled surfaces," *AMS Trans.*, v. 35, 1933, p. 341-347.
77. "Curved and ruled surfaces"; "Systems of lines in S_n ; irregular surfaces"; "Cremona transformations"; "Multiple correspondences," *Selected topics in algebraic geometry, II. Supplemental Report . . .* (NRC Bull., no. 96), 1934, p. 1-13, 25-36, 37-72.
78. "An involutorial line transformation determined by a bilinear congruence of twisted elliptic quartic curves" (with J. M. Clarkson), *AMS Bull.*, v. 40, 1934, p. 441-448.
79. "Some recent contributions to algebraic geometry," *AMS Bull.*, v. 40, 1934, p. 673-687.
80. "The Veneroni transformation in S_n " (with E. C. Rusk), *AMS Bull.*, v. 42, 1936, p. 585-592.
81. "On a system of involutorial Cremona transformations defined by a pencil of quadric surfaces," *Intern. Congress Mathems.*, Oslo, v. 2, 1937, p. 150-151.
82. "A series of involutorial Cremona transformations in S_n belonging multiply to a non-linear line complex" (with E. C. Rusk), *AJM*, v. 59, 1937, p. 775-782.
83. Reviews of books by Lefschetz, Scott, Hudson, Hessenberg, Jordan and Porter, and Klein in *AMM*, 1925-33; by Koenigs, Graf and Gubler, Stahl, Cesàro, Study, C. H. Müller and Presler, Schilling, Enriques, Haentzschel, Ludwig, Arendt, Meyer, Willis, Schüssler, Wilczynski, Nielsen, Schütte, Sturm, Scheibner, Schoenflies, Loria, E. Müller, Wilson, Doehlemann, Seferian, Salmon, Church and Bartlett, Hauck, Low, Auerbach, Hjelmlev, Timerding, Schmid, Armstrong,

Grossmann, H. W. Miller, Ince, Hedrick, Hudson, Hatton, Klein, v. Sanden, Comessatti, Mukhopadhyaya, Julia, d'Ocagne, Graustein, Ciani, Edge, Coolidge, F. Morley and F. V. Morley, Godeaux, and a review of 1906 Mathematical Tripos in *AMS Bull.*, 1897–1935.

20. EARLE RAYMOND HEDRICK

CURRICULUM VITAE.—B. Union City, Ind. 27 Sept. 1876. Prepared at high school in Ann Arbor (91–92) for entering U. Michigan (92–96; A.B. 96). Instr. math. in high school, Sheboygan, Wis. 96–97. Student at Harvard U. (97–99; A.M. 98). Parker fellow from Harvard U. at U. Göttingen (99–01; Ph.D. Feb. 01); at École Normale Supérieure, Paris, 01. Instr. math. Yale Sci. School (01–03). Prof. math. U. Missouri (03–20; prof. math. and teaching math. 20–24); director math. educational corps, Amer. Exped. Force, Jan.–June 19. Prof. and head math. dept. U. California at Los Angeles (Sept. 24–10 Mar. 37); VP and provost U. California (10 Mar. 37–). Summer term U. Chicago 12. Summer term U. California 17. Summer term U. Texas 20. Summer terms Columbia U. 26, 27, and 35. Summer term New York U. 36.

HONORS.—Mem. council AMS 05–07. Starred *Amer. Men Sci.* 06. Joint ed. *AMM* 13–15. VP AMS 16. First P MAA 16; mem. Board Trustees 17–22, 24–29, 32– . Chm. comm. of MAA on Math. Dictionary 17–35; see no. 36. Mem. Amer. Sect. Intern. Math. Union, representing MAA 20. MAA nominee mem. Div. Phys. Sci. NRC 20–23. Ed.-in-chief *AMS Bull.* 21–Mar. 37. Mem. sub-comm. on math. symbols of sectional comm. on sci. and engin. symbols and abbreviations 26–28. Coop. ed. *AM* 27–29. Fifth annual faculty research lect. U. California at L.A. 29; “Logical reasoning in mathematics and in science.” P AMS 29–30; ret. add. “Non-analytic functions of a complex variable” (Bibl. no. 56). VP AAAS and chm. Sect. A 31; ret. add. “Tendencies in the logic of mathematics” (no. 57). AMS nominee mem. Div. Phys. Sci. NRC 31–34. Chm. Amer. Sect. Intern. Comm. Teaching Math. 32–36. Decorated “Officier d’Académie” (France) “for services rendered to the cause of culture and of science” 32. Chm. comm. on teaching math. in colleges and univs. of the North Central Assoc. 32. Secy. Sect. A AAAS 33– . Mem. comm. MAA on training and utilization of advanced students in math. 33. Hon. Sc.D. U. Michigan 36. Dedication of *AMS Bull.*, v. 44, to E.R.H., by order of the council 38.

BIOGRAPHICAL NOTES.—Prof. Hedrick was a son of Simon and Amy Isabella (Vail) Hedrick. His father was descended from Henrik or Heinrich Hetrig who came from Northern Germany or Holland to Pennsylvania about 1670. His exploration of higher mathematics under the direction of Bôcher, Byerly, Osgood, B. O. Peirce, J. M. Peirce, and F. S. Woods, met with such success that he was appointed a fellow for three successive years. In his second year at Harvard he wrote a paper on three-dimensional determinants (no. 1) which appreciably simplified earlier presentations and contained a number of new results. During three semesters at U. Göttingen he attended lectures by Hilbert, Klein, Voigt and Schur, and his dissertation dealt with the analytic character of solutions of differential equations (no. 2). It was in fields of differential equations, calculus of variations, derivatives over assemblages, and functions of a real variable that Hedrick’s research interests later led to publications (nos. 4, 6, 8, 9, 19, 32, 40, 42, 46, 56). The months spent at Paris in contact with such men as Goursat, Picard, Hadamard, Appell, and Jules Tannery not only reinforced such interest, but brought to his attention problems in the teaching of mathematics, a subject which later, from

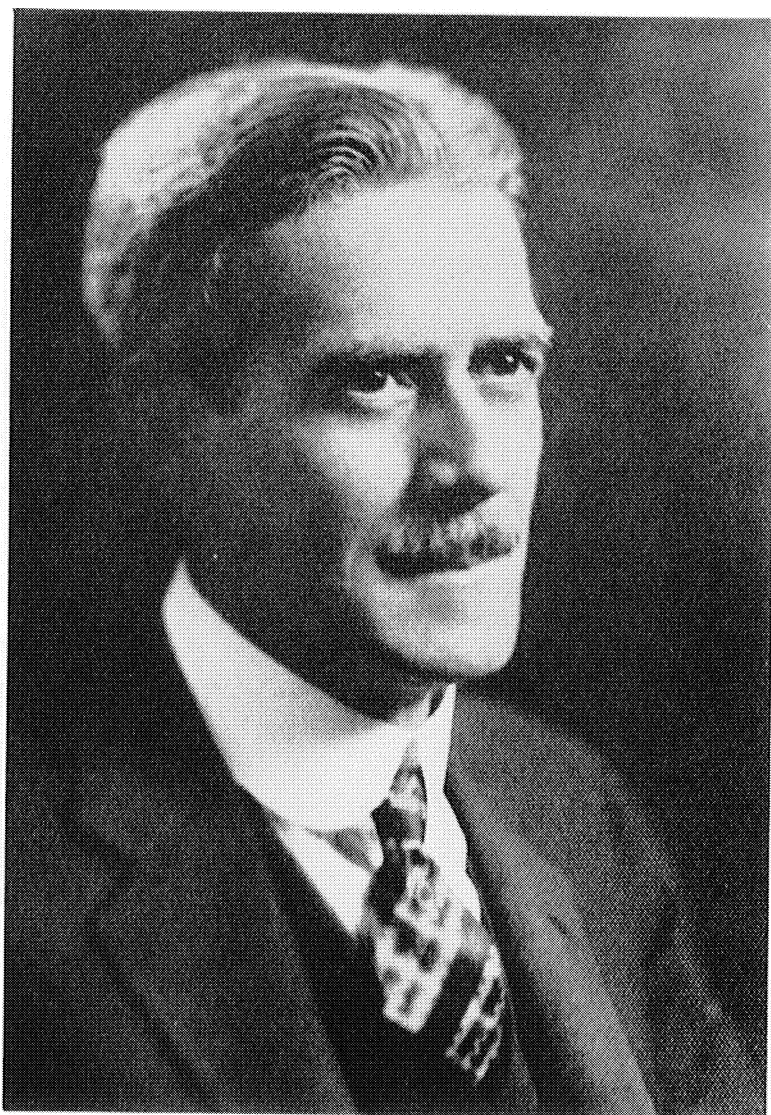
secondary school to graduate school, became a major interest of his life. The following three students received their doctorate under his direction at the U. Missouri, 1913–15: L. L. Silverman, Eula A. Weekes (Mrs. H. L. King), and E. F. Allen.

His translation of Goursat's *Cours d'Analyse* (no. 5), the first part of which appeared soon after his return from France, and (in collaboration with Noble) of the first third of Klein's *Elementarmathematik vom höheren Standpunkte aus* (no. 50), rendered real service to students and college teachers of mathematics in this country. His interest in mechanics first aroused by Ziwet in Michigan days, resulted in the publication (with Kellogg) in 1909 of his *Applications of the Calculus to Mechanics* (no. 16), which became an especially useful book for those teaching calculus to engineers. The attractions which problems of the engineer held for Hedrick is evinced by his papers on a generalized form of Hooke's law, and the transmission of heat in boilers (nos. 29, 31), and by his activities in the Society for the Promotion of Engineering Education, The American Society of Mechanical Engineering and the American Institute of Electrical Engineers. But furthermore, during the past twenty-five years he has been the editor of 34 v., by various authors, in a notable *Engineering Science Series* (no. 64).

In similar fashion we may consider Hedrick's secondary school texts (nos. 12, 33), the fact that an important part of his work at the U. Missouri was to assist in training teachers of mathematics in secondary schools, his many addresses on timely secondary school topics before national organizations and local bodies, as well as the 35 v. which he edited in the *Series of Mathematical Texts* (no. 63). Apart from secondary school texts in this *Series* there are numerous elementary college texts as well as important works of a more advanced nature.

Turning now to his activities in certain national organizations: for the past five years as Secy. of Sect. A, AAAS, he has been alert in conserving the varied and important interests of mathematicians. As one of the founders of the MAA and its first P he had an important part in moulding her policies, and he has ever since been a most zealous promoter of her interests, and one of her most valued counsellors. The debt of AMS to Hedrick is very great indeed. In chapter V, on the *Bulletin*, an attempt has been made to suggest problems faced during the critical seventeen years of his service as editor-in-chief, and his solutions, some of them based on long research. And in chapter III we have occasion to record his great services to the Society in other directions (see *AMS Bull.*, v. 44, p. 1–2, and portrait).

These notes suggest in inadequate manner that Hedrick, with most extraordinary energy, has been notably contributing to the development of mathematics throughout this country, in the secondary field, in the highly important field of applied mathematics, and in national societies. But along with all this extra-mural activity for more than a decade he was



E. R. Hedrick

1930

so eminently successful in helping to develop a strong university at Los Angeles, that he finally became its leader. His remarkable organizing and administrative abilities, the fertility of his ideas, and the thoroughness with which he deals with problems, have led to his services being sought in many directions, so that he recently served in a single year as member of more than two score scientific and educational committees and commissions. But in spare moments six daughters, and three sons find a father who joyously participates in their enthusiasms, or who carries on long-continued experiments in crossing varieties of flowers to produce new types.

SOURCES.—*Who's Who in Amer.*, v. 19. Doctoral diss. "Lebenslauf" (no. 2). *Amer. Men. Sci.*, 5th ed. "Poggendorff," v. 5-6. *Scientific Mo.*, v. 34, 1932, p. 86, portrait. *Science*, n.s., v. 85, p. 309. *Leaders in Educ.*, New York, 1932. *AMM*, v. 44, 1937, p. 274. Personal information.

BIBLIOGRAPHY

1. "On three dimensional determinants," *AM*, s. 2, v. 1, 1900, p. 49-67.
2. *Ueber den analytischen Character der Lösungen von Differentialgleichungen*, Göttingen, 1901, 77+1 ("Lebenslauf") p. Doctoral diss.
3. "On the sufficient conditions in the calculus of variations," *AMS Bull.*, v. 9, 1902, p. 11-24; "Supplementary note on the calculus of variations," v. 9, 1903, p. 245-247.
4. "On the characteristics of differential equations," *AM*, s. 2, v. 4, 1903, p. 121-159.
5. *A Course in Mathematical Analysis* by E. Goursat, trans., 2 v. in 3 (v. 2, parts I and II trans. with O. Dunkel), Boston, 1904-17, viii+548+x+259+viii+300 p.
6. "The calculus of variations," *Encycl. Amer.*, 1905; also in 1936 ed., v. 5, p. 179-184.
7. "On a function which occurs in the law of the mean," *AM*, s. 2, v. 7, 1906, p. 177-192.
8. "A peculiar example in minima of surfaces," *AM*, s. 2, v. 8, 1907, p. 172-174.
9. "On derivatives over assemblages," *AMS Trans.*, v. 8, 1907, p. 345-353.
10. "On a final form of the theorem of uniform continuity," *AMS Bull.*, v. 13, 1907, p. 378-380.
11. "A smooth closed curve composed of rectilinear segments with vertex points which are nowhere dense," *AM*, s. 2, v. 9, 1908, p. 163-166.
12. *An Algebra for Secondary Schools*, New York, etc., 1908, x+421 p.
13. "On the distance from a point to a surface," *AMS Bull.*, v. 14, 1908, p. 321-323.
14. "Recommendations for a high school course in algebra," Report of a comm. of Missouri So. Teachers Math. and Sci., E. R. Hedrick, chm., *School Sci. and Math.*, v. 8, 1908, p. 300-310.
15. "Approximations and approximation processes," *School Sci. and Math.*, v. 8, 1908, p. 617-625, 745-752.
16. *Applications of the Calculus to Mechanics* (with O. D. Kellogg), Boston, etc., 1909, vi+116 p.
17. "The treatment of geometry for secondary instruction," Nat. Educ. Assoc. of U. S., *Journ. of Proc.*, 1909, p. 515-519.
18. "Regarding a certain axiom," *School Sci. and Math.*, v. 9, 1909, p. 770-774. Add. before Missouri So. Teachers Math. and Sci., Columbia, Mo., 1 May 1909.
19. "On properties of a domain for which any derived set is closed," *AMS Trans.*, v. 12, 1911, p. 285-294.
20. "The introduction to geometry," *Ed. Bi-Monthly*, v. 5, 1911, p. 351-357.
21. "On the selection of topics for elementary algebra," *School Sci. and Math.*, v. 11, 1911, p. 51-60.
22. "Final report of national committee of fifteen on geometry syllabus" [E. R. Hedrick

- comm. mem.], *MT*, v. 5, 1912, p. 46–131. “Provisional report . . .,” *School Sci. and Math.*, v. 11, 1911, p. 329–355, 434–460, 509–531.
23. “Mathematics,” Non-Technical Lects. by mems. of the Faculty, U. Missouri, *Bull., Sci. Ser.*, v. 1, 1912, p. 37–53.
 24. “Foreword on behalf of the editors,” *AMM*, v. 20, 1913, p. 1–5.
 25. “Some things we wish to know,” *AMM*, v. 20, 1913, p. 105–107.
 26. “A direct definition of logarithmic derivative,” *AMM*, v. 20, 1913, p. 185–187.
 27. “The significance of Weierstrass’s theorem,” *AMM*, v. 20, 1913, p. 211–213.
 28. “A set of axioms for line geometry” (with L. Ingold), *AMS Trans.*, v. 15, 1914, p. 205–214.
 29. “A generalized form of Hooke’s law,” *Engin. News*, v. 74, 1915, p. 542–543. See comment by G. Paaswell, p. 707.
 30. “The calculus without symbols,” *SPEE Proc.*, v. 22, 1915, p. 125–130, followed by discussion.
 31. “On the transmission of heat in boilers” (with E. A. Fessenden), *Amer. So. Mech. Engin., Trans.*, v. 38, 1916, p. 407–433; followed by discussion.
 32. “Sur l’existence des fonctions implicites” (with W. D. A. Westfall), *SMF Bull.*, v. 44, 1916, p. 1–13.
 33. *Constructive Geometry. Exercises in Elementary Geometric Drawing*, New York, 1916, vi+75 p.
 34. “The significance of mathematics,” *AMM*, v. 24, 1917, p. 401–406.
 35. “In memoriam. Ellery William Davis,” *AMS Bull.*, v. 25, 1918, p. 36–38.
 36. [Report as chm. comm. on Math. Dictionary], *AMM*, v. 25, 1918, p. 60–61.
 37. *Logarithmic and Trigonometric Tables*, rev. ed., “prepared under the direction of” E. R. Hedrick, New York, 1920, xxii+142 p.; reprinted thirteen times up to 1938; some tables included in books in Macmillan’s “A Series of Mathematical Texts” ed. by E.R.H. (no. 63).
 38. “The national committee on mathematical requirements,” *Texas Math. Teachers’ Bull.*, v. 6, no. 2, 1921, p. 7–15. Add. in Austin, Texas.
 39. “Remarks on the report of the national committee on mathematical requirements on college entrance requirements,” *MT*, v. 14, 1921, p. 137–139.
 40. “The existence domain of implicit functions” (with W. D. A. Westfall), *MA*, v. 85, 1922, p. 74–77.
 41. “Functionality in mathematical instruction in schools and colleges,” *MT*, v. 15, 1922, p. 191–207.
 42. “Theory of non-analytic functions of a complex variable” (with L. Ingold and W. D. A. Westfall), *Journ. d. Mathèm.*, s. 9, v. 2, 1923, p. 327–342.
 43. “The function concept in secondary school mathematics,” *The Reorganization of Mathematics in Secondary Education* (Report on Nat. Comm. on Math. Requirements of MAA), 1923, chap. VII, p. 64–73; reprinted (*Riverside Math. Monographs*), Boston, 1927, p. 92–105.
 44. “Analytic functions in three dimensions” (with L. Ingold), *AMS Trans.*, v. 27, 1925, p. 551–555.
 45. “The Beltrami equations in three dimensions” (with L. Ingold), *AMS Trans.*, v. 27, 1925, p. 556–562.
 46. “On derivatives of non-analytic functions,” *NAS Proc.*, v. 14, 1928, p. 649–654.
 47. “Conjugate functions in three dimensions” (with L. Ingold), *Journ. d. Mathèm.*, s. 9, v. 7, 1928, p. 409–416.
 48. “On certain properties of non-analytic functions of a complex variable,” *CMS Bull.*, v. 20, 1928, p. 109–124.
 49. “Concerning the Michelson-Morley experiment” (with L. Ingold), *Astrophys. J.*, v. 68, 1928, p. 374–382; *Contributions from Mount Wilson Obs.*, no. 373, 1928, p. 34–42.
 50. *Elementary Mathematics from an Advanced Standpoint. Arithmetic, Algebra, Analysis* by F. Klein, trans. (with C. A. Noble), New York, 1932, x+274 p.

51. "The teaching of trigonometry for engineers," *Four Papers on the Teaching of Math.*, SPEE Bull., v. 19, 1932, p. i-iii, 1-12. Also in *Journ. Engin. Ed.*, v. 22, 1931, p. 299-310.
52. "Desirable cooperation between educationists and mathematicians," *School and Society*, v. 36, 1932, p. 769-777.
53. "What mathematics means to the world," *MT*, v. 25, 1932, p. 249-263.
54. "Formalism in mathematical teaching," *MT*, v. 25, 1932, p. 441-450.
55. "Science teaching as service," *Calif. Quart. Secondary Ed.*, v. 8, 1933, p. 367-370.
56. "Non-analytic functions of a complex variable," *AMS Bull.*, v. 39, 1933, p. 75-96. AMS ret. P add. 31 Dec. 1931.
57. "Tendencies in the logic of mathematics," *Science*, n.s., v. 77, 1933, p. 335-343. Add. VP AAAS and chm. Sect. A 28 Dec. 1932.
58. "An application of the Dedekind cut notion to integration" (with W. M. Whyburn), *AJM*, v. 55, 1933, p. 390-398.
59. "Meaning of mathematics," *Scientific Mo.*, v. 41, 1935, p. 369-371.
60. "Crises in economics, education and mathematics," *MT*, v. 29, 1936, p. 109-114.
61. "Teaching for transfer of training in mathematics," *MT*, v. 30, 1937, p. 50-55.
62. Reviews of books by Boehm, Hilbert, Geissler, Fricke, Humbert, Bolza, Hancock, Kneser, Pascal, Baire, and Hadamard in *AMS Bull.*, 1902-14.
63. *A Series of Mathematical Texts*, ed. by E. R. Hedrick, 1912-1938: G. D. Birkhoff, *The Origin, Nature, and Influence of Relativity*; N. B. Conkwright, *Differential Equations*; C. H. Currier and E. E. Watson, *General Analysis*; E. W. Davis and W. C. Brenke, *The Calculus*; H. B. Dwight, *Tables of Integrals and other Mathematical Data*; T. S. Fiske and W. R. Longley, *Four-Place Mathematical Tables*; W. B. Ford, *A Brief Course in College Algebra*; W. B. Ford and C. Ammerman, *Plane and Solid Geometry*; J. G. Fowlkes and T. T. Goff, *Modern Life Arithmetics* (six book series and three book series); W. C. Graustein, *Introduction to Higher Geometry*; A. M. Harding and G. W. Mullins, (a) *Analytic Geometry*, (b) *College Algebra*, (c) *Plane Trigonometry*; J. O. Hassler and R. R. Smith, *The Teaching of Secondary Mathematics*; T. F. Holgate, *Projective Pure Geometry*; A. M. Kenyon and L. Ingold, (a) *Plane and Spherical Trigonometry* (b) *Plane Trigonometry for Schools and Colleges*; A. M. Kenyon and W. V. Lovitt, *Mathematics for Agriculture and General Science*; H. W. Kuhn and J. H. Weaver, *Elementary College Algebra*; W. R. Longley and H. B. Marsh, *Algebra*; J. V. McKelvey, *Calculus*; W. O. Menge and J. W. Glover, *An Introduction to the Mathematics of Life Insurance*; J. H. Neelley and J. I. Tracey, *Differential and Integral Calculus*; S. E. Rasor, *Mathematics for Students of Agriculture*; H. L. Rietz, J. F. Reilly, and R. Woods, *Plane and Spherical Trigonometry*; W. H. Roever, *The Mongean Method of Descriptive Geometry*; E. B. Skinner, (a) *Introduction to Trigonometry and Analytic Geometry*, (b) *College Algebra*; W. L. Vosburgh, F. W. Gentleman, and J. O. Hassler, *Junior High School Mathematics*; J. W. Young and F. M. Morgan, (a) *Plane Trigonometry*, (b) *Elementary Mathematical Analysis*; A. Ziwet and L. A. Hopkins, (a) *Analytic Geometry and Algebra*, (b) *Elements of Analytic Geometry*. In this series are also two of Hedrick's v. nos. 33 and 37.
64. *Engineering Science Series*, ed. by E. R. Hedrick, 1913-1938: F. C. Caldwell, *Modern Lighting*; S. D. Chambers, *Mechanics of Engineering*; F. H. Cherry, *Descriptive Geometry: An Introduction to Engineering Graphics*; C. N. Cross, *Heat Engines*; R. F. Deimel, *Mechanics of the Gyroscope*; T. T. Eyre, *Engines and Boilers*; V. M. Faires, (a) *The Design of Machine Elements*, (b) *Problems on the Design of Machine Elements*, (c) *Applied Thermodynamics*, (d) *Elementary Thermodynamics*, (e) *Problems on Applied Thermodynamics*; F. E. Giesecke, A. Mitchell, and H. C. Spencer, (a) *Technical Drawing*, (b) *Technical Drawing Problems*; L. E. Grinter, *Theory of Modern Steel Structures*, L. A. Hazeltine, *Electrical Engineering*; H. J. Hughes and A. T. Safford, *A Treatise on Hydraulics*; D. C. Jackson and J. P. Jackson, *Alternating Currents and Alternating Current Machinery*; E. Kenison and H. C. Bradley, *Descriptive Geometry*; A. E. Kennelly, *Electrical Vibration Instruments*; R. G. Kloeffler, *Telephone Communication Systems*; R. G. Kloeffler, J. L. Brenneman, and J. M. Kerchner, *Direct-Current Machinery*; C. A. Norman, *Principles of Machine Design*; C. A. Norman, E. S. Ault, and I. F. Zarobsky, *Fundamentals of Machine Design*;

N. C. Riggs, *Applied Mechanics*; H. Rubey, (a) *Engineering Surveys*; (b) *Route Surveys*; G. D. Shepardson, *Elements of Electrical Engineering*; C. M. Smith, *Electric and Magnetic Measurements*; C. McD. Townsend, *The Hydraulic Principles Governing River and Harbor Construction*; A. V. Vallance and M. E. Farris, *Principles of Mechanism*; M. P. Weinbach, (a) *Alternating Current Circuits*, (b) *Principles of Transmission in Telephony*; G. Young, Jr. and H. E. Baxter, (a) *Descriptive Geometry*, (b) *Mechanics of Materials*.

21. LUTHER PFAHLER EISENHART

CURRICULUM VITAE.—B. York, Pa. 13 Jan. 1876. Prepared in public schools of his native city for entrance into Pennsylvania C., whose name was changed in 1921 to Gettysburg C. (92-96; A.B. 96; instr. preparatory dept. 96-97). Graduate student of math., phys., and astr. at JHU (97-00; Ph.D. 00). Instr. math. Princeton U. (00-05; preceptor 05-09; prof. 09- ; dean of the faculty 25-33; dean of the graduate school 33-).

HONORS.—Trustee Gettysburg C. 07-14. Starred *Amer. Men Sci.* 10. Joint ed. *AM* Sept. 11-June 25. Mem. Amer. Phil. So. 13. VP AMS 14. VP AAAS and chm. Sect. A 16. Ed. *AMS Trans.* 17-23; managing ed. 20-23. Hon. Sc.D. Gettysburg C. 21. Mem. NAS 22. VP MAA 23; trustee 19-22, 25-30. AMS nominee mem. Div. Phys. Sci. NRC Apr. 23-28; mem. exec. comm. 25-28. Colloq. Lect. AMS 25 (Bibl. no. 95). Trustee AMS 25-26, 31-34. Hon. LL.D. Gettysburg C. 26. P Assoc. Amer. Colleges 30. Mem. comm. (with S. P. Capen and G. S. Ford) surveying Brown U. 30; see Bibl. no. 104. Hon. Sc.D. Columbia U. 31. P AMS 31-32. Mem. Div. For. Relations NRC as chm. Amer. Sect. Intern. Math. Union 31-33. Hon. Sc.D. U. Pennsylvania 33. Assoc. ed. *Com. Mathem.* 34- . Mem. Visiting Comm. dept. math. Mass. Inst. Tech. 34-36. Hon. Sc.D. Lehigh U. 35. Chm. Div. Phys. Sci. NRC 37- .

BIOGRAPHICAL NOTES.—Prof. Eisenhart is a son of Charles Augustus and Emma Catherine (Pfahler) Eisenhart, each being of German descent. His father was a business man particularly in the field of electricity and telephony. Prof. Eisenhart is one who to an extraordinary degree is endowed with the ability to turn almost instantly from intense concentration in one field to similar concentration in an entirely different field. In this way he has not only ably dealt with his teaching, with the preparation of 8 young men for the doctorate 1903-28 (A. E. Young, F. W. Beal, J. M. Stetson, R. D. Beetle, E. S. Hammond, W. E. Cleland, H. Levy, and M. S. Knebelman), with exacting editorial work and university administrative obligations, with important undertakings outside of the university, but also has turned out a wealth of research work in the field of differential geometry and its physical applications. The recently published (1934) index to the *Encyk. d. Math. Wiss.*, v. 3, contains more than a score of references to his work. Some of his most important results are summed up in the four volumes which he published during the eleven years 1923-33 (nos. 85, 91, 95, 110). However, Prof. Eisenhart's first book in 1909 (no. 27) was *A Treatise on the Differential Geometry of Curves and Surfaces* and was a development of courses which had been given at Princeton for a number of years. It was not the first work in differential geometry to be published by an American, since Wilczynski's *Projective Differential Geometry of Curves and Ruled Surfaces* had appeared three years earlier; but it was the first general work in the field. It is in textbook form, with numer-



L. P. Eisenhart

1932

ous problems, introducing the student to classical and modern methods (compare rev. by G. A. Bliss, *AMS Bull.*, v. 17). One of the most interesting novelties of the v. was the so-called "moving trihedrals" for twisted curves as well as surfaces so freely used in writings of Darboux and others. From the first, methods of the theory of functions of a real variable are employed. The work was of great value in introducing the American student to an important field by the most modern method of the time. The first of the other four v., *Transformations of Surfaces* (no. 85), was a work summarizing, developing, and unifying investigations, during the first quarter of the present century, by such men as Bianchi, Darboux, Demoulin, Eisenhart, Guichard, Jonas, Koenigs, Ribaucour, and Tzitzeica. They deal directly or indirectly with transformation of surfaces of a given kind into surfaces of the same kind (see rev. by W. C. Graustein, *AMS Bull.*, v. 30). The then recent physical interpretation of intrinsic differential geometry of spaces stimulated the preparation of the volume on *Riemannian Geometry* (no. 91). Riemann proposed the generalization of the theory of surfaces as developed by Gauss, to spaces of any order, and introduced certain fundamental ideas in this general theory. Important contributions to it were made by Bianchi, Beltrami, Christoffel, Schur, Voss, and others, and Ricci coordinated and extended the theory with the use of tensor analysis and his absolute calculus. The book gave a presentation of the existing theory of Riemannian geometry after a period of considerable study and development of the subject by Levi-Civita, Eisenhart and many others. "One more real contribution to the mathematical literature of America" (C. L. E. Moore, rev. in *AMM*, v. 33; see also S. Lefschetz, *DB*, v. 61). This work naturally paved the way for Eisenhart's next published work *Non-Riemannian Geometry* (1927, no. 95; rev. by J. M. Thomas in *AMS Bull.*, v. 35), although this was delivered in 1925 as Colloq. Lects., under the title, "The new differential geometry," before the *Riemannian Geometry* (no. 91) had appeared. Non-Riemannian geometry had its origin in an article by Weyl (*MZ*, v. 2, 1918) and the fundamental idea is the association with a given manifold of a connection which forms a basis for comparing vectors at different points. The work concludes with an excellent bibliography of books and memoirs referred to in the text, developments made by Finsler, Berwald, Synge, J. H. Taylor, etc. In accounts of this subject frequent reference is made to the paper by Eisenhart and Veblen (no. 73), and later papers by them on the geometry of paths.

Eisenhart's *Continuous Groups of Transformations* (1933, no. 110; rev. by A. Wintner, *AMS Bull.*, v. 40) is a natural development of his earlier books, and sets forth the general theory of Lie and his contemporaries and the results of recent investigations with the aid of the methods of the tensor calculus and concepts of the new differential geometry. The study of continuous groups of transformations inaugurated by Lie resulted in the

developments by Engel, Killing, Scheffers, Schur, Cartan, Bianchi and Fubini, a chapter which closed at about the turn of the century. The new chapter began about 1920 with the extended studies of tensor analysis, Riemannian geometry and its generalizations, and the application of the theory of continuous groups to the new physical theories. Eisenhart has thus developed a remarkable body of original material and has notably served his colleagues by frequent surveys of fields in which he had become a specialist.

Professor Eisenhart's son Churchill has specialized in the field of mathematical statistics and is instructor in mathematics at the U. Wisconsin.

SOURCES.—*Who's Who in Amer.*, v. 19. "Biographical sketch" in doctoral diss. (Bibl. no. 6). *Amer. Men Sci.*, 5th ed.

BIBLIOGRAPHY

1. "A demonstration of the impossibility of a triply asymptotic system of surfaces," *AMS Bull.*, v. 7, 1901, p. 184–186.
2. "Possible triply asymptotic systems of surfaces," *AMS Bull.*, v. 7, 1901, p. 303–305.
3. "Surfaces whose first and second fundamental forms are the second and first respectively of another surface," *AMS Bull.*, v. 7, 1901, p. 417–423.
4. "Lines of length zero on surfaces," *AMS Bull.*, v. 8, 1902, p. 241–243.
5. "Note on isotropic congruences," *AMS Bull.*, v. 8, 1902, p. 301–303.
6. "Infinitesimal deformation of surfaces," *AJM*, v. 24, 1902, p. 173–204. Also as a separate with special title page and "biographical sketch," 35 p. Doctoral diss.
7. "Conjugate rectilinear congruences," *AMS Trans.*, v. 3, 1902, p. 354–371.
8. "Infinitesimal deformation of the skew helicoid," *AMS Bull.*, v. 9, 1902, p. 148–152.
9. "Surfaces referred to their lines of length zero," *AMS Bull.*, v. 9, 1903, p. 242–245.
10. "Isothermal-conjugate systems of lines on surfaces," *AJM*, v. 25, 1903, p. 213–248.
11. "Surfaces whose lines of curvature in one system are represented on the sphere by great circles," *AJM*, v. 25, 1903, p. 349–364.
12. "Surfaces of constant mean curvature," *AJM*, v. 25, 1903, p. 383–396.
13. "Congruences of curves," *AMS Trans.*, v. 4, 1903, p. 470–488.
14. "Congruences of tangents to a surface and derived congruences," *AJM*, v. 26, 1904, p. 180–208.
15. "Three particular systems of lines on a surface," *AMS Trans.*, v. 5, 1904, p. 421–437.
16. "Surfaces with the same spherical representation of their lines of curvature as pseudo-spherical surfaces," *AJM*, v. 27, 1905, p. 113–172.
17. "On the deformation of surfaces of translation," *AMS Bull.*, v. 11, 1905, p. 486–494.
18. "Surfaces of constant curvature and their transformations," *AMS Trans.*, v. 6, 1905, p. 472–485.
19. "Surfaces analogous to the surfaces of Bianchi," *Annali M.*, s. 3, v. 12, 1905, p. 113–143.
20. "Certain surfaces with plane or spherical lines of curvature," *AJM*, v. 28, 1906, p. 47–70.
21. "Associate surfaces," *MA*, v. 62, 1906, p. 504–538.
22. "Transformations of minimal surfaces," *Annali M.*, s. 3, v. 13, 1906, p. 249–262.
23. "Applicable surfaces with asymptotic lines of one surface corresponding to a conjugate system of another," *AMS Trans.*, v. 8, 1907, p. 113–134, 535.
24. "Certain triply orthogonal systems of surfaces," *AJM*, v. 29, 1907, p. 168–212.
25. "Surfaces with isothermal representation of their lines of curvature and their transformations," *AMS Trans.*, v. 9, 1908, p. 149–177; v. 11, 1910, p. 475–486.
26. "Surfaces with the same spherical representation of their lines of curvature as spherical surfaces," *AJM*, v. 30, 1908, p. 19–42.

27. *A Treatise on the Differential Geometry of Curves and Surfaces*, Boston, 1909, xi+474 p.
28. "The twelve surfaces of Darboux and the transformation of Moutard," *AJM*, v. 32, 1910, p. 17-36.
29. "Congruences of the elliptic type," *AMS Trans.*, v. 11, 1910, p. 351-370.
30. "A fundamental parametric representation of space curves," *AM*, s. 2, v. 13, 1911, p. 17-35.
31. "Sopra le deformazioni continue delle superficie reali applicabili sul paraboloide a parametro puramente immaginario," *AL Rend.*, s. 5, v. 21, pt. 1, 1912, p. 458-462.
32. "Ruled surfaces with isotropic generators," *CMP Rend.*, v. 34, 1912, p. 29-40.
33. "Minimal surfaces in Euclidean four-space," *AJM*, v. 34, 1912, p. 215-236.
34. "Certain continuous deformations of surfaces applicable to the quadrics," *AMS Trans.*, v. 14, 1913, p. 365-402.
35. "Transformations of surfaces of Guichard and surfaces applicable to quadrics," *Annali M.*, s. 3, v. 22, 1914, p. 191-247.
36. "Transformations of surfaces of Voss," *AMS Trans.*, v. 15, 1914, p. 245-265.
37. "Transformations of conjugate systems with equal point invariants," *AMS Trans.*, v. 15, 1914, p. 397-430.
38. "Conjugate systems with equal tangential invariants and the transformation of Moutard," *CMP Rend.*, v. 39, 1915, p. 153-176.
39. "Transformations of surfaces Ω ," *NAS Proc.*, v. 1, 1915, p. 62-65.
40. "One-parameter families of curves," *AJM*, v. 37, 1915, p. 179-191.
41. "Transformations of conjugate systems with equal invariants," *NAS Proc.*, v. 1, 1915, p. 290-295.
42. "Surfaces Ω and their transformations," *AMS Trans.*, v. 16, 1915, p. 275-310.
43. "Sulle superficie di rotolamento e le trasformazioni di Ribaucour," *AL Rend.*, s. 5, v. 24, pt. 2, 1915, p. 349-352.
44. "Surfaces with isothermal representation of their lines of curvature as envelopes of rolling," *AM*, s. 2, v. 17, 1915, p. 64-71.
45. "Transformations of surfaces Ω ," *AMS Trans.*, v. 17, 1916, p. 53-99.
46. "Deformations of transformations of Ribaucour," *NAS Proc.*, v. 2, 1916, p. 173-177.
47. "Conjugate systems with equal point invariants," *AM*, s. 2, v. 18, 1916, p. 7-17.
48. "Surfaces generated by the motion of an invariable curve whose points describe straight lines," *CMP Rend.*, v. 41, 1916, p. 94-102.
49. "Deformable transformations of Ribaucour," *AMS Trans.*, v. 17, 1916, p. 437-458.
50. "Certain surfaces of Voss and surfaces associated with them," *CMP Rend.*, v. 42, 1917, p. 145-166.
51. "Transformations T of conjugate systems of curves on a surface," *AMS Trans.*, v. 18, 1917, p. 97-124.
52. "Triads of transformations of conjugate systems of curves," *NAS Proc.*, v. 3, 1917, p. 453-457.
53. "Conjugate planar nets with equal invariants," *AM*, s. 2, v. 18, 1917, p. 221-225.
54. "Transformations of applicable conjugate nets of curves on surfaces," *NAS Proc.*, v. 3, 1917, p. 637-640.
55. "Operation of the dropping rule," *Princeton Alumni Weekly*, v. 17, 1917, p. 567-568.
56. "Darboux's contribution to geometry," *AMS Bull.* v. 24, 1918, p. 227-237; German trans. in *Acta M.*, v. 42, 1919, p. 275-284.
57. "Princeton's new war courses," *Princeton Alumni Weekly*, v. 18, 1918, p. 823-824.
58. "Surfaces which can be generated in more than one way by the motion of an invariable curve," *AM*, s. 2, v. 19, 1918, p. 217-230.
59. "Transformations of planar nets," *AJM*, v. 40, 1918, p. 127-144.
60. "Transformations of applicable conjugate nets of curves on surfaces," *AMS Trans.*, v. 19, 1918, p. 167-185.
61. "New three-year course," *Princeton Alumni Weekly*, v. 19, 1919, p. 724-725.

62. "Triply conjugate systems with equal point invariants," *AM*, s. 2, v. 20, 1919, p. 262-273.
63. "Transformations of surfaces applicable to a quadric," *AMS Trans.*, v. 20, 1919, p. 323-338.
64. "Transformations of cyclic systems of circles," *NAS Proc.*, v. 5, 1919, p. 555-557.
65. "The permanent gravitational field in the Einstein theory," *AM*, s. 2, v. 22, 1920, p. 86-94. Also *NAS Proc.*, v. 6, 1920, p. 678-682.
66. "Sulle congruenze di sfere di Ribaucour che ammettono una deformazione finita," *AL Rend.*, s. 5, v. 29, pt. 2, 1920, p. 31-33.
67. "Conjugate systems of curves R and their transformations," *Intern. Congress Mathems.*, Strasbourg, 1921, p. 407-409.
68. "Transformations of surfaces applicable to a quadric," *Journ. d. Mathém.*, s. 8, v. 4, 1921, p. 37-66.
69. "Conjugate nets R and their transformations," *AM*, s. 2, v. 22, 1921, p. 161-181.
70. "The Einstein solar field," *AMS Bull.*, v. 27, 1921, p. 432-434.
71. "Sulle trasformazioni T dei sistemi tripli coniugati di superficie," *AL Rend.*, s. 5, v. 30, pt. 2, 1921, p. 399-401.
72. "Einstein static fields admitting a group G_2 of continuous transformations into themselves," *NAS Proc.*, v. 7, 1921, p. 328-334.
73. "The Riemann geometry and its generalization" (with O. Veblen), *NAS Proc.*, v. 8, 1922, p. 19-23.
74. "Ricci's principal directions for a Riemann space and the Einstein theory," *NAS Proc.*, v. 8, 1922, p. 24-26.
75. "The Einstein equations for the solar field from the Newtonian point of view," *Science*, n.s., v. 55, 1922, p. 570-572.
76. "Fields of parallel vectors in the geometry of paths," *NAS Proc.*, v. 8, 1922, p. 207-212.
77. "Spaces with corresponding paths," *NAS Proc.*, v. 8, 1922, p. 233-238.
78. "Condition that a tensor be the curl of a vector," *AMS Bull.*, v. 28, 1922, p. 425-427.
79. "Affine geometries of paths possessing an invariant integral," *NAS Proc.*, v. 9, 1923, p. 4-7.
80. "Another interpretation of the fundamental gauge-vector of Weyl's theory of relativity," *NAS Proc.*, v. 9, 1923, p. 175-178.
81. "Orthogonal systems of hypersurfaces in a general Riemann space," *AMS Trans.*, v. 25, 1923, p. 259-280.
82. "Symmetric tensors of the second order whose first covariant derivatives are zero," *AMS Trans.*, v. 25, 1923, p. 297-306.
83. "Einstein and Soldner," *Science*, n.s., v. 58, 1923, p. 516.
84. "The geometry of paths and general relativity," *AM*, s. 2, v. 24, 1923, p. 367-392.
85. *Transformations of Surfaces*, Princeton, 1923, ix+379 p.
86. "Space-time continua of perfect fluids in general relativity," *AMS Trans.*, v. 26, 1924, p. 205-220.
87. "Geometries of paths for which the equations of the paths admit a quadratic first integral," *AMS Trans.*, v. 26, 1924, p. 378-384.
88. "Linear connections of a space which are determined by simply transitive continuous groups," *NAS Proc.*, v. 11, 1925, p. 246-250.
89. "Fields of parallel vectors in a Riemannian geometry," *AMS Trans.*, v. 27, 1925, p. 563-573.
90. "Einstein's recent theory of gravitation and electricity," *NAS Proc.*, v. 12, 1926, p. 125-129.
91. *Riemannian Geometry*, Princeton, 1926, vii+262 p.
92. "Geometries of paths for which the equations of the paths admit $n(n+1)/2$ independent linear first integrals," *AMS Trans.*, v. 28, 1926, p. 330-338.
93. "Congruences of parallelism of a field of vectors," *NAS Proc.*, v. 12, 1926, p. 757-760.
94. "Displacements in a geometry of paths which carry paths into paths" (with M. S. Knebelman), *NAS Proc.*, v. 13, 1927, p. 38-42.

95. *Non-Riemannian Geometry* (AMS Colloq. Pub. no. 8), 1927, viii+184 p. Reprinted 1934.
96. "Teaching at Princeton," Assoc. Amer. Colleges, *Bull.*, v. 14, 1928, no. 5.
97. "Will Princeton's progress be retarded?" *Princeton Alumni Weekly*, v. 28, 1928, p. 595-596.
98. "Affine geometry," *Encycl. Brit.*, 14th ed., v. 1, 1929, p. 279.
99. "Differential geometry," *Encycl. Brit.*, 14th ed., v. 7, 1929, p. 366-367.
100. "Contact transformations," *AM*, s. 2, v. 30, 1929, p. 211-249.
101. "Dynamical trajectories and geodesics," *AM*, s. 2, v. 30, 1929, p. 591-606.
102. "Projective normal coordinates," *NAS Proc.*, v. 16, 1930, p. 731-740.
103. "The intellectual life in the colleges," Assoc. Amer. Colleges, *Bull.*, v. 16, 1930, no. 1.
104. "Report of the survey committee" (with S. P. Capen and G. S. Ford), Brown U., *Bull.*, v. 27, 1930, 50 p.; there are many pages of appendices.
105. "Henry Burchard Fine and the Fine Memorial Hall," *Scientific Mo.*, v. 33, 1931, p. 565-568.
106. "Intransitive groups of motions," *NAS Proc.*, v. 18, 1932, p. 193-202.
107. "Equivalent continuous groups," *AM*, s. 2, v. 33, 1932, p. 665-670.
108. Report as dean of the faculty for the years 1925-33 and as chm. dept. math., Princeton U., *Report of the President*, 1933, p. 10-16, 110-115. Similarly in *Report*, 1934, p. 50-53, 123-128 for reports as dean of the graduate school, and as chm. dept. math. Also 1935, p. 64-68, 156-160; 1936, p. 77-80, 163-168; 1937, p. 78-86, 177-183.
109. "Spaces admitting complete absolute parallelism," *AMS Bull.*, v. 39, 1933, p. 217-226. AMS ret. P add. 28 Dec. 1932.
110. *Continuous Groups of Transformations*, Princeton, 1933, ix+301 p.
111. "Separable systems in Euclidean 3-space," *Phys. Rev.*, s. 2, v. 45, 1934, p. 427-428.
112. "Separable systems of Stäckel," *AM*, s. 2, v. 35, 1934, p. 284-305.
113. "Stäckel systems in conformal Euclidean space," *AM*, s. 2, v. 36, 1935, p. 57-70.
114. "Groups of motions and Ricci directions," *AM*, s. 2, v. 36, 1935, p. 823-832.
115. "Graduate study and research: Lehigh University 1935 Founder's Day address," *Science*, n.s., v. 83, 1936, p. 147-150.
116. "Simply transitive groups of motions," *MMP*, v. 43, 1936, p. 448-462.
117. "Invariant theory of homogeneous contact transformations," *AM*, s. 2, v. 37, 1936, p. 747-765.
118. "The college's part in the guidance of youth," *School and Society*, v. 43, 1936, May 23.
119. "The graduate school of arts and sciences," *School and Society*, v. 45, 1937, p. 497-503.
120. *Coordinate Geometry. Princeton U. 1937-1938*, Ann Arbor, Mich., 1937, iv+107 p.; Planograph print. Rev. ed. 1938, vi+136 p.
121. Proposal of toast to municipality of Oslo, at dinner, 15 July 1936, *Intern. Congress Mathems.*, Oslo. v. 1, 1937, p. 53-54.
122. "Fields of parallel vectors in Riemannian space," *AM*, v. 39, 1938, p. 316-321. Compare nos. 89 and 91, p. 67-72.
123. Reviews of books by Tannenber, Guichard, Wright, Bianchi, Christoffel, Darboux, Eddington, Schell, Einstein, and Silberstein in *AMS Bull.*, 1901-24; by Birkhoff in *Science*, 1923.

22. ARTHUR BYRON COBLE

CURRICULUM VITAE.—B. Williamstown, Pa. 3 Nov. 1878. Educ. Pennsylvania C. whose name was changed in 1921 to Gettysburg C. (93-97, A.B. 97; A.M. 00); teacher public schools (97-98); student and student assist. JHU (98-01; fellow 01-02; Ph.D. 02). Instr. U. Missouri (02-03); research assist. Carnegie Inst. at JHU (03), and Greifswald U. and Bonn U. (04); instr. math. JHU (04-06; assoc. 06-09; assoc. prof. 09-18; prof. 27-28). Prof. math. U. Illinois (18-27 and since 28). Visiting prof. U. Chicago 19.

HONORS.—Starred *Amer. Men Sci.* 10. VP AMS 17. Joint ed. *AMS Trans.* 20-25. Chm. Chicago Sect. AMS 22. Mem. NAS 24. Mem. NRC Comm. on Rational Transformations 24-28;

see Bibl. no. 32. Ed., repr. AMS, *AJM* 27-33; assoc. ed. 18-26. Colloq. lect. AMS 28; see Bibl. no. 33. Hon. Lt.D. Gettysburg C. 32. AMS nominee mem. Div. Phys. Sci. NRC 32-35. P AMS 33-34; ret. add. see Bibl. no. 37. Joint ed. *DMJ* 36-38.

BIOGRAPHICAL NOTES.—Prof. Coble is a son of Reuben Coble, a merchant and banker in Lykens, Pa., whose grandfather emigrated from Württemberg, Germany to America in 1810 and settled in York County, Pa. His mother Emma I. Haegy, was of Scotch-Irish extraction.

Among Prof. Coble's publications one set (nos. 7, 8, 13, 14, 15, 19) consists of investigations which relate to configurations which occur in finite geometries or in connection with finite groups. In the most significant of these (no. 15) we find for the first time a clear-cut presentation of the different rôles played by the period characteristics and theta characteristics in the theta function theory. In no. 16, on restricted systems of equations, formulae are obtained, not merely for the order of a manifold defined by the vanishing of determinants of a matrix, but also for the genus of the curve which is a linear section of such a manifold. In no. 31, written in collaboration with Prof. Frank Morley, the range of cases in which algebraic resultants can be specifically given is greatly extended. The papers on symmetric binary forms and involutions (no. 10) present some new interpretations of such forms as primals of a particular character with respect to a rational norm-curve. Closely related to these are the studies of porisms, and of algebraic forms with a closure property (nos. 18, 23, 30), which contain the first systematic study of such problems.

A considerable body of Coble's research (nos. 9, 11, 12, 17, 20, 22, 26, 28) was suggested by the fact that in the Galois theory of equations, and in other algebraic situations, the representations which are desired are rational rather than linear. One would naturally expect to find in such situations more important applications of Cremona transformations and groups than had appeared. This expectation is realized in connection with the quintic equation (nos. 9, 11, 12, 28). In pursuing this application of Cremona groups, it seemed necessary to relieve in some measure the exceptional character of the F -points of the transformations. This was accomplished by the introduction of the idea of congruence of sets of points under Cremona transformations. From this more general point of view it was possible to handle satisfactorily more difficult algebraic problems such as that of the determination of the twenty-seven lines of a cubic surface (no. 17). A general account of this is given in no. 25; its position in the field of Cremona transformations is set forth in no. 32; its relation to theta and theta modular function theory is brought out in no. 33; and a résumé is found in *Encyk. d. Math. Wiss.* v. 3, part 2 B, p. 2107-2113. There are scores of other references to work of Coble in this v. (see index).

Studies of the relations between hyperelliptic theta functions and irrational binary invariants, and of generalizations of the Weddle surface and hyperelliptic Kummer surface are made in nos. 34, 35, 37, 38. In an at-



Arthur B. Coble

1933

tempt to bring our knowledge of the Abelian theta functions of genus four, and the allied geometry into the same satisfactory state as obtains in the case of the functions of genus three, a considerable variety of geometric configurations associated with an algebraic curve of genus four has been discussed in no. 27. The linear groups with a quadratic invariant associated with certain Cremona groups are discussed in nos. 36, 39, 40, and 41.

The following 22 students received their doctorate under the direction of Professor Coble at JHU and U. Illinois, 1914–38: Bessie I. Miller, W. F. Shenton, C. P. Sousley, J. R. Musselman, C. C. Bramble, Jessie M. Jacobs (Mrs. H. J. Müller, and Mrs. C. Offerman), R. Woods, R. M. Mathews, T. L. Bennett, H. L. Black, Elizabeth M. Cooper, Frances Harshbarger, G. E. Moore, C. W. Strom, Mildred E. Taylor, S. F. Barber, Josephine H. Chanler, E. R. Ott, B. G. Clark, G. B. Huff, F. C. Gentry, R. W. Kempfer.

Professor Coble enjoys as recreations, golf, tennis, swimming, tramping, bridge, billiards, and light reading.

SOURCES.—*Who's Who in Amer.*, v. 19. *Amer. Men Sci.*, 5th ed. *Leaders in Educ.* "Pogendorff," v. 5–6. Personal information.

BIBLIOGRAPHY

1. "On the reduction of the decimic to Sylvester's canonical form," *JHU Circulars*, no. 3, 1901, p. 54–55.
2. "The quartic curve as related to conics," *AMS Trans.*, v. 4, 1903, p. 65–85. Doctoral diss.
3. "Collineations whose characteristic determinants have linear elementary divisors with an application to quadratic forms," *AJM*, v. 27, 1905, p. 25–46.
4. "The normal form of a ternary collineation and the simultaneous reduction of two conics to a normal form," *JHU Circulars*, no. 1, 1905, p. 27–38.
5. "The linear relations among the minors of a symmetric determinant," *JHU Circulars*, no. 9, 1906, p. 86–90.
6. "On the relation between the three-parameter groups of a cubic space curve and a quadric surface," *AMS Trans.*, v. 7, 1906, p. 1–20.
7. "An invariant condition for certain automorphic algebraic forms," *AJM*, v. 28, 1906, p. 333–366.
8. "A configuration in finite geometry isomorphic with that of the 27 lines of a cubic surface," *JHU Circulars*, no. 7, 1908, p. 80–88.
9. "An application of the form-problems associated with certain Cremona groups to the solution of equations of higher degree," *AMS Trans.*, v. 9, 1908, p. 396–424.
10. "Symmetric binary forms and involutions," *AJM*, v. 31, 1909, p. 183–212; 355–364; v. 32, 1910, p. 333–364.
11. "An application of Moore's cross-ratio group to the solution of the sextic equation," *AMS Trans.*, v. 12, 1911, p. 311–325.
12. "The reduction of the sextic equation to the Valentiner form-problem," *MA*, v. 70, 1911, p. 337–350.
13. "The lines and triple tangent planes of a cubic surface," *JHU Circulars*, no. 2, 1911, p. 59–63.
14. "The linear complex in the finite geometry (mod 2) of an S_5 ," *JHU Circulars*, no. 2, 1912, p. 43–46.
15. "An application of finite geometry to the characteristic theory of the odd and even theta functions," *AMS Trans.*, v. 14, 1913, p. 241–276.

16. "Restricted systems of equations," *AJM*, v. 36, 1914, p. 167-186, 395-418.
17. "Point sets and allied Cremona groups," *AMS Trans.*, v. 16, 1915, p. 155-198; v. 17, 1916, p. 345-385; v. 18, 1917, p. 331-372. Summaries in *NAS Proc.*, v. 1, 1915, p. 245-248; v. 2, 1916, p. 244-246, 575-576.
18. "A proof of White's porism," *NAS Proc.*, v. 2, 1916, p. 530-531.
19. "An isomorphism between theta characteristics and the $(2p+2)$ -point," *AM*, s. 2, v. 17, 1916, p. 101-112.
20. "Theta modular groups determined by point sets," *AJM*, v. 40, 1918, p. 317-340.
21. "Concerning a method for finding a particular integral," *AMM*, v. 26, 1919, p. 12-15.
22. "The ten nodes of the rational sextic and of the Cayley symmetroid," *AJM*, v. 41, 1919, p. 243-265.
23. "Multiple binary forms with the closure property," *AJM*, v. 43, 1921, p. 1-19.
24. "A covariant of three circles," *AMS Bull.*, v. 27, 1921, p. 434-437.
25. "Cremona transformations and applications to algebra, geometry, and modular functions," *AMS Bull.*, v. 28, 1922, p. 329-364.
26. "Associated sets of points," *AMS Trans.*, v. 24, 1922, p. 1-20.
27. "Geometric aspects of the Abelian modular functions of genus four," *AJM*, v. 46, 1924, p. 143-192; v. 51, 1929, p. 495-514; summary in *NAS Proc.*, v. 7, 1921, p. 245-249, 334-338; v. 9, 1923, p. 183-187.
28. "The equation of the eighth degree," *AMS Bull.*, v. 30, 1924, p. 301-313.
29. "Maps of 12 countries with five sides with a group of order 120 containing an ikosahedral subgroup," (with H. R. Brahana), *AJM*, v. 48, 1926, p. 1-20.
30. "Double binary forms with the closure property," *AMS Trans.*, v. 28, 1926, p. 357-383.
31. "New results in elimination" (with F. Morley), *AJM*, v. 49, 1927, p. 463-488.
32. "Planar Cremona transformations"; "Cremona transformations in space and hyper-space," Chap. IV and VIII of *Topics in Algebraic Geometry*, *NRC Bull.*, no. 63, 1928, p. 79-121, 197-226.
33. *Algebraic Geometry and Theta Functions* (*AMS Colloq. Pub.*, v. 10), 1929, vii+282 p.
34. "A generalization of the Weddle surface, of its Cremona group, and of its parametric expression in terms of hyperelliptic theta functions," *AJM*, v. 52, 1930, p. 433-500.
35. "Hyperelliptic functions and irrational binary invariants," *AJM*, v. 54, 1932, p. 425-452; v. 55, 1933, p. 1-21, 349-375.
36. "Cremona's Diophantine equation," *AJM*, v. 56, 1934, p. 459-489.
37. "The geometry of the Weddle manifold W_p ," *AMS Bull.*, v. 41, 1935, p. 209-222. *AMS ret. P add.* 28 Dec. 1934.
38. "The geometry of the Weddle manifold W_p " (with Josephine H. Chanler), *AJM*, v. 57, 1935, p. 183-218.
39. "Collineation groups in a finite space with a linear and a quadratic invariant," *AJM*, v. 58, 1936, p. 15-34.
40. "Groups of Cremona transformations in a space of planar type," *DMJ*, v. 2, 1936, p. 1-9, 205-219.
41. "A class of linear groups with integral coefficients," *DMJ*, v. 3, 1937, p. 175-199.
42. "Frank Morley," *AMS Bull.*, v. 44, 1938, p. 167-170.
43. Reviews of books by H. P. Hudson, and H. Malet in *AMS Bull.*, 1923 and 1928 and by Coolidge in *AMM*, 1932.

23. SOLOMON LEFSCHETZ

CURRICULUM VITAE.—B. Moscow, Russia, 3 Sept. 1884. Reared in Paris, France; student École Centrale, Paris (02-05; degree as "ingénieur des arts et manufactures"). Upon graduation in autumn 05, came to the U.S. and was a few months with the Baldwin Locomotive works. An engineering apprentice and then on the engineering staff of Westinghouse Electric and Mfg. Co.,



Stephens

1935

Pittsburgh, Pa. 07-10. Fellow Clark U. (10-11; Ph.D. 11). Instr. math. U. Nebraska (11-13); instr. U. Kansas (13-16; assist. prof. 16-19; assoc. prof. 19-23; prof. 23-25). Visiting prof. Princeton U. (24-25; assoc. prof. 25-28; prof. 28-33; H. B. Fine research prof. 33-). Naturalized citizen of U.S. 17 June 12.

HONORS.—Awarded the Prix Bordin (3000 francs) by the Acad. des Sci., Institut de France, for a notable contribution in the fields of algebraic multiplicities and topology 19; the memoir was a manuscript afterwards published in somewhat modified form as Bibl. no. 24. Collaborating ed. *DB*, Paris, 23- . Second award of Bôcher Memorial Prize (\$100) offered for a notable research memoir in *AMS Trans.* v. 19-24, divided equally between E. T. Bell and S. Lefschetz 24; the latter's memoir was entitled "On certain numerical invariants . . ." (no. 24). Mem. NRC research comm. on Analysis Situs 24-32. Mem. NRC comm. on Rational Transformations 24-28; see Bibl. no. 42. Mem. NAS 25. Joint ed. *AM* April 28- . Mem. comm. eds. *CMP Rend.* 28-35. Mem. Amer. Phil. So. 29. Lect. at Moscow (5 lects.), Hamburg (2), Göttingen (1) 31. Assoc. ed. *Com. Mathem.* 34- . Invited lect. second Soviet Math. Congress, Moscow 34; add., Bibl. no. 62. Invited speaker Topological Congress, Moscow, 35. P AMS 35-36. For. mem. Royal Bohemian So. of Sci., Prague 35. Five lects. at Paris (Sorbonne 3, So. Math. d. France, séminaire Julia); short course, 3 weeks, at Warsaw; at Prague 2 lects. and at Brno 1, all in 36. Hon. mem. Czechoslovakian Union of Math. and Phys. 36. Corresp. mem. Royal Acad. Sci., Letters and Arts, Padua 37.

BIOGRAPHICAL NOTES.—Prof. Lefschetz is one of America's foreign-born mathematicians who has very notably enriched its literature, and he is internationally recognized as a leader in the fields of algebraic geometry and topology. He lost both of his hands in 1907; the heroic spirit which later enabled him to overcome all but insurmountable obstacles, and to attain to his present position of eminence, must be unique in the annals of the mathematical brotherhood. Some years before he had left the U. Kansas the French crowned his research achievements by the award of the Prix Bordin; for the report of the commission, consisting of Jordan, Appell, Painlevé, Humbert, Hadamard, Goursat, Boussinesq, Lecornu, Picard, see *CR Paris*, v. 169, p. 1200-1202.

In Prof. Lefschetz's research in Algebraic Geometry the central problem with which he has been occupied has been the classification of curves and surfaces and related questions. One of his chief results may be described as follows: Severi introduced an algebraic relation of equivalence between algebraic curves on a surface. Referring to the Riemann manifold M which represents the surface, each algebraic curve determines a unique z -dimensional cycle of the manifold. Lefschetz showed that the relations of homology between these cycles correspond exactly to Severi's relation of equivalence. He has also given the necessary and sufficient condition in order that a z -dimensional cycle on M be equivalent to the cycles just considered. Other noteworthy results are that the Kronecker index of two algebraic cycles and the number of intersections of the corresponding curves or manifolds counted in the usual sense are the same, and similarly for higher dimensions. This enabled him to give a topological treatment of the classification of multiple periodic functions, intersections on Abelian varieties, and the theory of correspondences on an algebraic curve. The

influence of these results in recent research may readily be traced in the work of the younger algebraic geometers, notably Hodge and Zariski.

Lefschetz's first research in pure topology was concerned with the fixed point problem and this has occupied him off and on ever since (see nos. 33, 38, 41, chapter 7 in no. 48, 67). The main result may be stated as follows: Given a separable metric space it is possible in many cases to calculate an invariant number θ attached to transformations of the space and having the property that $\theta \neq 0$ implies that there is at least one fixed point. The number θ depends only upon the transformations of the rational cycles or cocycles. In this respect compare the work of H. Hopf and A. W. Tucker. Other important contributions are, the introduction of rational coefficients (no. 41), relative cycles (nos. 34, 41), and of cocycles, called pseudocycles (no. 46), which are of constant use in modern topology. Among important recent contributions are the method of the semi-singular complex which made it possible to free local connectedness and Borsuk's theory of retraction from all restrictions regarding dimension. Spaces of type *LC* or *HLC* (endowed with a strongly uniform local connectedness) are the maximal spaces compact metric for which the fixed point formulas are known to hold (see nos. 56, 58, 67). The *Encyk. d. Math. Wiss.*, v. 3. 1. 2. B and 3. 2. 2. give nearly two scores of references to results of Prof. Lefschetz's research (see index).

The following 8 men received their doctorate under the direction of Prof. Lefschetz at Princeton U., 1926–37: P. A. Smith, W. W. Flexner, A. W. Tucker, R. J. Walker, N. E. Steenrod, H. Wallman, S. Wylie, C. H. Dowker.

SOURCES.—*Who's Who in Amer.*, v. 19. *Amer. Men Sci.*, 5th ed. "Poggendorf," v. 5. Personal information.

BIBLIOGRAPHY

1. "Two theorems on conics," *AM*, s. 2, v. 14, 1912, p. 47–50.
2. "On the V_3^3 with five nodes of the second species in S_4 ," *AMS Bull.*, v. 18, 1912, p. 384–386.
3. "Double curves of surfaces projected from space of four dimensions," *AMS Bull.*, v. 19, 1912, p. 70–74.
4. "On some topological properties of plane curves and a theorem of Möbius," *AJM*, v. 35, 1913, p. 189–200.
5. "On the existence of loci with given singularities," *AMS Trans.*, v. 14, 1913, p. 23–41. Doctoral diss.
6. "Geometry on ruled surfaces," *AJM*, v. 36, 1914, p. 392–394.
7. "Note on the n -dimensional cycles of an algebraic n -dimensional variety," *CMP Rend.*, v. 40, 1915, p. 38–43.
8. "On cubic surfaces and their nodes," Kansas U., *Sci. Bull.*, v. 9, 1915, p. 69–78.
9. "The equation of Picard-Fuchs for an algebraic surface with arbitrary singularities," *AMS Bull.*, v. 21, 1915, p. 227–232.
10. "Direct proof of De Moivre's formula," *AMM*, v. 23, 1916, p. 366–368.
11. "The arithmetic genus of an algebraic manifold immersed in another," *AM*, s. 2, v. 17, 1916, p. 197–212.
12. "Sur les intégrales multiples des variétés algébriques," *CR Paris*, v. 164, 1917, p. 850–853.

13. "On the residues of double integrals belonging to an algebraic surface," *QJM*, v. 47, 1917, p. 333-343.
14. "Sur certains cycles à deux dimensions des surfaces algébriques," *AL Rend.*, s. 5, v. 26, 1917, p. 228-234.
15. "Sur les intégrales doubles des variétés algébriques," *Annali M.*, s. 3, v. 26, 1917, p. 227-260.
16. "Note on a problem in the theory of algebraic manifolds," Kansas U., *Sci. Bull.*, v. 10, 1917, p. 1-9.
17. "Sur l'analyse situs des variétés algébriques," *CR Paris*, v. 168, 1919, p. 672-674.
18. "Sur les variétés abéliennes," *CR Paris*, v. 168, 1919, p. 758-761.
19. "On the real folds of Abelian varieties," *NAS Proc.*, v. 5, 1919, p. 103-106.
20. "Real hypersurfaces contained in Abelian varieties," *NAS Proc.*, v. 5, 1919, p. 296-298.
21. "Algebraic surfaces, their cycles and integrals," *AM*, s. 2, v. 21, 1920, p. 225-258; a correction, v. 23, 1922, p. 333.
22. "Quelques remarques sur la multiplication complexe," *Intern. Congress Mathems.*, Strasbourg, 1921, p. 300-307.
23. "Sur le théorème d'existence des fonctions abéliennes," *AL Rend.*, s. 5, v. 30, pt. 1, 1921, p. 48-50.
24. "On certain numerical invariants of algebraic varieties with application to abelian varieties," *AMS Trans.*, v. 22, 1921, p. 327-482.
25. "Sur les intégrales de seconde espèce des variétés algébriques," *CR Paris*, v. 176, 1923, p. 941-943.
26. "Continuous transformations of manifolds," *NAS Proc.*, v. 9, 1923, p. 90-93.
27. "Report on curves traced on algebraic surfaces," *AMS Bull.*, v. 29, 1923, p. 242-258.
28. "Progrès récents dans la théorie des fonctions abéliennes" [Résumé de travaux de M. Scorza], *DB*, v. 47, 1923, p. 120-128.
29. "Sur les intégrales multiples des variétés algébriques," *Journ. d. Mathém.*, s. 9, v. 3, 1924, p. 319-343.
30. *L'Analysis Situs et la Géométrie Algébrique (É. Borel Monographs)*, Paris, 1924, vi+154 p.
31. "Intersections of complexes on manifolds," *NAS Proc.*, v. 11, 1925, p. 287-289.
32. "Continuous transformations of manifolds," *NAS Proc.*, v. 11, 1925, p. 290-292.
33. "Intersections and transformations of complexes and manifolds," *AMS Trans.*, v. 28, 1926, p. 1-49.
34. "Transformations of manifolds with a boundary," *NAS Proc.*, v. 12, 1926, p. 737-739.
35. "Un théorème sur les fonctions abéliennes," *In Memoriam N. I. Lobatshevskii*, v. 2. Clavnauka, 1927, p. 186-190.
36. "The residual set of a complex on a manifold and related questions," *NAS Proc.*, v. 13, 1927, p. 614-622, 805-807.
37. "Correspondences between algebraic curves," *AM*, s. 2, v. 28, 1927, p. 342-354.
38. "Manifolds with a boundary and their transformations," *AMS Trans.*, v. 29, 1927, p. 429-462, 848.
39. "On the functional independence of ratios of theta functions," *NAS Proc.*, v. 13, 1927, p. 657-659.
40. "A theorem on correspondences on algebraic curves," *AJM*, v. 50, 1928, p. 159-166.
41. "Closed point sets on a manifold," *AM*, s. 2, v. 29, 1928, p. 232-254.
42. "Transcendental theory"; "Singular correspondences between algebraic curves"; "Hyperelliptic surfaces and Abelian varieties," *Selected Topics in Algebraic Geometry (NRC Bull.*, no. 63), v. 1, 1928, p. 310-395.
43. "Duality relations in topology," *NAS Proc.*, v. 15, 1929, p. 367-369.
44. *Géométrie sur les Surfaces et les Variétés Algébriques (Mém. d. Sci. Mathém.*, no. 40), Paris, 1929, 66 p.
45. "Les transformations continues des ensembles fermés et leurs points fixes," *CR Paris*, v. 190, 1930, p. 99-100.

46. "On transformations of closed sets," *AM*, s. 2, v. 31, 1930, p. 271-280.
47. "On the duality theorems for the Betti members of topological manifolds" (with W. W. Flexner), *NAS Proc.*, v. 16, 1930, p. 530-533.
48. *Topology* (*AMS Colloq. Pub.*, v. 12), 1930, ix+410 p. A 2d ed. in preparation.
49. "On compact spaces," *AM*, s. 2, v. 32, 1931, p. 521-538.
50. "Invariance absolue et invariance relative en géométrie algébrique," *Mat. Sbornik*, v. 39, 1932, no. 3, p. 97-102.
51. "On separable spaces," *AM*, s. 2, v. 33, 1932, p. 525-537.
52. "On certain properties of separable spaces," *NAS Proc.*, v. 18, 1932, p. 202-203.
53. "On analytical complexes" (with J. H. C. Whitehead), *AMS Trans.*, v. 35, 1933, p. 510-517.
54. "On generalized manifolds," *AJM*, v. 55, 1933, p. 469-504.
55. "On singular chains and cycles," *AMS Bull.*, v. 39, 1933, p. 124-129.
56. "On locally connected and related sets," *AM*, s. 2, v. 35, 1934, p. 118-129; 2d paper in *DMJ*, v. 2, 1936, p. 435-442.
57. *Topology* (mimeographed lects.), Inst. for Adv. Study, 1935, [5]+203 p.
58. "Chain-deformations in topology," *DMJ*, v. 1, 1935, p. 1-18.
59. "Application of chain-deformations to critical points and extremals," *NAS Proc.*, v. 21, 1935, p. 220-222.
60. "A theorem on extremals I, II," *NAS Proc.*, v. 21, 1935, p. 272-274, 362-364.
61. "Critical sets," *DMJ*, v. 1, 1935, p. 392-412.
62. "Algebraičeskaja geometrija: metody, problemy, tendentsii," *Trudy Vtorogo Vsesjuznogo Matematičeskogo S'ezda*, Leningrad 24-30 Ijunia 1934, Leningrad, Moscow, v. 1, 1935, p. 337-349.
63. "Sur les transformations des complexes en sphères," *FM*, v. 27, 1936, p. 94-115.
64. "Matematičeskaja defatel'nost' v Prinstone," *Uspekhi Matematičeskikh Nauk*, Moscow, v. 1, 1936, p. 271-273.
65. "Algebraičeskaja geometrija," *Uspekhi Matematičeskikh Nauk*, v. 3, 1937, p. 63-77.
66. *Lectures on Algebraic Geometry 1936-37* (mimeographed lects.), Princeton U., 1937, 69 p.
67. "On the fixed point formula," *AM* 1937, p. 819-822.
68. "The role of algebra in topology," *AMS Bull.*, v. 43, 1937, p. 345-359. AMS ret. P add. 30 Dec. 1936.
69. "On chains of topological spaces," *AM*, v. 39, 1938, p. 383-396.
70. Reviews of books by Severi, Veblen, Kerékjártó, Jung, Sierpinski, and Zariski in *AMS Bull.*, 1922-1936; by Silberstein, Evans, Veblen, W. A. Manning, Shaw, Dickson, Mitchell, Vandiver, Wahlin, Einstein, Steinmetz, Birkhoff, Poor, Eisenhart, Fisher, Rietz, Lovitt, Bliss, White, Curtiss, MacMillan, Ford, Fry, D. Jackson, T. Y. Thomas, R. L. Moore, Ritt, Lane, Hancock, and Morse in *DB*, 1922-1935.

24. ROBERT LEE MOORE

CURRICULUM VITAE.—B. Dallas, Tex. 14 Nov. 1882. Student U. Texas (98-01; Sc.B. 01; fellow 01-02); instr. math. High School, Marshall, Tex. (02-03); student U. Chicago (03-05; Ph.D. 05). Assist. prof. U. Tennessee (05-06); instr. Princeton U. (06-08); instr. Northwestern U. (08-11); U. Pennsylvania (11-16; assist. prof. 16-20); assoc. prof. U. Texas (20-23; prof. 23-).

HONORS.—Assoc. ed. *AMS Trans.*, 14-Jan. 27. Starred *Amer. Men Sci.* 21. VP AMS 23. Colloq. lect. AMS 29. Mem. AMS comm. *Colloq. Pubs.* 29-36; chm. 30-Nov. 33. Mem. NAS 31. Visiting Lect. AMS academic year 31-32. P AMS 37-38.

BIOGRAPHICAL NOTES.—Prof. Moore was the fifth of six children of Charles J. and Louisa Ann (Moore) Moore. His father came from New England and his mother from Kentucky; both were of English descent.



R. L. Moore

1937

We have already noted that President Fine was led to adopt mathematics as a career mainly through the influence of George Bruce Halsted, at one time "instructor in post graduate mathematics" in Princeton U. The same may be said of President R. L. Moore who specialized in mathematics during the regime of Halsted as professor at the U. Texas. R. L. Moore's first publication (Bibl. no. 1) was a neat redundancy proof which he discovered while a graduate student in 1902, and which Halsted published. This led to a delightfully friendly and encouraging letter to R. L. Moore from E. H. Moore, then ed.-in-chief of *AMS Trans.*, who had there published a paper on projective axioms of geometry, a few months earlier.

R. L. Moore has not only achieved success notably by research in fields of importance and current interest, such as foundations of mathematics, analysis situs, point sets, and functions of a real variable, but he has also been a source of inspiration to disciples, particularly those (13) who have written doctor's dissertations under his direction, at the U. Pennsylvania (1916-18), and U. Texas (1922-35), namely: J. R. Kline (U. Pa.), G. H. Hallett, Jr. (U. Pa.), Anna M. Mullikin,¹ R. L. Wilder, R. G. Lubben, G. T. Whyburn, J. H. Roberts, J. L. Dorroh, C. M. Cleveland, C. W. Vickery, E. C. Klipple, R. E. Basye, F. B. Jones. The bibliographies of Whyburn (66 titles) and Wilder (32) were published in *Scripta Mathem.*, v. 4, among those of leading Amer. mathems., not more than 40 years of age. Such National Research Fellows as W. L. Ayres, H. M. Gehman, N. E. Rutt, and L. Zippin (also in *Scripta Mathem.* series) have gone to Texas to work under Moore. Three of his doctors (Kline, Wilder, Whyburn) have given invited addresses before the AMS (*Bull.*, 1928, 1932, 1936). Indeed Moore may almost be thought of as the founder of a "school" in analysis situs. While his Bibliography must here very largely speak for itself, a few comments and references to sources for more detailed discussions may be furnished.

Veblen's "Theory of plane curves in non-metrical analysis situs" (*AMS Trans.*, 1905) is based on axioms in his doctoral diss. Moore showed (Bibl. no. 8) that any plane satisfying these axioms is really metrical in the sense that it contains a system of continuous curves such that, with reference to these curves regarded as straight lines, it is an ordinary Euclidean plane. Of his set of axioms for plane analysis situs (no. 10) Chittenden has written (*AMS Bull.*, v. 33, p. 22): "The importance of the regularly and perfectly separable, therefore metric, spaces in the analysis of continua is indicated by the fact that nine years before the publication of the discoveries of Urysohn, R. L. Moore assumed these properties in the first of a system of axioms for the foundations of plane analysis situs." In no. 13 Moore estab-

¹ Compare Mazurkiewicz, "Remarque sur un théorème de M. Mullikin," *FM*, v. 6, 1924, p. 37.

lished the fact that every space satisfying axioms of the system Σ_1 or the system Σ_2 (of no. 10) is topologically equivalent to an ordinary Euclidean plane. A point set M is said to be arc-wise connected if every two points of M are extremities of a simple continuous arc lying wholly in M . Theorem 15 in no. 10 is to the effect that every domain is arc-wise connected; it was found in no. 11 that every continuous curve is arc-wise connected (also obtained by Mazurkiewicz and Tietze). Still later (no. 51) Moore extended this result and proved that every connected, and connected im Kleinen inner limiting set, is arc-wise connected (also proved by Menger, *MMP*, v. 36, p. 210; see *AMS Bull.*, v. 35, p. 776-777).

In no. 12 it is shown that in order for a simply connected, bounded plane domain R to have a simple closed curve as its boundary, it is necessary and sufficient that R should be uniformly connected im Kleinen. The problem of determining conditions under which the any-to-finite Borel theorem is valid in a space \mathcal{L} was first solved in no. 15 (cf. T. H. Hildebrandt, *AMS Bull.*, v. 32, p. 462; and Frechet, *École Normale Sup., Annales*, v. 38, p. 342 f.). In no. 23 it is shown that if, in a Euclidean space of three dimensions, K is an open curve, and G is a self-compact set of simple open curves such that (i) through each point of k there is only one curve of the set G , (ii) each curve of the set G contains a point k , (iii) no two curves of the set G have a point in common, and (iv) the set of curves G is equi-continuous with respect to every bounded point set; then the point set obtained by adding together all the curves of the set G is a simple open surface.

In no. 32 the notion of upper semi-continuous collection is introduced and in no. 37 it is shown that if G is an upper semi-continuous collection of mutually exclusive compact continua filling up a plane S and no element of G separates S then, with respect to its elements regarded as points, G is topologically equivalent to a plane. In no. 45 the notion of junction point of a continuum is introduced; and in no. 48 the notion of a triodic continuum. The volume of Colloquium Lectures (no. 50) was intended to be a self-contained treatment of the foundations of the point-set theoretic branch of analysis situs and is chiefly concerned with those topics which are the results of Moore's own work (see rev. by Gehman, *AMS Bull.*, v. 39). For a discussion of Moore's papers on separation theorems (no. 36, 43, 44, 46, 47) reference may be made to Kline's report on "Separation theorems and their relation to recent developments in analysis situs" referred to above; the reports of Wilder and Whyburn also discuss some other work of Moore. There are many references to Moore's work in *FM* v. 4-26, especially by Kuratowski, but among other foreigners are Borsuk, Chojnacki, Eilenberg, and Zarankiewicz. The survey of W. Wilkosz, in his *Les Propriétés topologiques du plan Euclidien (Mém. d. Sci. Mathém.*, no. 45) Paris, 1931 may be also mentioned in conclusion.

SOURCES.—*Who's Who in Amer.*, v. 19. *Amer. Men Sci.*, 5th ed. Personal information.

BIBLIOGRAPHY

1. "The betweenness assumptions" [written up by G. B. Halsted], *AMM*, v. 9, 1902, p. 98–101. In this connection compare E. H. Moore, *AMM*, v. 9, 152. See also G. B. Halsted, *Rational Geometry*, second ed., New York, 1907, p. 241–246.
2. "Geometry in which the sum of the angles of every triangle is two right angles," *AMS Trans.*, v. 8, 1907, p. 369–378.
3. "Sets of metrical hypotheses for geometry," *AMS Trans.*, v. 9, 1908, p. 487–512. Doctoral diss.
4. "A note concerning Veblen's axioms for geometry," *AMS Trans.*, v. 13, 1912, p. 74–76.
5. "On Duhamel's theorem," *AM*, s. 2, v. 13, 1912, p. 161–166.
6. "The linear continuum in terms of point and limit," *AM*, s. 2, v. 16, 1915, p. 123–133.
7. "On the linear continuum," *AMS Bull.*, v. 22, 1915, p. 117–122.
8. "On a set of postulates which suffice to define a number-plane," *AMS Trans.*, v. 16, 1915, p. 27–32.
9. "Concerning a non-metrical pseudo-Archimedean axiom," *AMS Bull.*, v. 22, 1916, p. 225–236.
10. "On the foundations of plane analysis situs," *AMS Trans.*, v. 17, 1916, p. 131–164; brief summary in *NAS Proc.*, v. 2, 1916, p. 270–272.
11. "A theorem concerning continuous curves," *AMS Bull.*, v. 23, 1917, p. 233–236.
12. "A characterization of Jordan regions by properties having no reference to their boundaries," *NAS Proc.*, v. 4, 1918, p. 364–370.
13. "Concerning a set of postulates for plane analysis situs," *AMS Trans.*, v. 20, 1919, p. 169–178.
14. "Continuous sets that have no continuous sets of condensation," *AMS Bull.*, v. 25, 1919, p. 174–176.
15. "On the most general class L of Fréchet in which the Heine-Borel-Lebesgue theorem holds true," *NAS Proc.*, v. 5, 1919, p. 206–210.
16. "On the most general plane closed point-set through which it is possible to pass a simple continuous arc" (with J. R. Kline), *AM*, s. 2, v. 20, 1919, p. 218–223.
17. "On the Lie-Riemann-Helmholtz-Hilbert problem of the foundations of geometry," *AJM*, v. 41, 1919, p. 299–319.
18. "Concerning simple continuous curves," *AMS Trans.*, v. 21, 1920, p. 333–347.
19. "Concerning certain equicontinuous systems of curves," *AMS Trans.*, v. 22, 1921, p. 41–55.
20. "Concerning connectedness im Kleinen and a related property," *FM*, v. 3, 1922, p. 232–237.
21. "Concerning continuous curves in the plane," *MZ*, v. 15, 1922, p. 254–260.
22. "On the relation of a continuous curve to its complementary domains in space of three dimensions," *NAS Proc.*, v. 8, 1922, p. 33–38.
23. "On the generation of a simple surface by means of a set of equicontinuous curves," *FM*, v. 4, 1923, p. 106–117.
24. "Concerning the cut-points of continuous curves and of other closed and connected point sets," *NAS Proc.*, v. 9, 1923, p. 101–106.
25. "An uncountable, closed, and non-dense point set each of whose complementary intervals abuts on another one at each of its ends," *AMS Bull.*, v. 29, 1923, p. 49–50.
26. "Report on continuous curves from the viewpoint of analysis situs," *AMS Bull.*, v. 29, 1923, p. 289–302.
27. "Concerning the sum of a countable number of mutually exclusive continua in the plane," *FM*, v. 6, 1924, p. 189–202.
28. "Concerning the common boundary of two domains," *FM*, v. 6, 1924, p. 203–213.
29. "Concerning relatively uniform convergence," *AMS Bull.*, v. 30, 1924, p. 504–505.
30. "An extension of the theorem that no countable point set is perfect," *NAS Proc.*, v. 10, 1924, p. 168–170.

31. "Concerning the prime parts of certain continua which separate the plane," *NAS Proc.*, v. 10, 1924, p. 170-175.
32. "Concerning upper semi-continuous collections of continua which do not separate a given continuum," *NAS Proc.*, v. 10, 1924, p. 356-360.
33. "Concerning sets of segments which cover a point set in the Vitali sense," *NAS Proc.*, v. 10, 1924, p. 464-467.
34. "Concerning the prime parts of a continuum," *MZ*, v. 22, 1925, p. 307-315.
35. "A characterization of a continuous curve," *FM*, v. 7, 1925, p. 302-307.
36. "Concerning the separation of point sets by curves," *NAS Proc.*, v. 11, 1925, p. 469-476.
37. "Concerning upper semi-continuous collections of continua," *AMS Trans.*, v. 27, 1925, p. 416-428.
38. "Concerning the relation between separability and the proposition that every uncountable point set has a limit point," *FM*, v. 8, 1926, p. 189-192.
39. "Conditions under which one of two given closed linear point sets may be thrown into the other one by a continuous transformation of a plane into itself," *AJM*, v. 48, 1926, p. 67-72.
40. "Covering theorems," *AMS Bull.*, v. 32, 1926, p. 275-282.
41. "A connected and regular point set which contains no arc," *AMS Bull.*, v. 32, 1926, p. 331-332.
42. "Concerning indecomposable continua and continua which contain no subsets that separate the plane," *NAS Proc.*, v. 12, 1926, p. 359-363.
43. "Concerning paths that do not separate a given continuous curve," *NAS Proc.*, v. 12, 1926, p. 745-753.
44. "Some separation theorems," *NAS Proc.*, v. 13, 1927, p. 711-716.
45. "Concerning triods in the plane and the junction points of plane continua," *NAS Proc.*, v. 14, 1928, p. 85-88.
46. "On the separation of the plane by a continuum," *AMS Bull.*, v. 34, 1928, p. 303-306.
47. "A separation theorem," *FM*, v. 12, 1928, p. 295-297.
48. "Concerning triodic continua in the plane," *FM*, v. 13, 1929, p. 261-263.
49. "Concerning upper semi-continuous collections," *MMP*, v. 36, 1929, p. 81-88.
50. *Foundations of Point Set Theory* (*AMS Colloq. Pub.*, v. 13), 1932, vii+486 p.
51. "Concerning compact continua which contain no continuum that separates the plane," *NAS Proc.*, v. 20, 1934, p. 41-45.
52. "A set of axioms for plane analysis situs," *FM*, v. 25, 1935, p. 13-28.
53. "Fundamental theorems concerning point sets: I, Foundations of a point set theory of spaces in which some points are contiguous to others; II, Upper semi-continuous collections of the second type; III, On the structure of continua," *RI Pamphlets*, v. 23, 1936, p. 1-74.
54. "Concerning essential continua of condensation," *AMS Trans.*, v. 42, 1937, p. 41-52.
55. Review of a book by Veblen and Young in *AMS Bull.*, 1920.